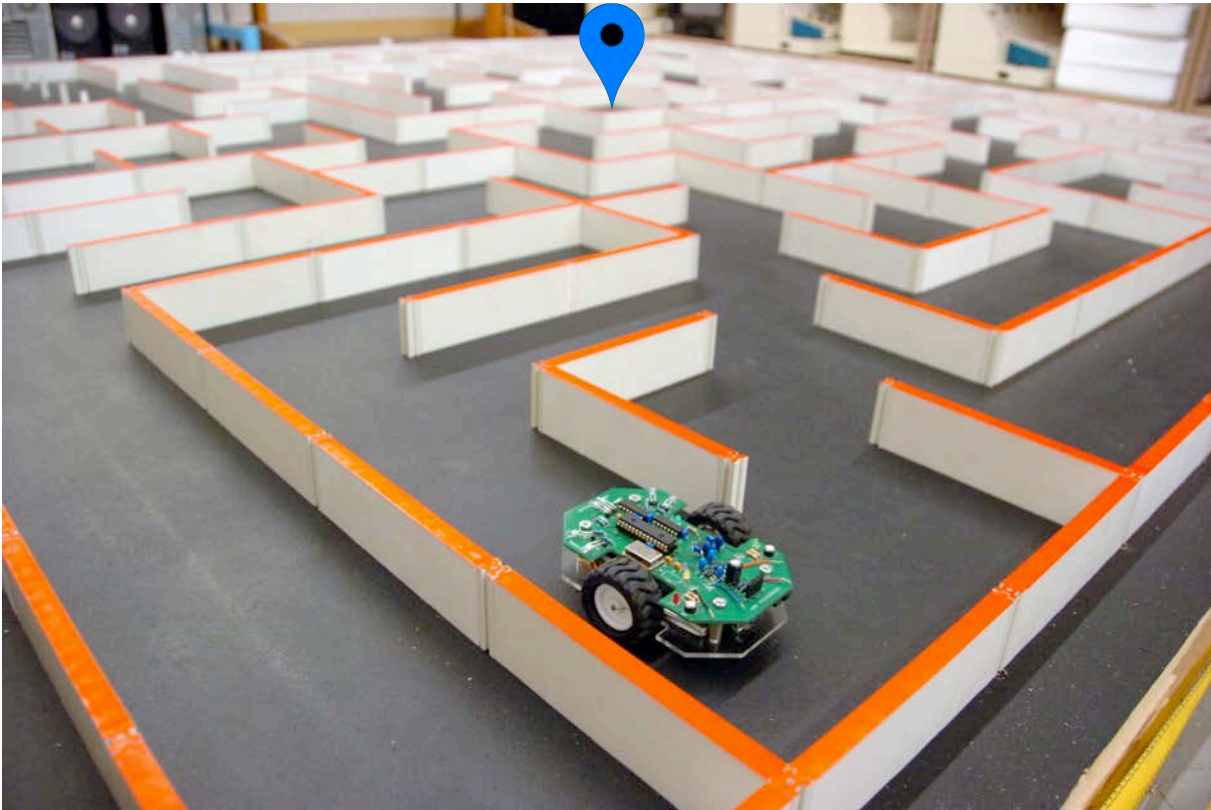


Autonomous Navigation: Global Search



<https://app.emaze.com/@AIRRTROT/idea-2-the-robot-maze#1>

Robotics 102
Introduction to AI and Programming
University of Michigan and Berea College
Fall 2021

Michigan Robotics 102 - robotics102.org

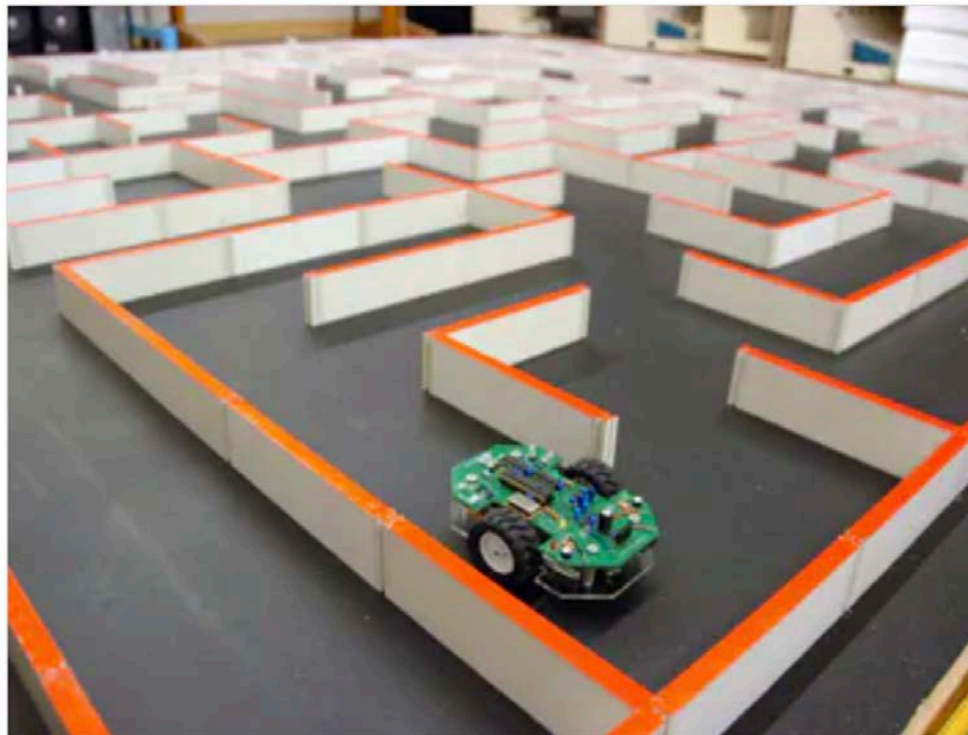


Jordan Wong
Published June 19, 2015

IEEE Micromouse

Autonomous mouse that can traverse any 16 by 16 maze.

 Intermediate  Full instructions provided  1,762



<https://www.hackster.io/jordanjameswong/micromouse-83dab7>



2011 All Japan micromouse contest: Ng BengKiat 4th Fast RUN
<https://www.youtube.com/watch?v=CLwICJKV4dw>

micromouse run

Privacy, simplified.

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All regions Safe search: moderate Any time All sizes All colors All types All layouts All Licenses

1280 x 720

Micromouse "Venus" - Official Search Run - YouTube.com

480 x 360

micromouse test run 23 - YouTube.com

1280 x 720

micromouse test run 22 - YouTube.com

1280 x 720

2012 Californima Micromouse Competition 1... youtube.com

1280 x 720

Micromouse Practice Run - YouTube.com

1280 x 720

[4K] Practice Run for Micromouse GreenGiant 5... youtube.com

480 x 360

vacuum_micromouse_test_run - YouTube.com

1280 x 720

Micromouse "Xiphosura" - Test Run - YouTube.com

1280 x 720

IEEE Micromouse "Run For Your Money" - Full Test ... youtube.com

723 x 1024

2013 All Japan Mic... micromouseusa.com

480 x 360

micromouse test run 17 - YouTube.com

3718 x 2092

IEEE Micromouse "Run For Your Money" - My pr... reddit.com

1280 x 720

Micromouse Green Giant 5.10V run a 2016 All A... youtube.com

1280 x 720

CSU Chico Micromouse Final Run on Vimeo vimeo.com

480 x 360

micromouse test run 18 - YouTube.com

Share Feedback

Our goal

Our goal

Give you the power of autonomous navigation



Our goal

Give you the power of autonomous navigation



Our goal

Give you the power of autonomous navigation



Autonomous Navigation



Goal location



Start location

Autonomous Navigation by global search



Goal location

***Think of our robot's navigation
as solving a maze***



Start location

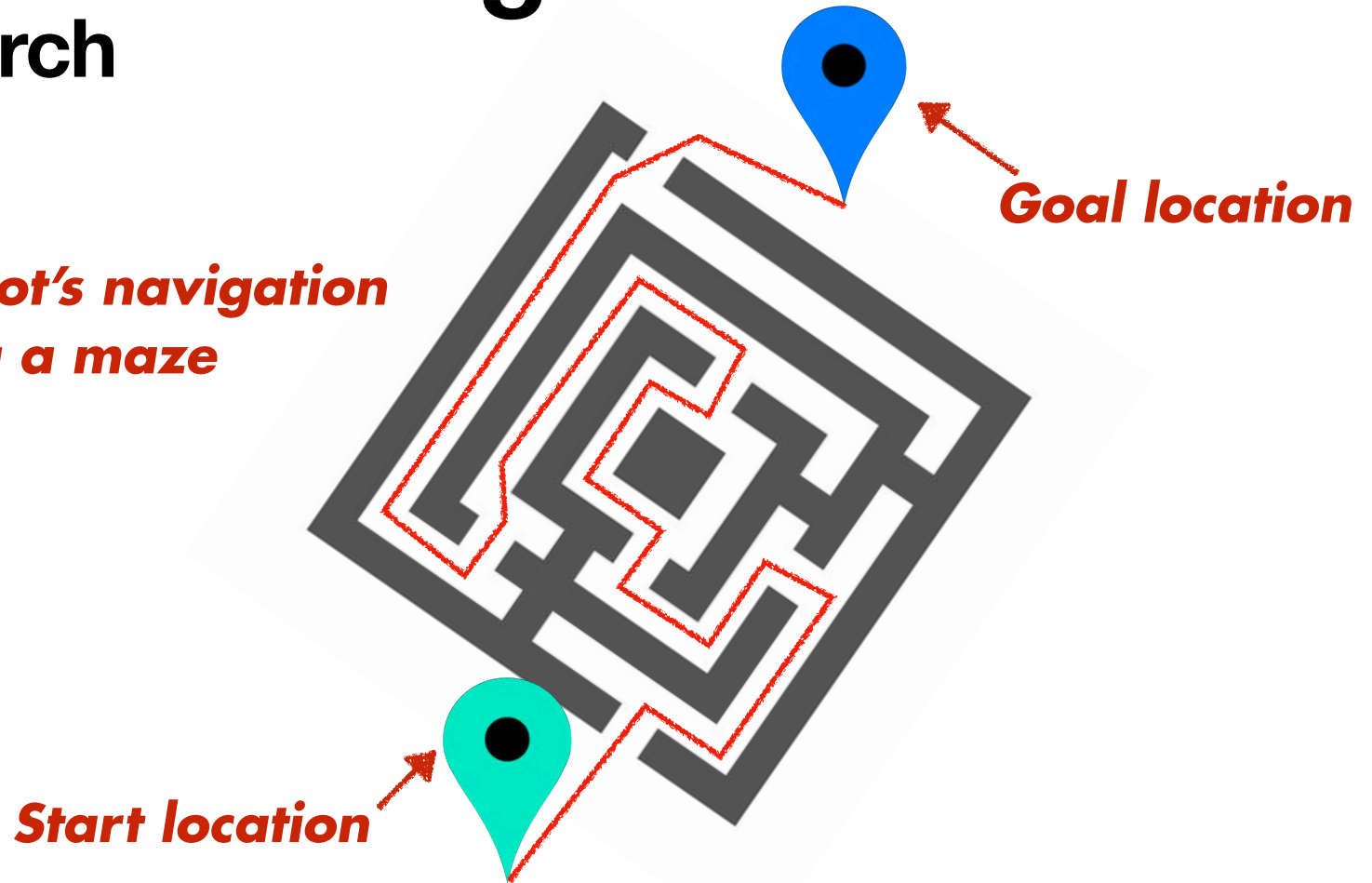
Autonomous Navigation by global search

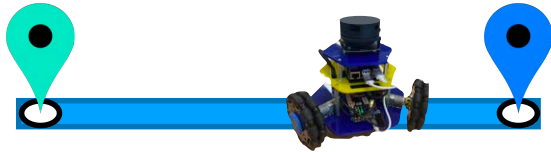
*Think of our robot's navigation
as solving a maze*



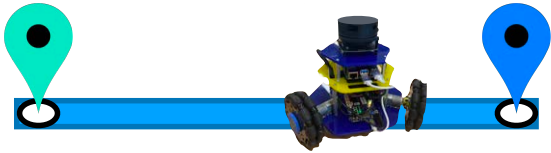
Autonomous Navigation by global search

*Think of our robot's navigation
as solving a maze*



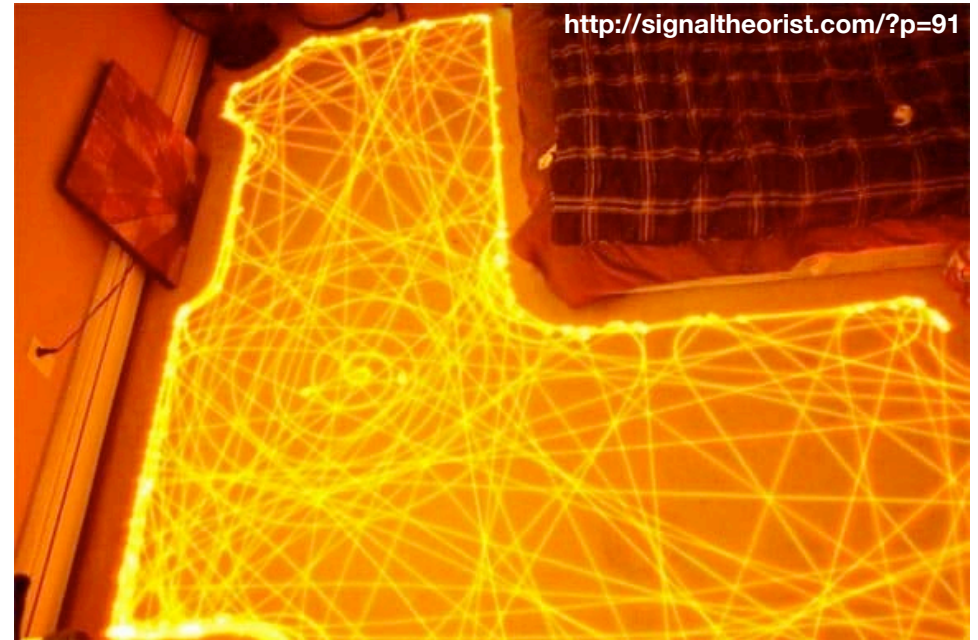


What options do we have for navigating our robot?

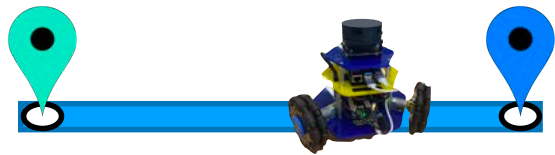


What options do we have for navigating our robot?

Just move randomly



Random walk algorithms



What options do we have for navigating our robot?

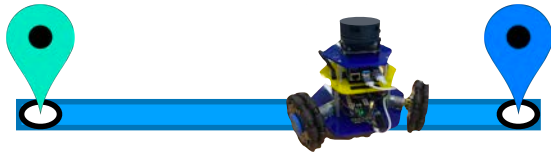
Just move randomly

Follow wall to goal



Bug algorithms

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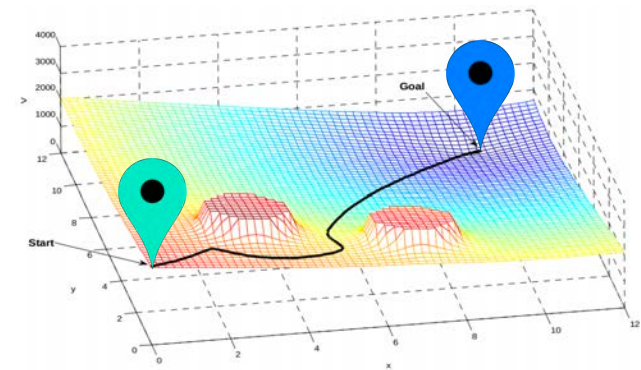
Just move randomly

Follow wall to goal

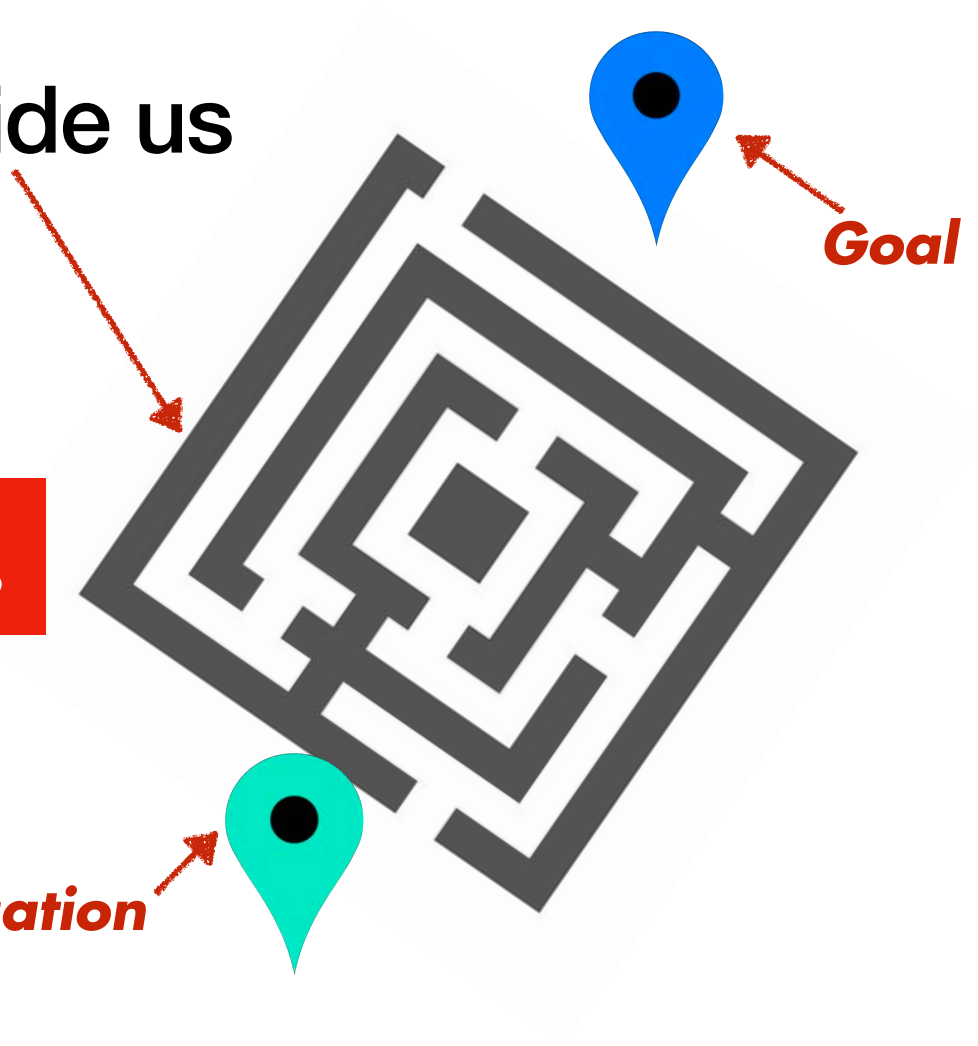
Build a map to guide us

Project 2: Potential Fields

Autonomous
navigation to a
goal location



Build a map to guide us



Goal location

What path would a potential field produce?

Start location

Build a map to guide us

What path would a potential field produce?

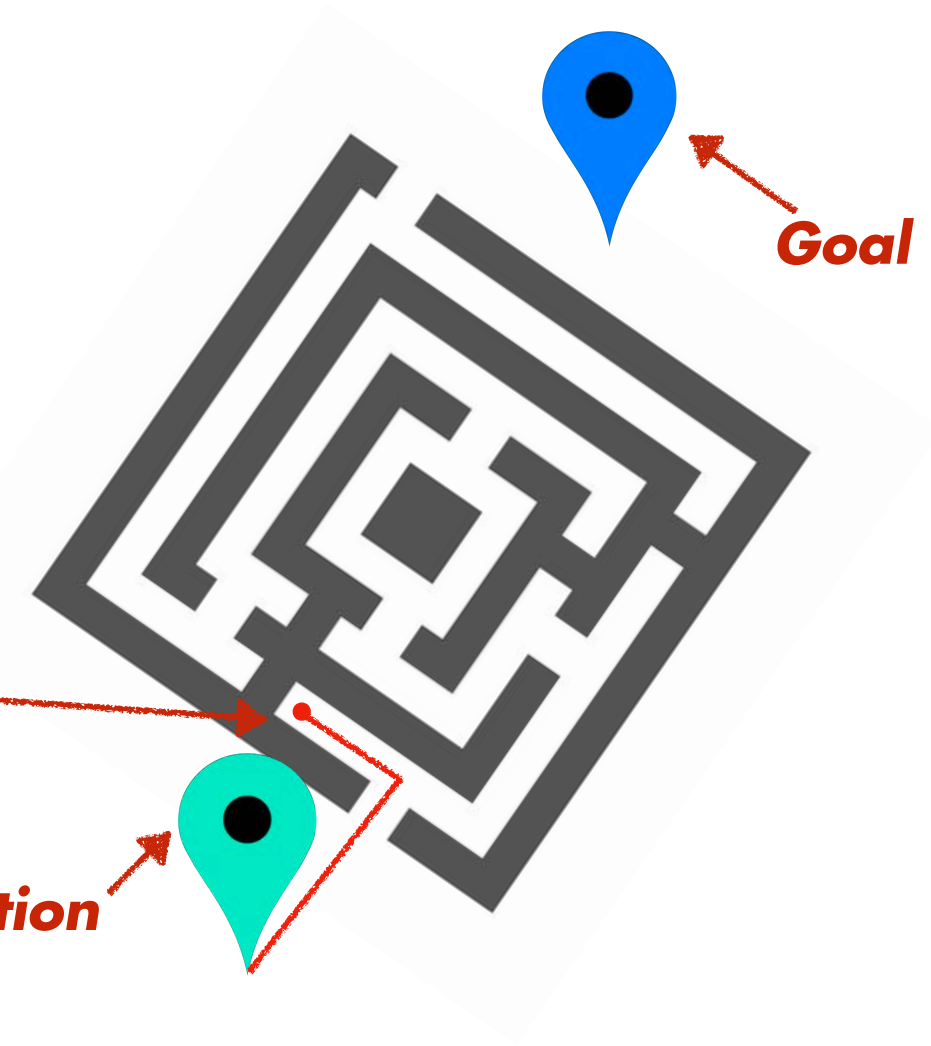


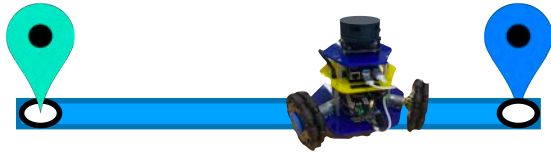
What path would a potential field produce?

**Local minimum
(or dead end)**

Start location

Goal location



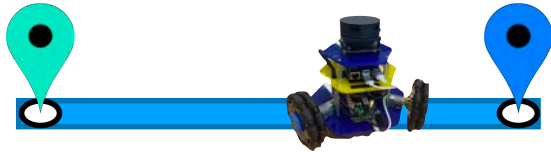


What options do we have for navigating our robot?

Just move randomly

Follow wall to goal

Build a map to guide us



Just move randomly

Follow wall to goal

Build a map to guide us

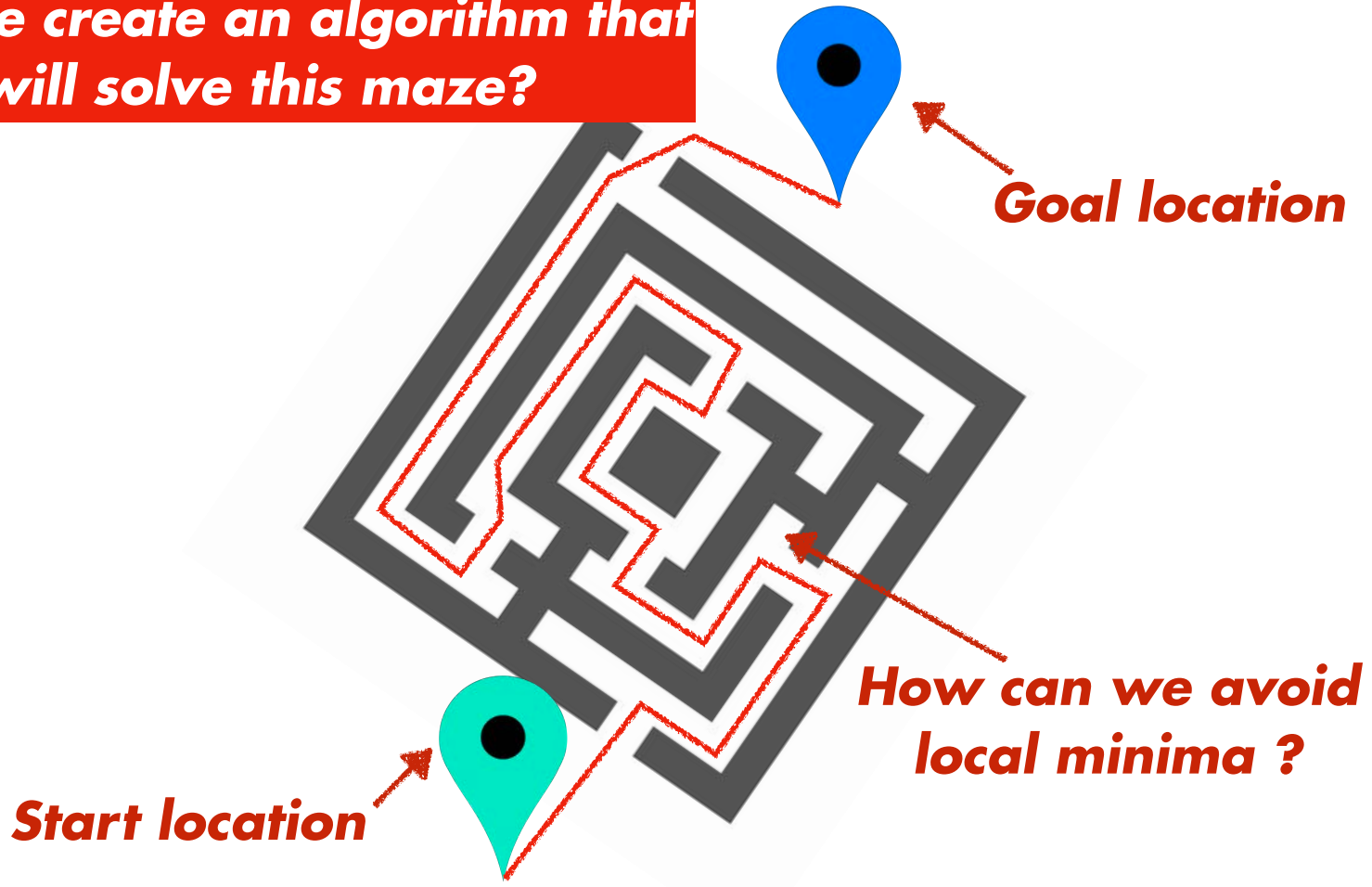
Consider all possible paths

Project 3: A* Pathfinding

Autonomous
navigation to a
goal location

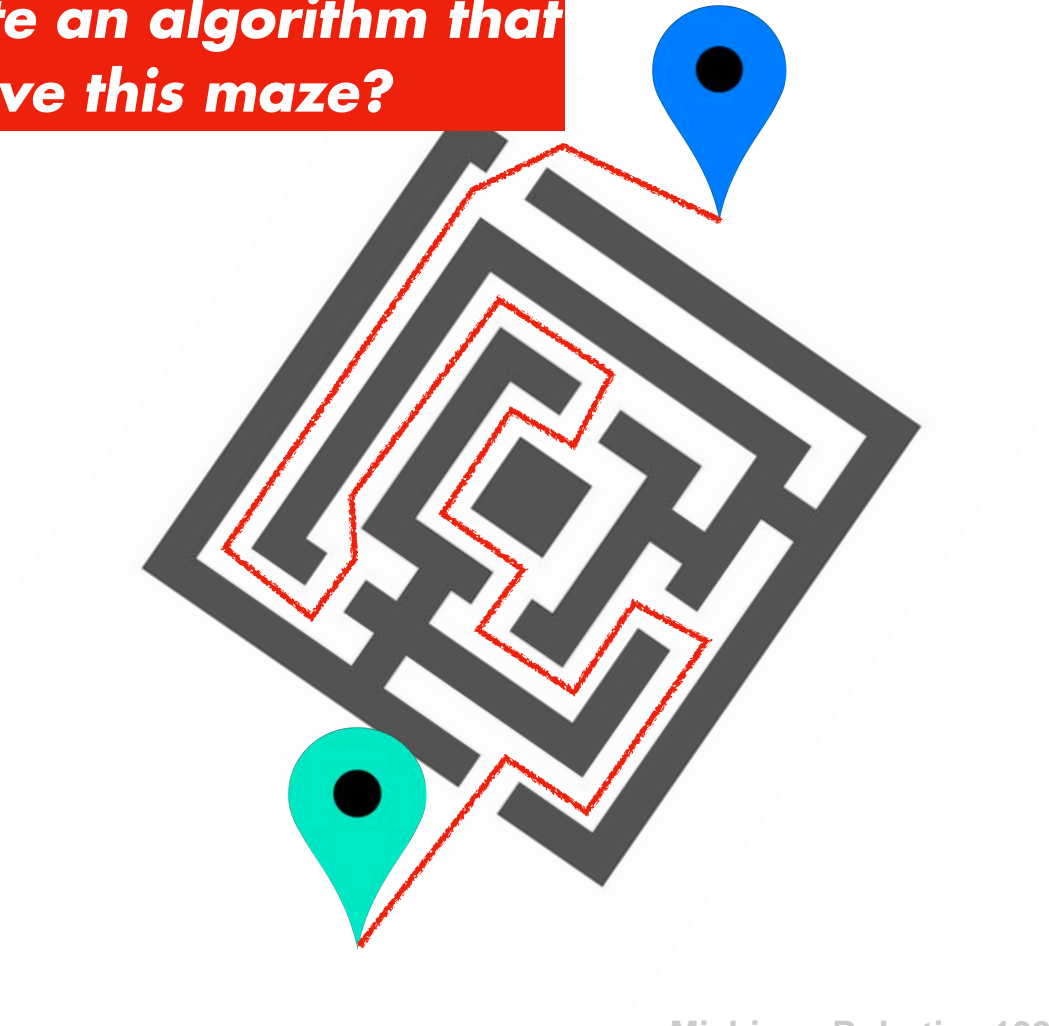
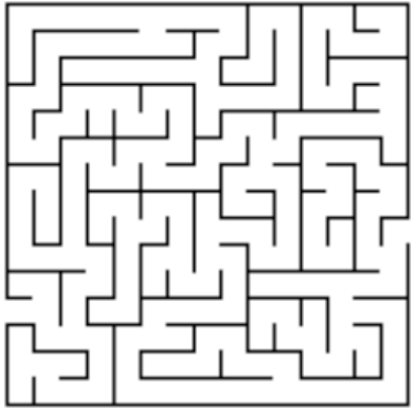


Can we create an algorithm that will solve this maze?



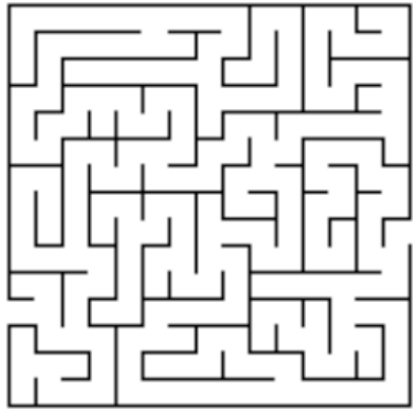
Can we create an algorithm that will solve this maze?

and this one?



Can we create an algorithm that will solve this maze?

and this one?

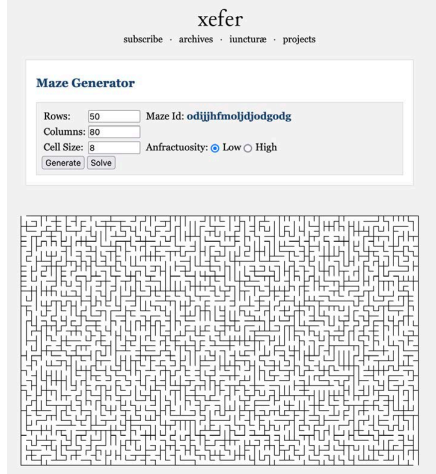


and this one?

xefer
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Maze Generator

Rows: Maze Id: odijjhfmljodjodgdg
Columns:
Cell Size: Anfractuosity: Low High

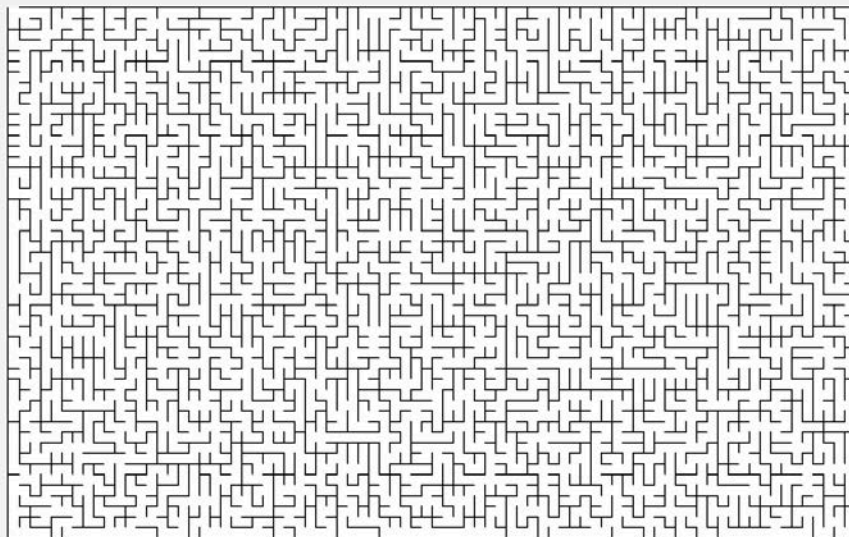


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Maze Generator

Rows: Maze Id: **odijhfmoljdjodgodg**
Columns:
Cell Size: Anfractuosity: Low High



<https://www.xefer.com/maze-generator>

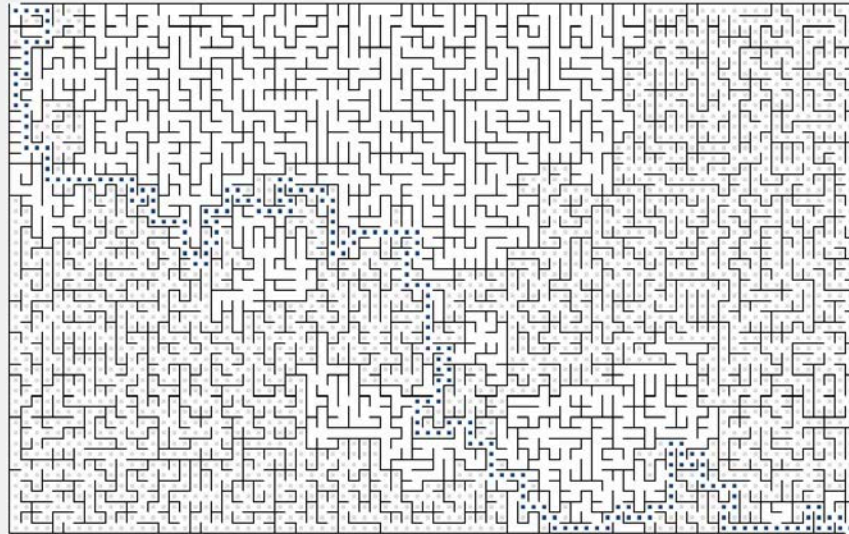
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Maze Generator

Rows: Maze Id: **odijjhfmojldjodgodg**
Columns:
Cell Size: Anfractuosity: Low High



How does this algorithm work?

<https://www.xefer.com/maze-generator>

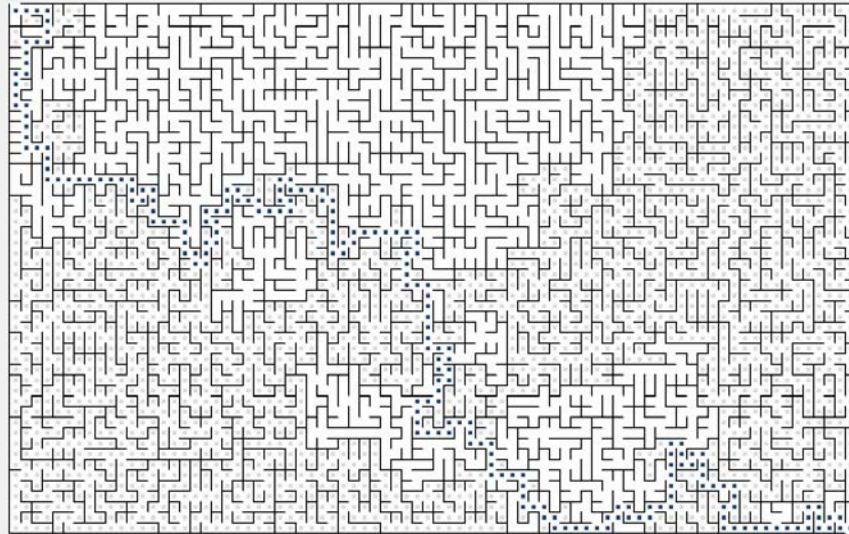
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Maze Generator

Rows: Maze Id: **odijjhfmojldjodgodg**
Columns:
Cell Size: Anfractuosity: Low High



How does this algorithm work?

Represent the map as a graph

<https://www.xefer.com/maze-generator>

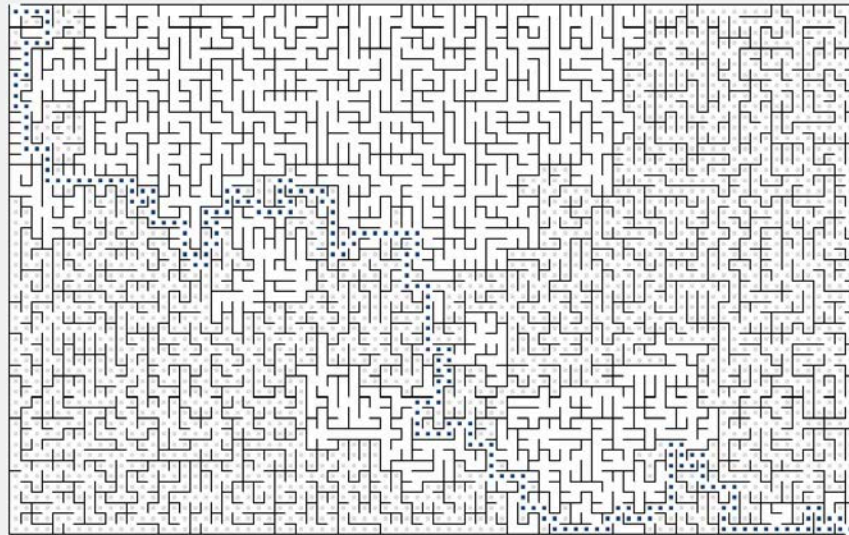
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Maze Generator

Rows: Maze Id: **odijjhfmojldjodgodg**
Columns:
Cell Size: Anfractuosity: Low High



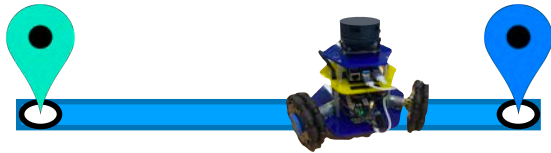
How does this algorithm work?

Represent the map as a graph

Search over all possible paths

<https://www.xefer.com/maze-generator>

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Just move randomly

Follow wall to goal

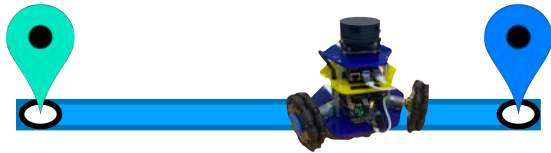
Build a map to guide us

Consider ***Search over all possible paths*** all paths

Project 3: A* Pathfinding

Autonomous
navigation to a
goal location





Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths

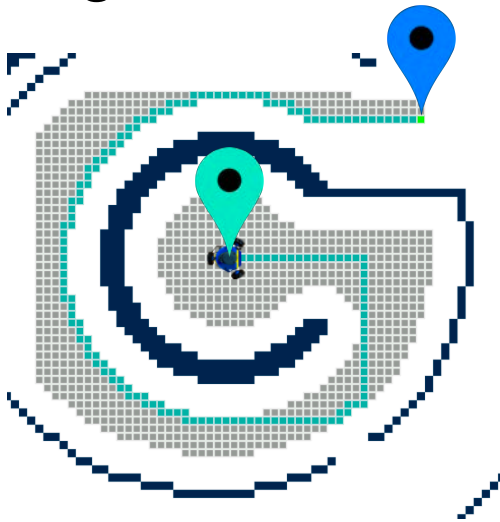
Project 3: A* Pathfinding

Autonomous
navigation to a
goal location



Project 3: A* Pathfinding

Autonomous
navigation to a
goal location



Search over all possible paths

Already done from Project 2

- Build map of environment
- Represent map as graph with a grid layout
- Store parent of each node
along route to start location
- Store path distance at each node
along route to start location
- Global search to find routing

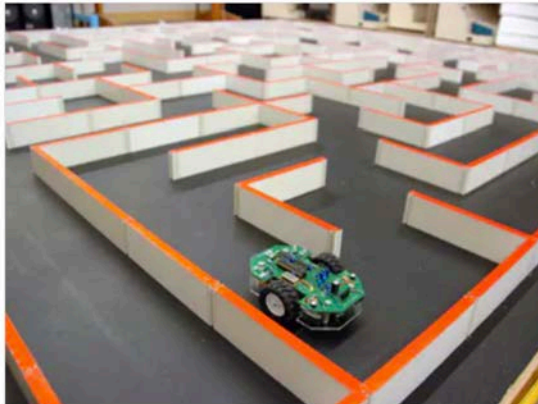
Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Jordan Wong
Published June 19, 2015

IEEE Micromouse

Autonomous mouse that can traverse any 16 by 16 maze.

Intermediate Full instructions provided 1,762



Micro Mouse Flood Fill Algorithm Demo

Maze Editing Tools
Erase wall
Add wall

CUHK
Micromouse
Flood Fill
Algorithm Demo
2003
Designed by MY Wong

Load Maze
Save Maze
Reset
Start

Show Value Maze
 Show Value Maze 2
 Blank
 Show Given Maze

Speed Control
High Low

<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:



<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

Provides cell-to-cell routing along found path



<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

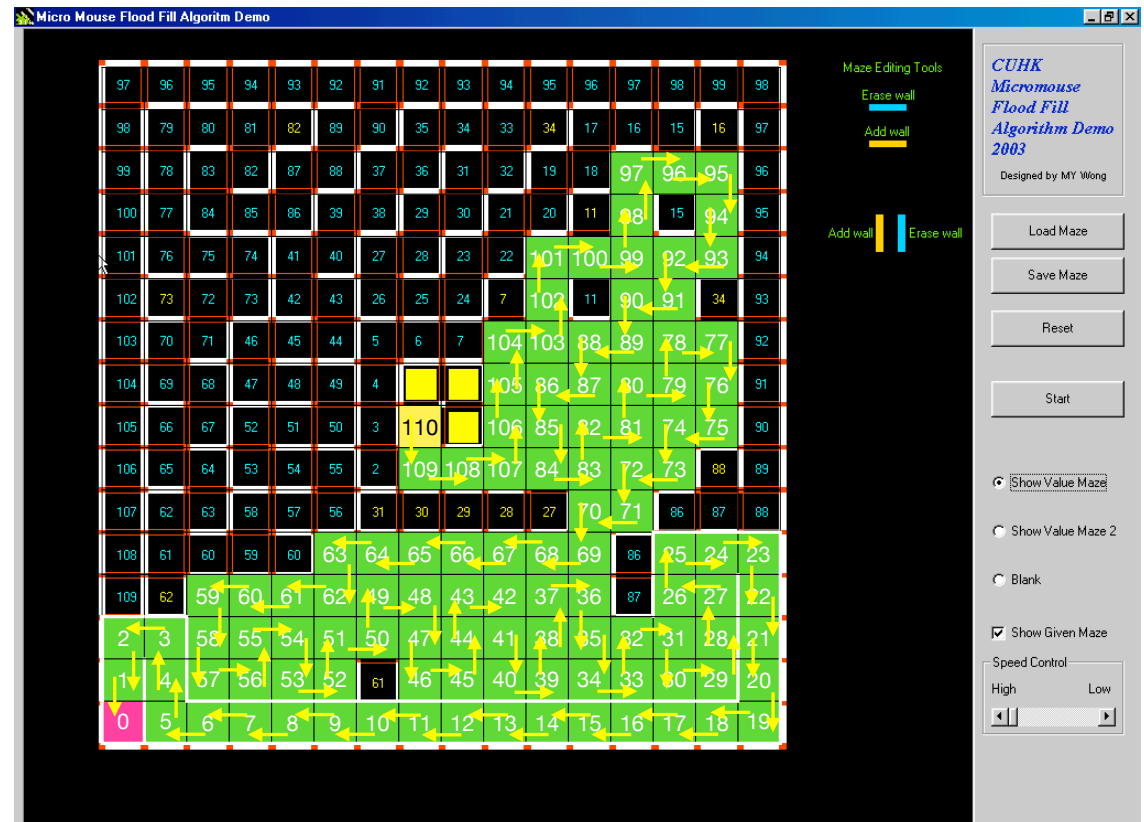
Michigan Robotics 102 - robotics102.org

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

Provides cell-to-cell routing along found path

Distance along path at each cell



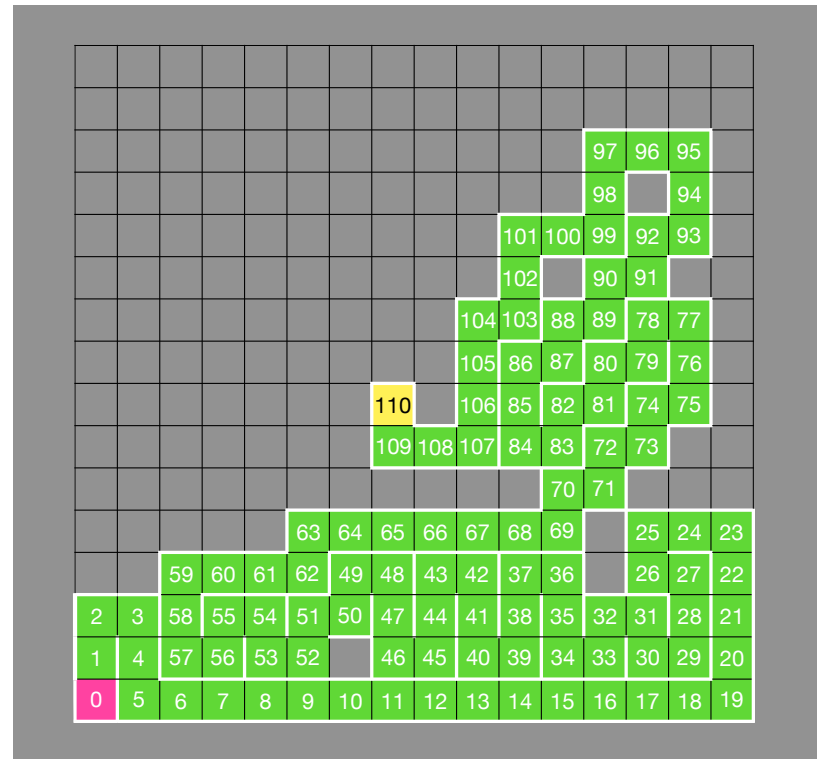
<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

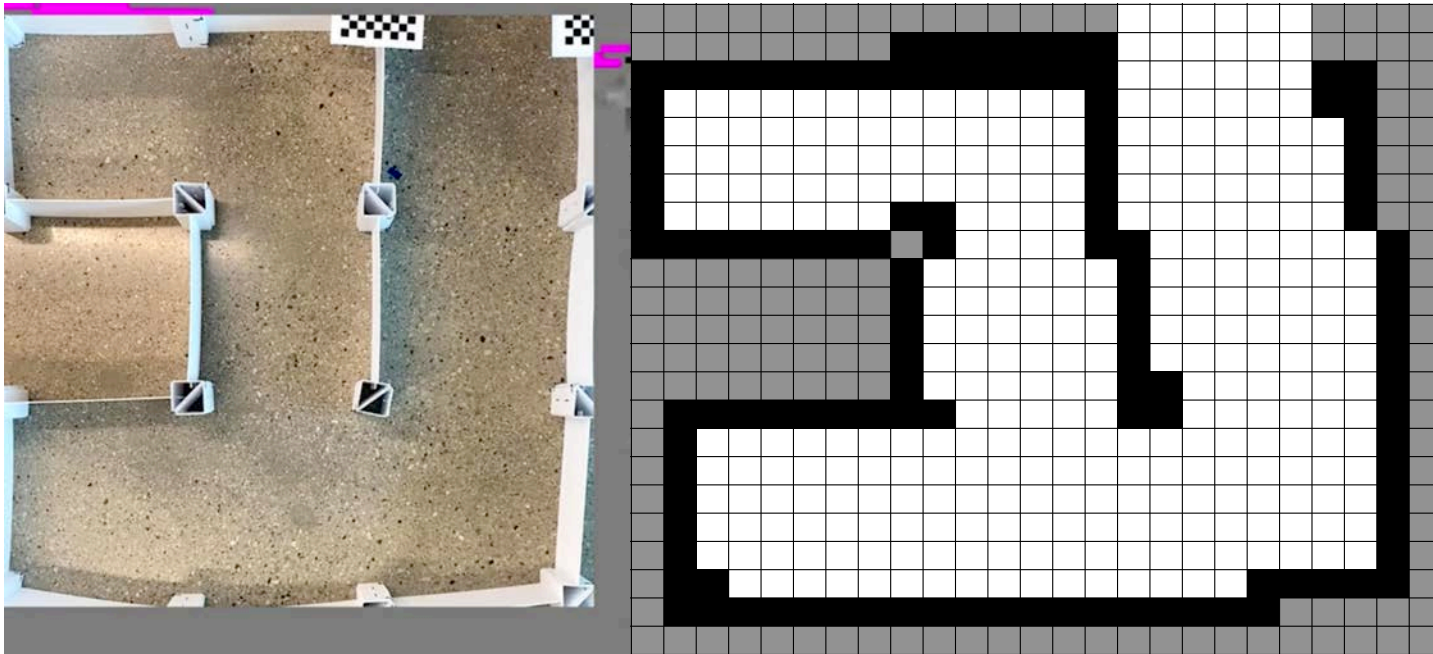
Provides cell-to-cell routing along found path

Distance along path at each cell



**Remember what this graph looks
like for our robot maps**

***Robot map is stored as an image
and represented as a graph***

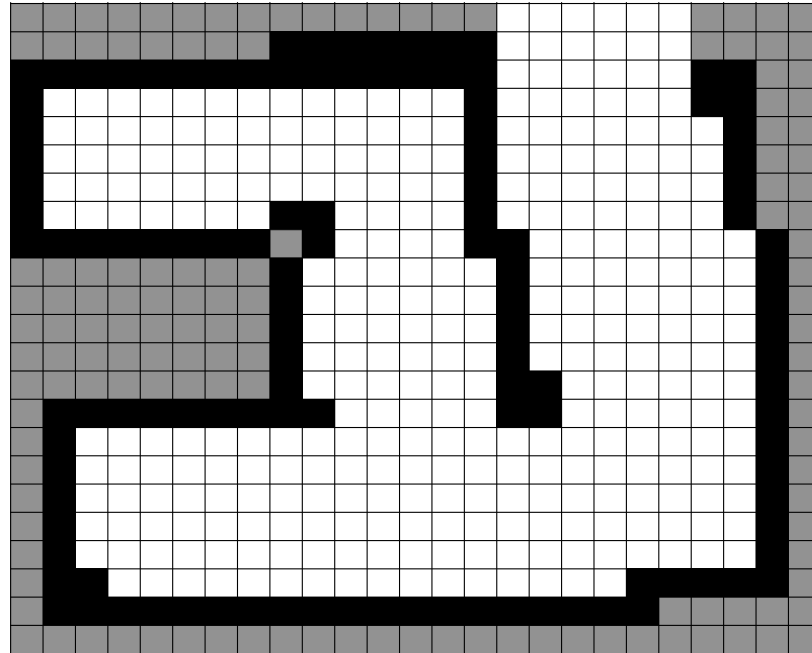


Real world

SLAM output

***Robot map is stored as an image
and represented as a graph***

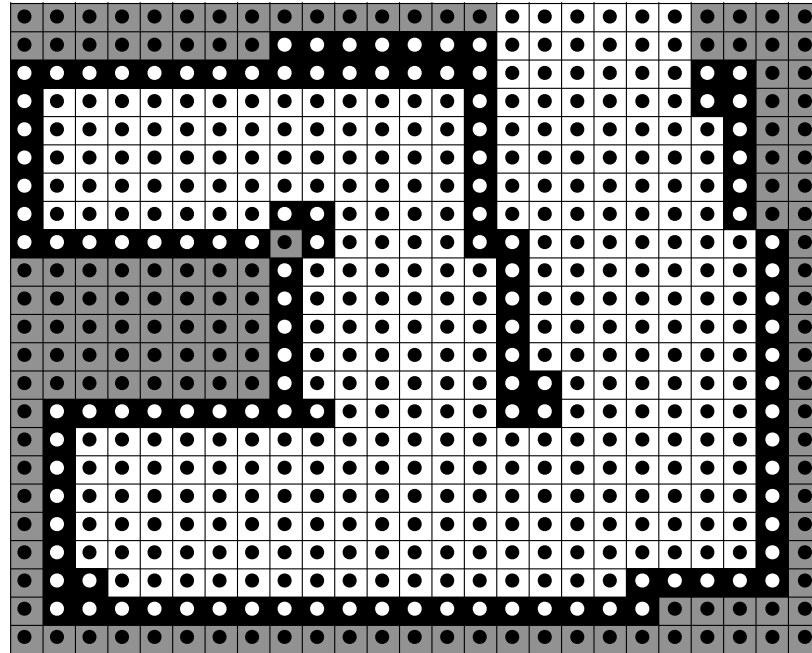
***A vector of cells over
robot locations***



***Robot map is stored as an image
and represented as a graph***

***A vector of cells over
robot locations***

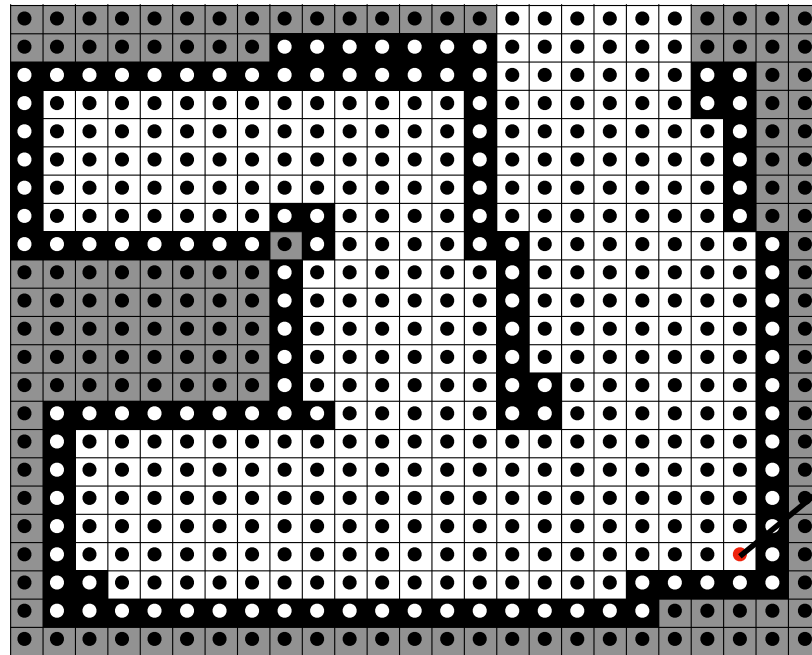
***Every cell has a
node in the graph***



**Robot map is stored as an image
and represented as a graph**

**A vector of cells over
robot locations**

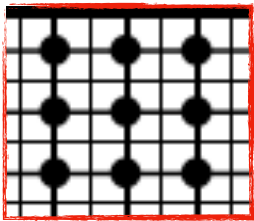
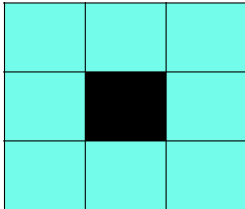
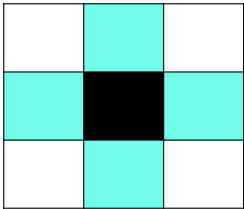
**Every cell has a
node in the graph**



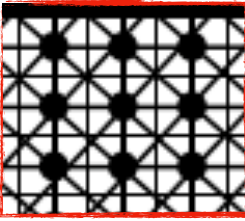
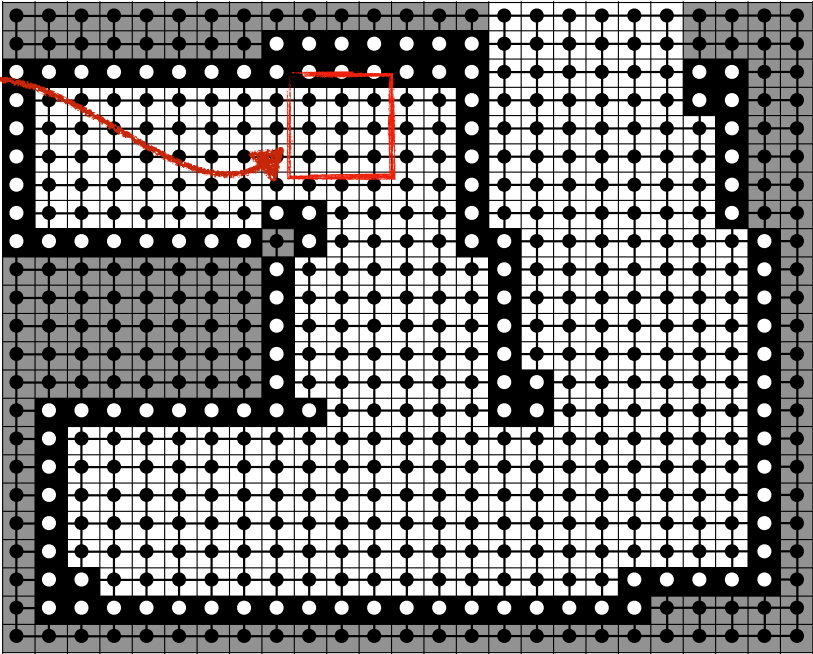
```
origin_x: 2.2  
origin_y: 0.3  
occupied: false
```

**A graph node
stores a struct of
information about
the cell**

Grid graphs are typically either 4-connected or 8-connected

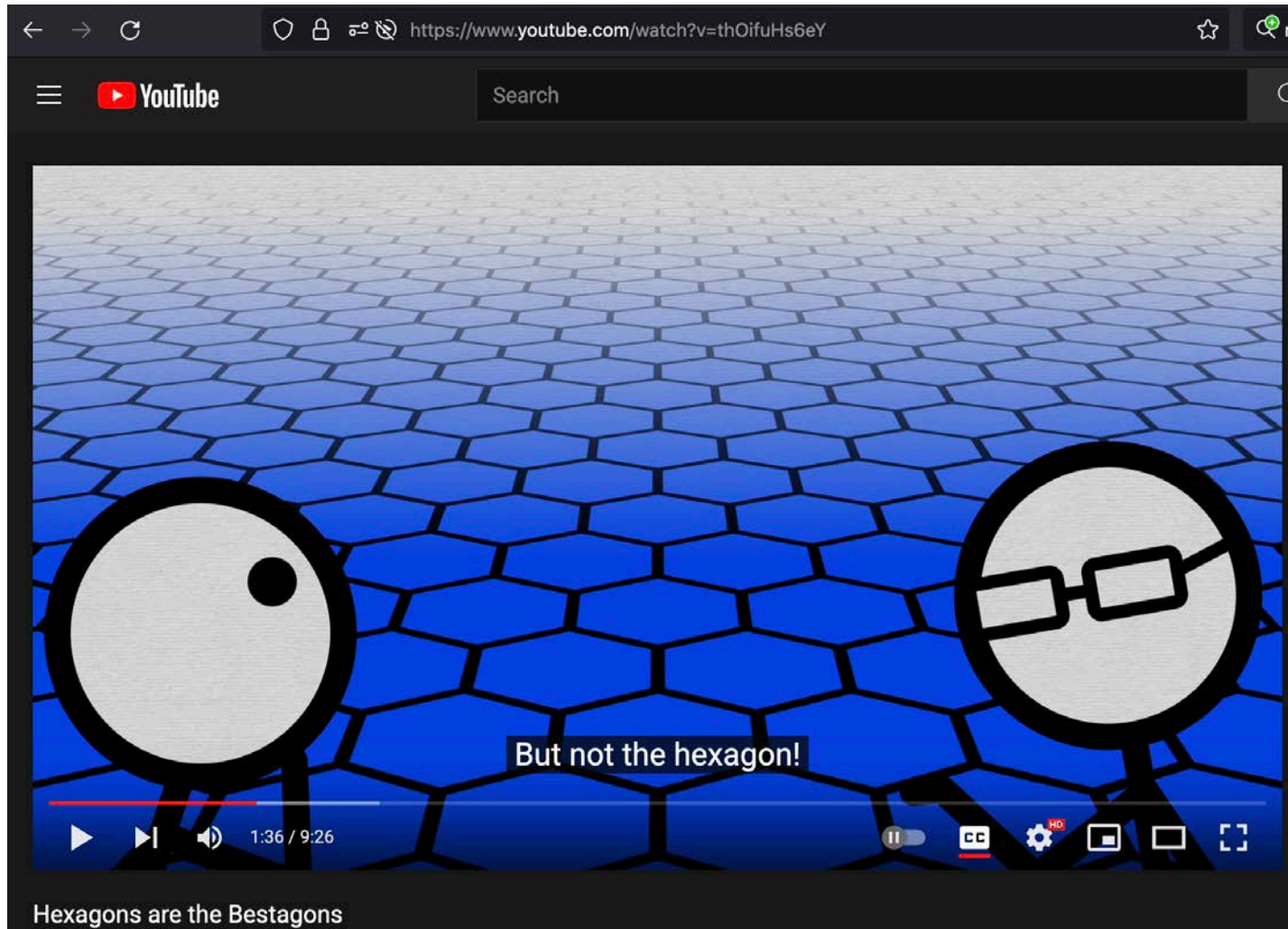


"NSEW"



Diagonals included

Quick tangent: Why are hexagons the bestagons ?

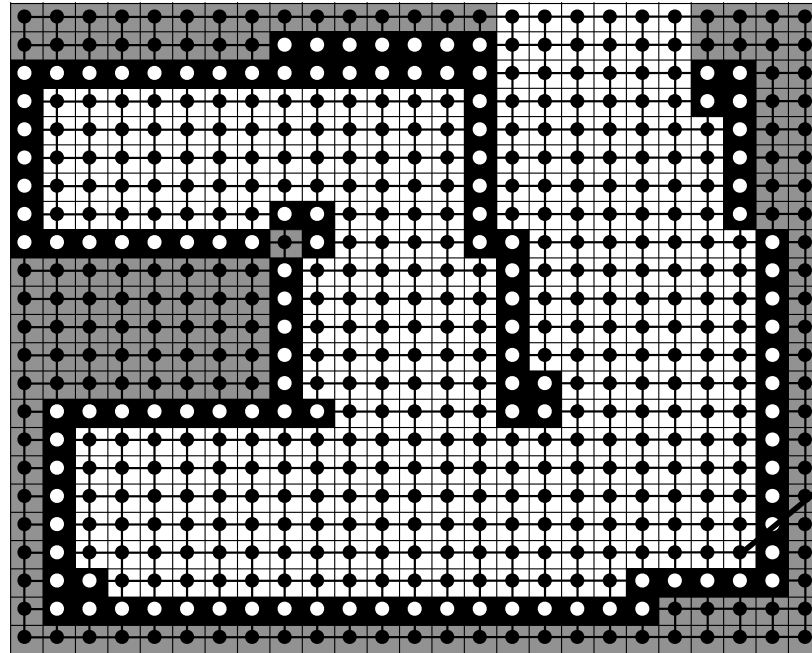


- ❑ Store parent of each node along route to start location
- ❑ Store path distance at each node along route to start location

Path expressed as the route to navigate at a node

```
origin_x: 2.2  
origin_y: 0.3  
occupied: false  
parent: ??  
distance: ??
```

A graph node stores a struct of information about the cell

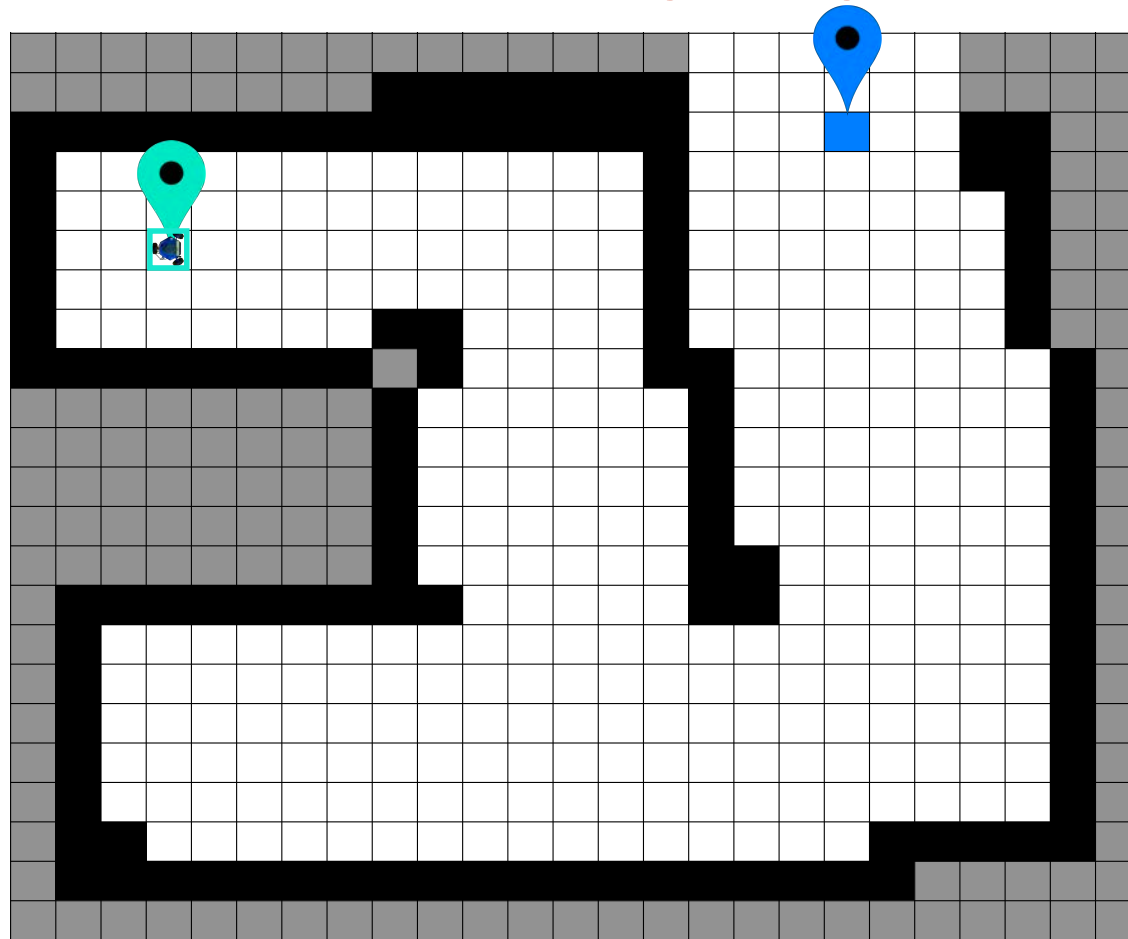


A vector of cells over robot locations

Every cell has a node in the graph

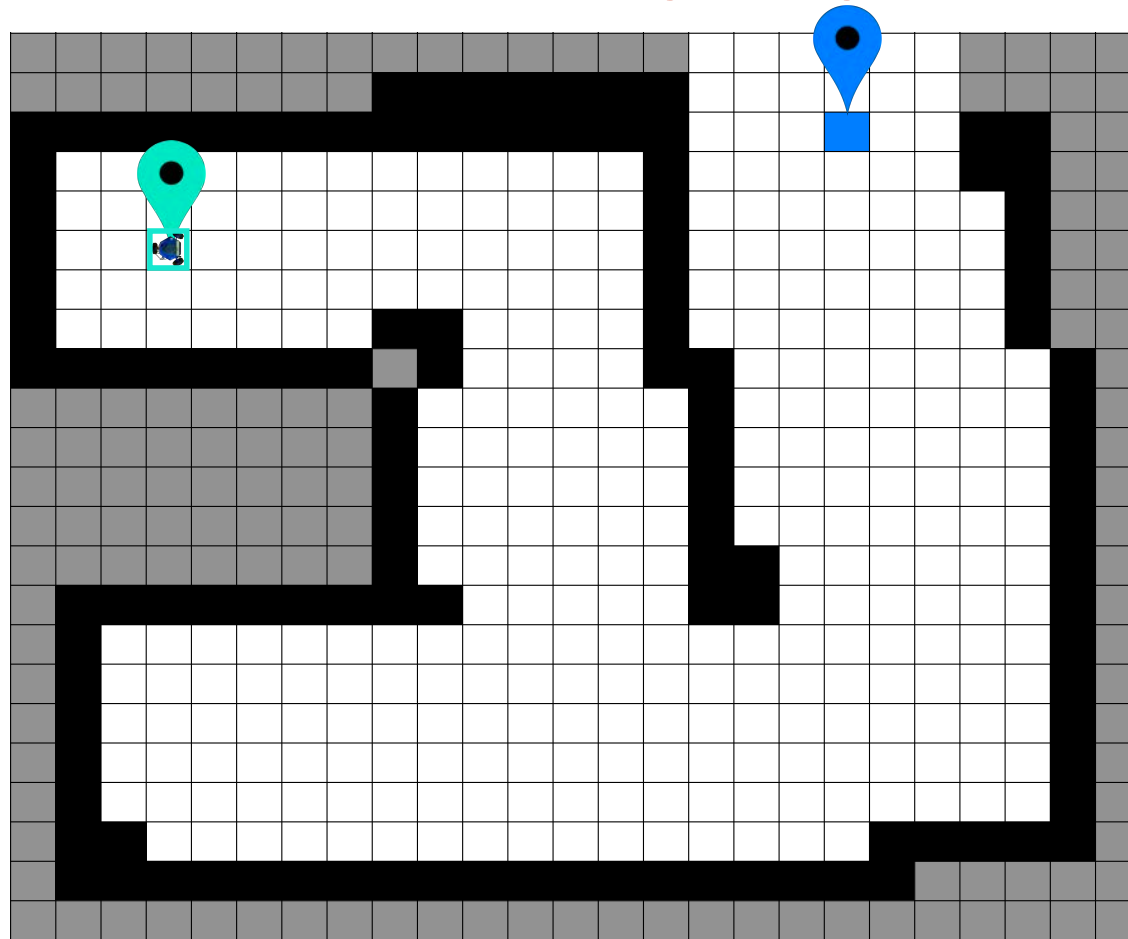
Every pair of neighboring cells shares an edge in the graph

Assume robot planning a route from a given start location to a given goal location



How does Floodfill compute .parent and .distance for each node?

Assume robot planning a route from a given start location to a given goal location

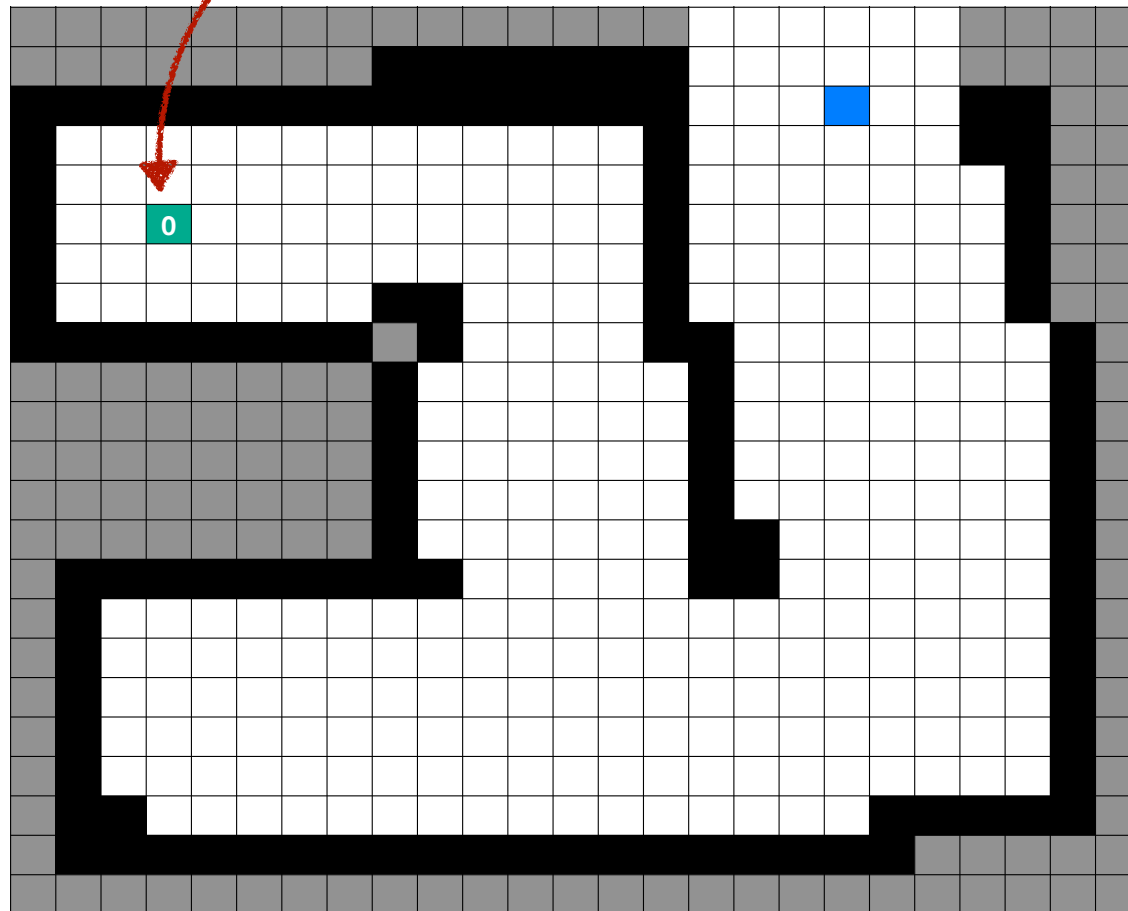


How does Floodfill compute .parent and .distance for each node?

Grow outward from the node at the start location

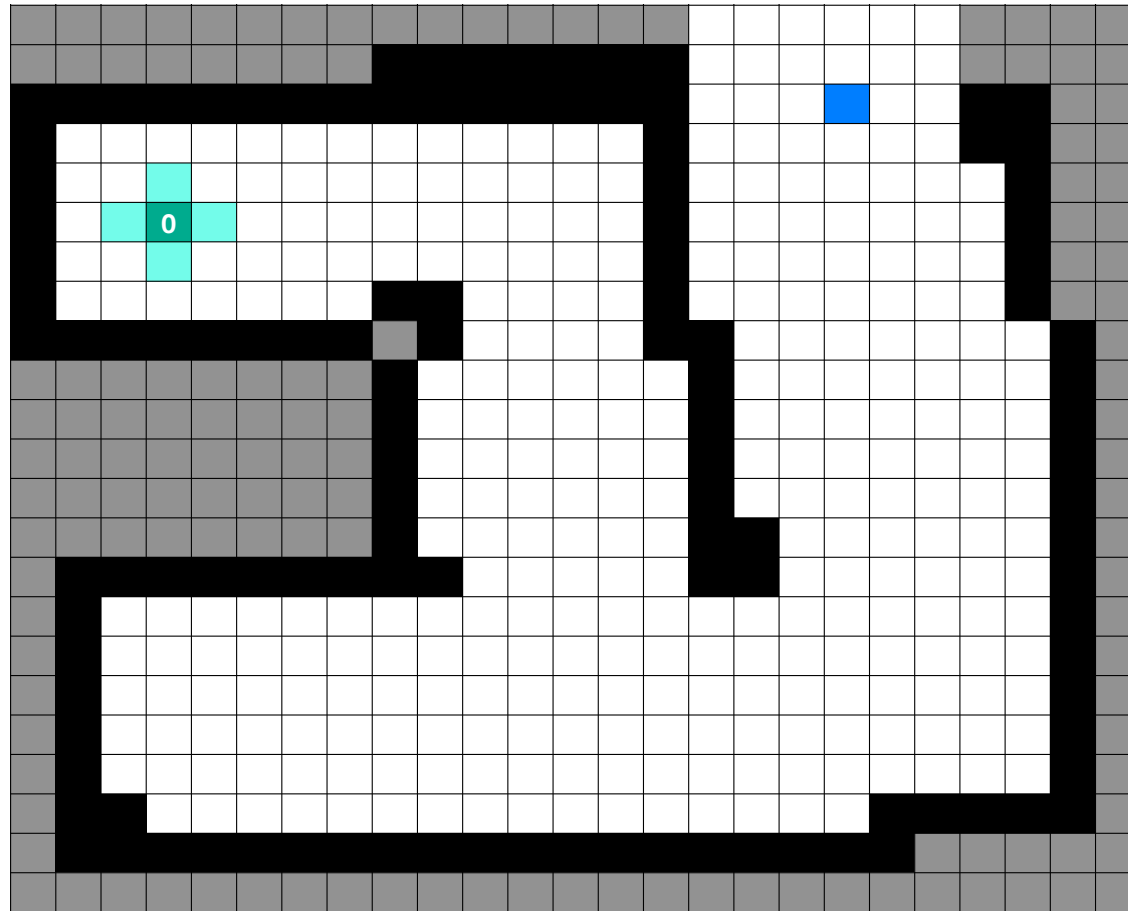
**Begin from
start node
with
no parent and
zero distance**

The start is the "root" of our search graph



**Begin from
start node
with
no parent and
zero distance**

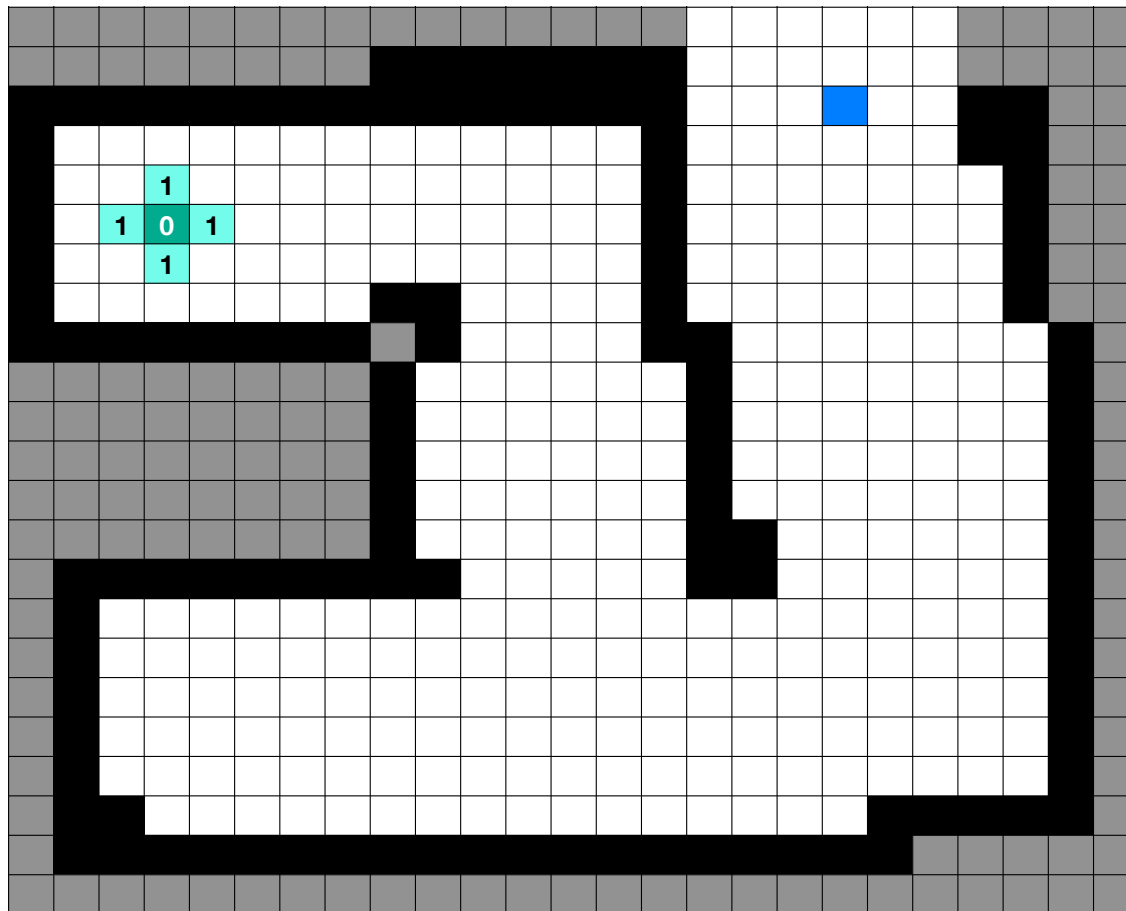
**All neighbors
of start are
"visited"**



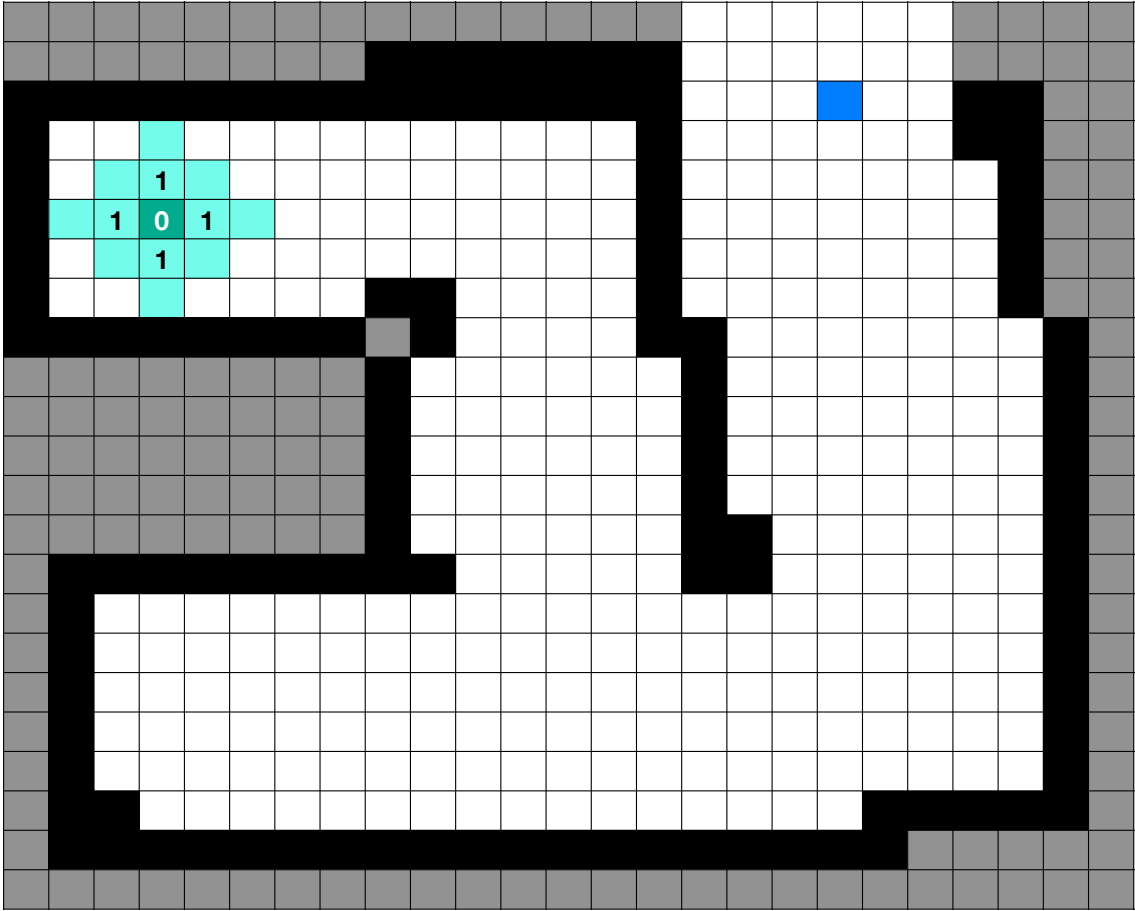
**Begin from
start node
with
no parent and
zero distance**

**All neighbors
of start are
"visited"**

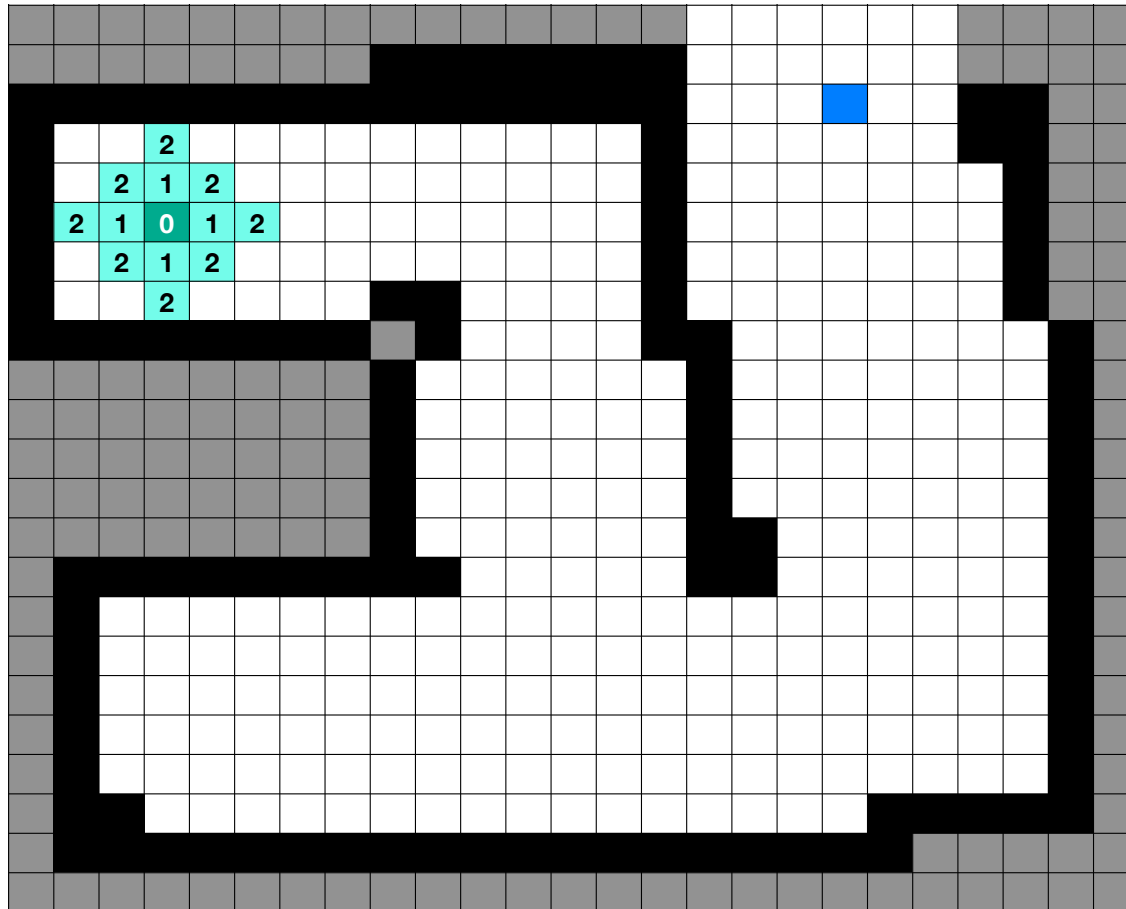
**And assigned
one plus the
smallest
distance**



Then, visit the neighbors of nodes just visited

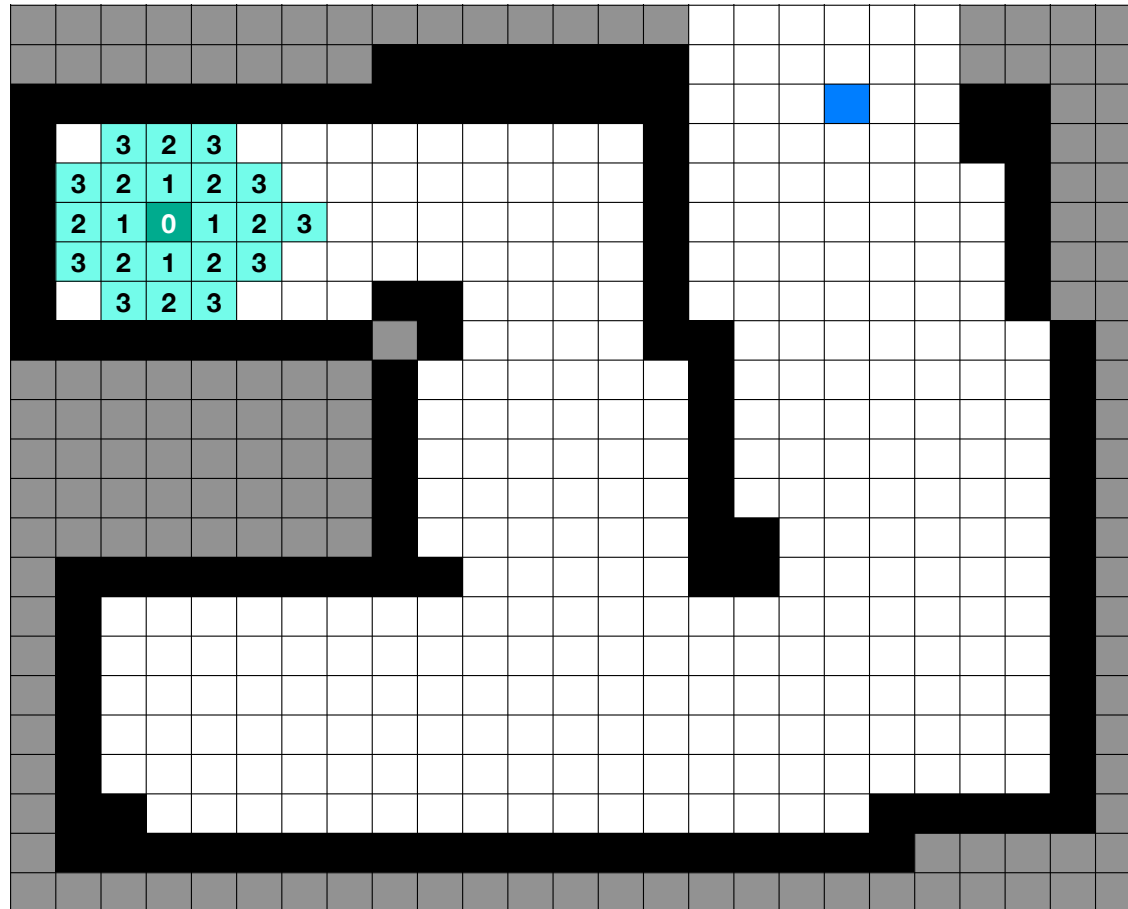


Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

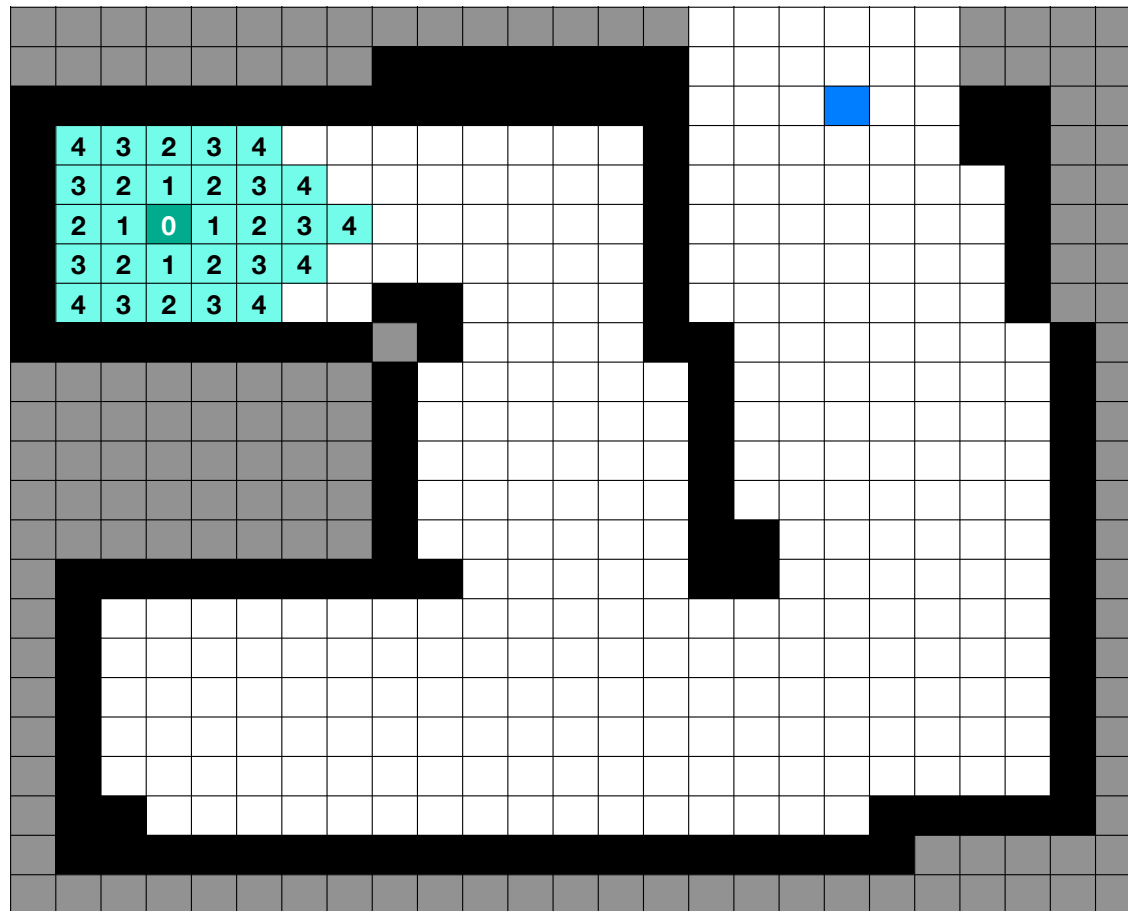
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

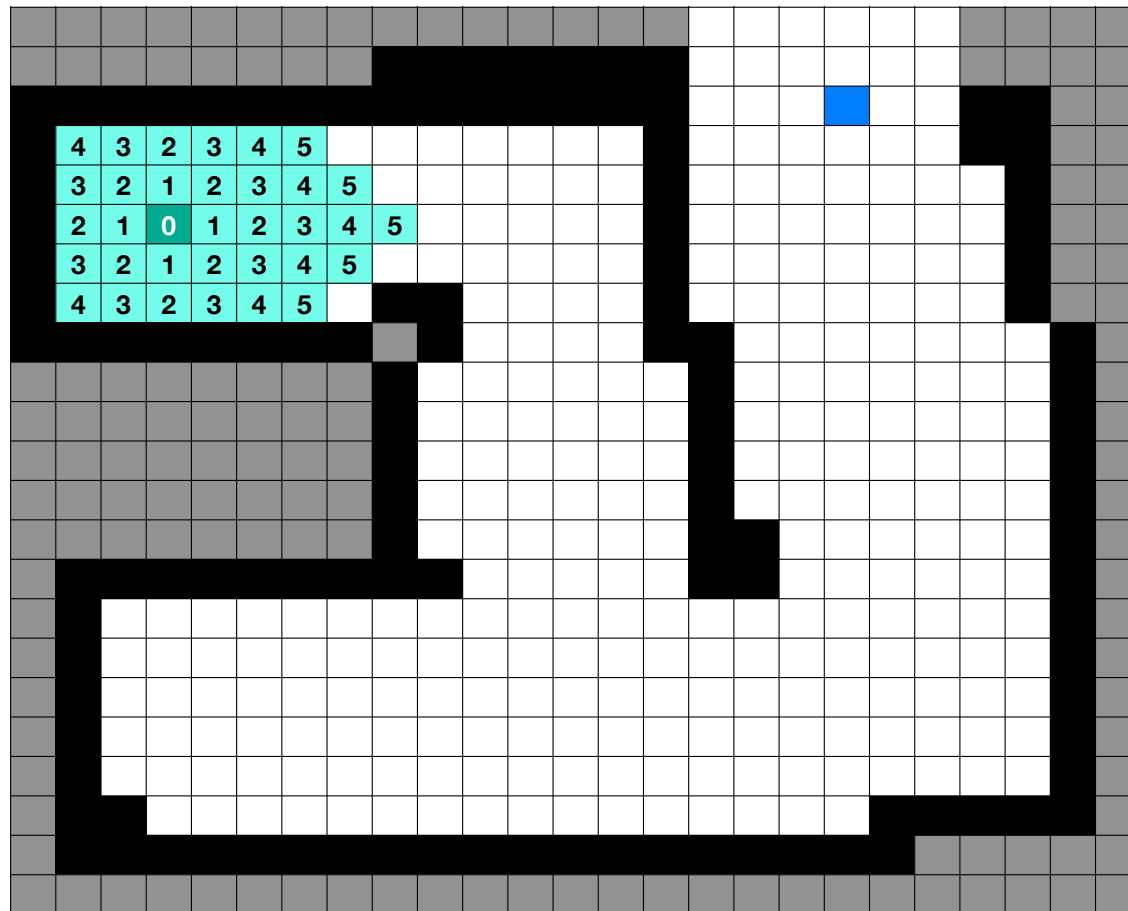
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

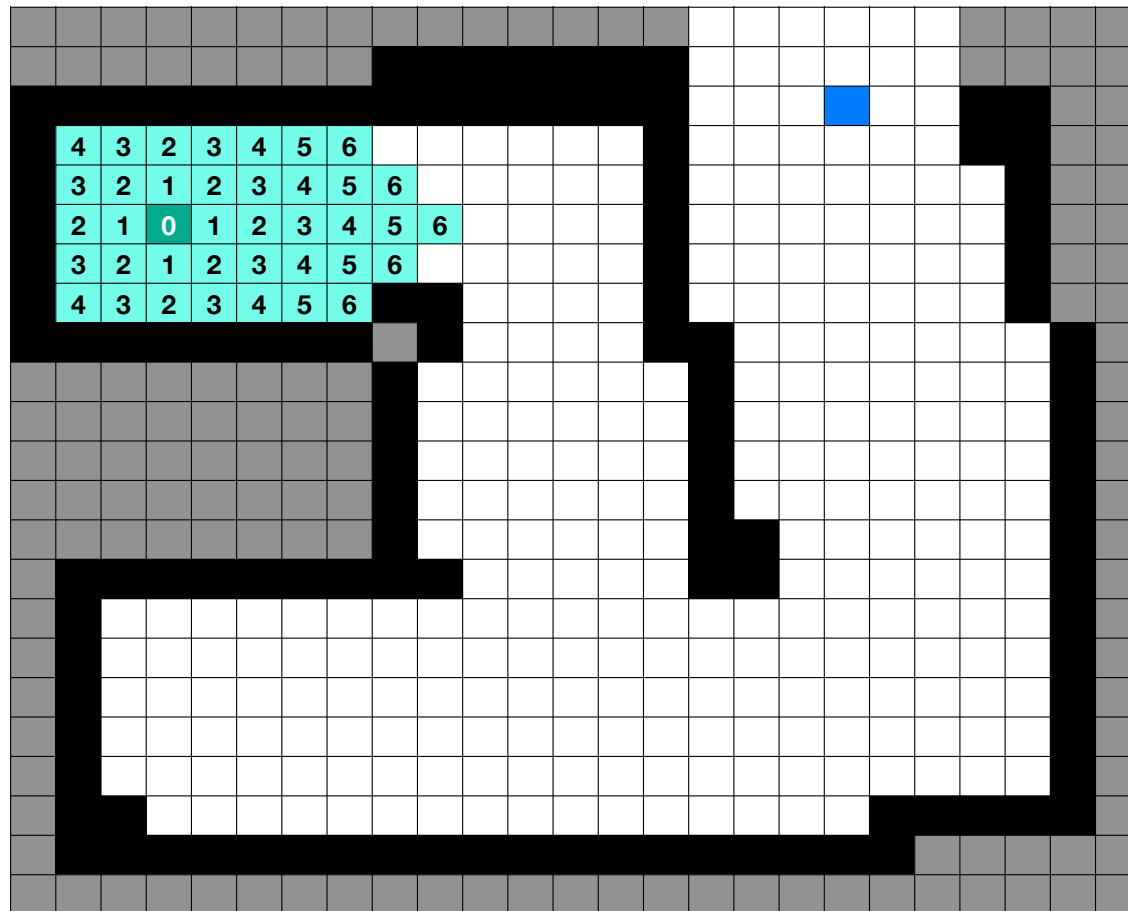
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

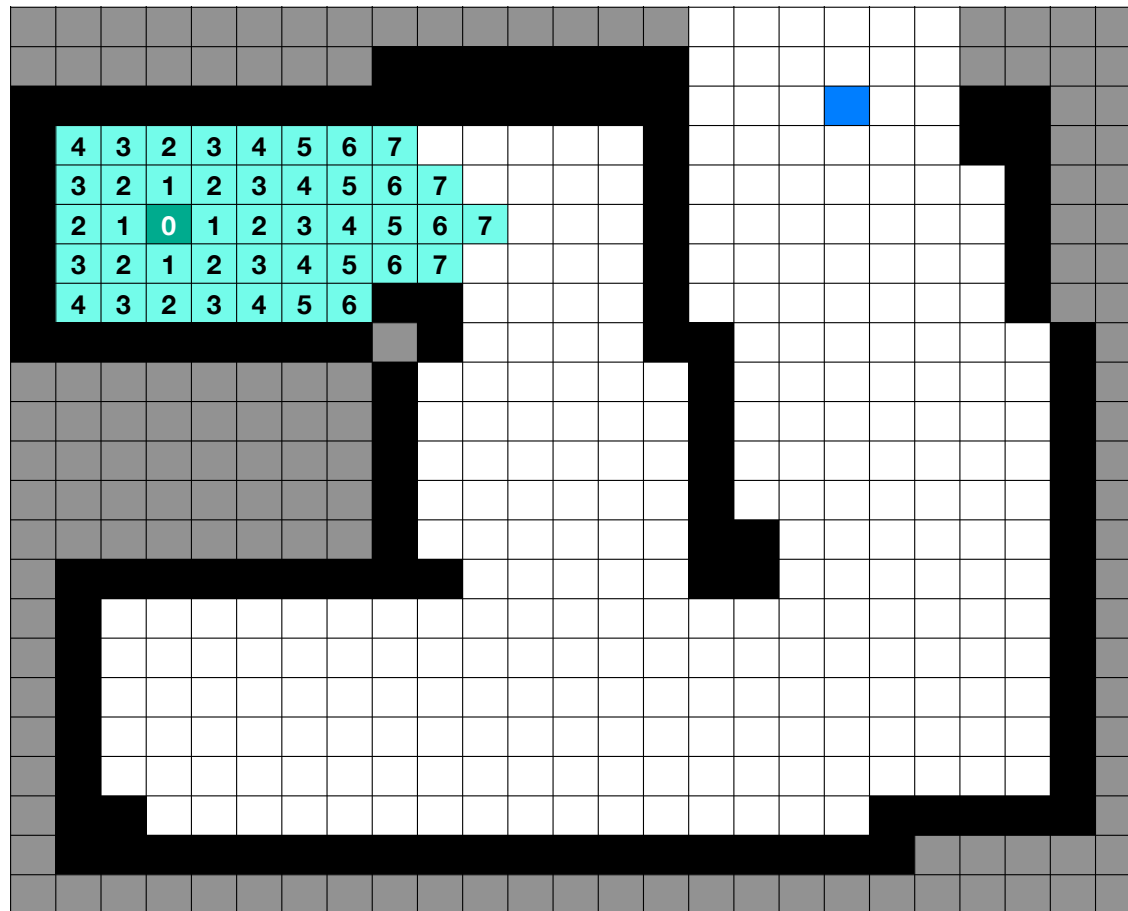
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

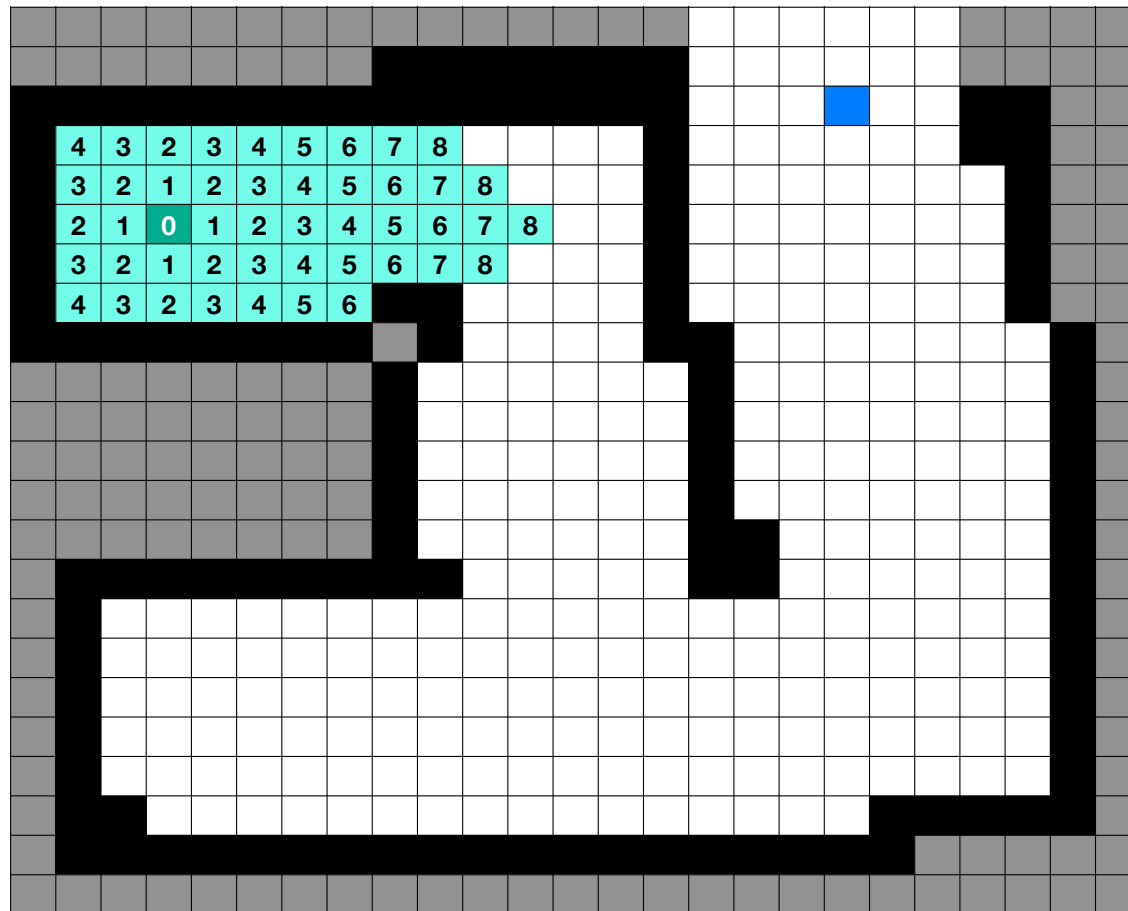
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

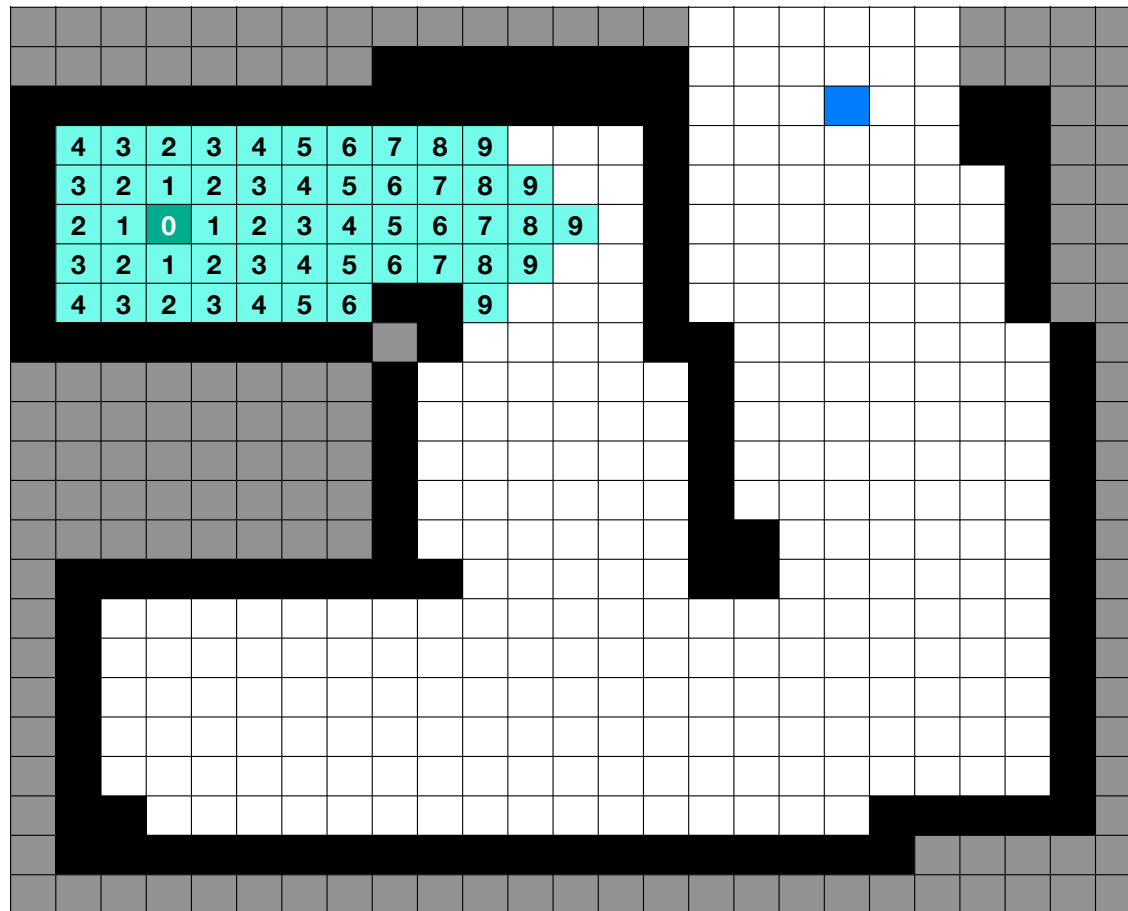
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

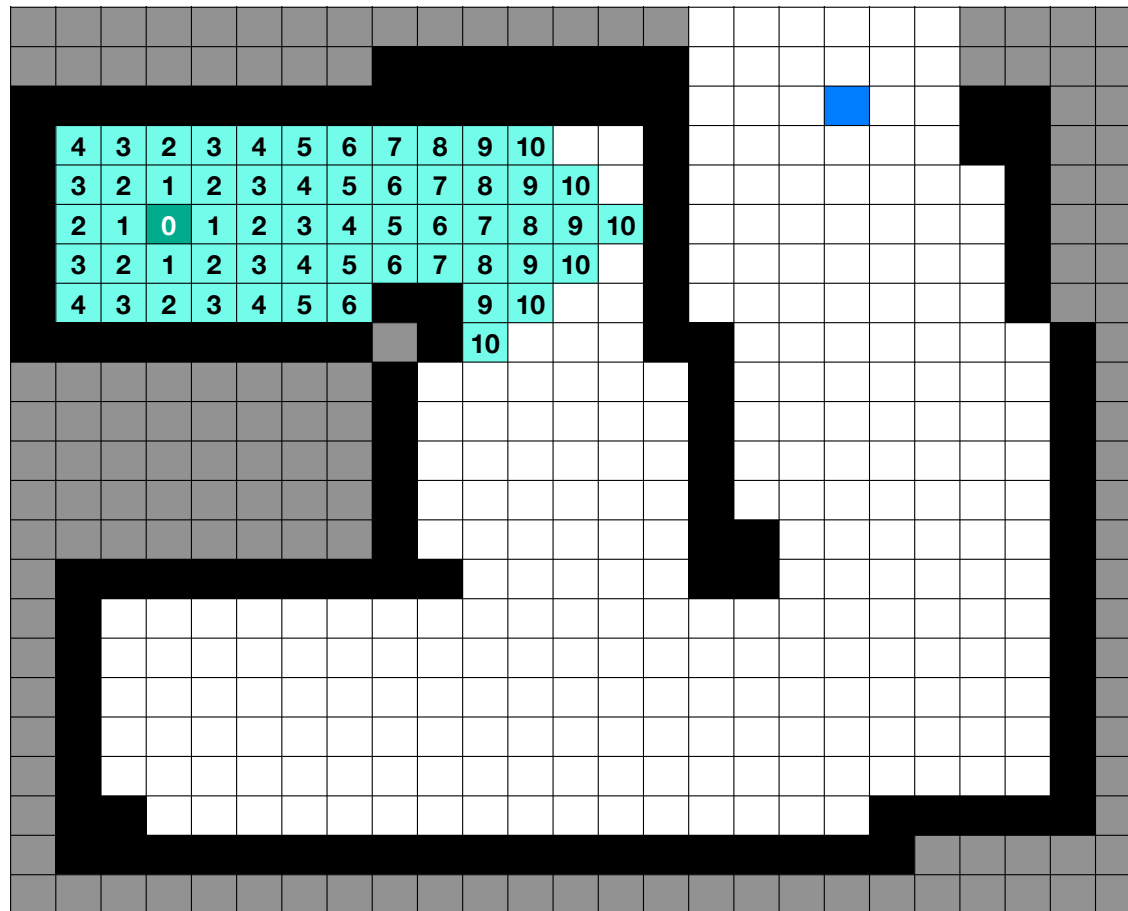
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

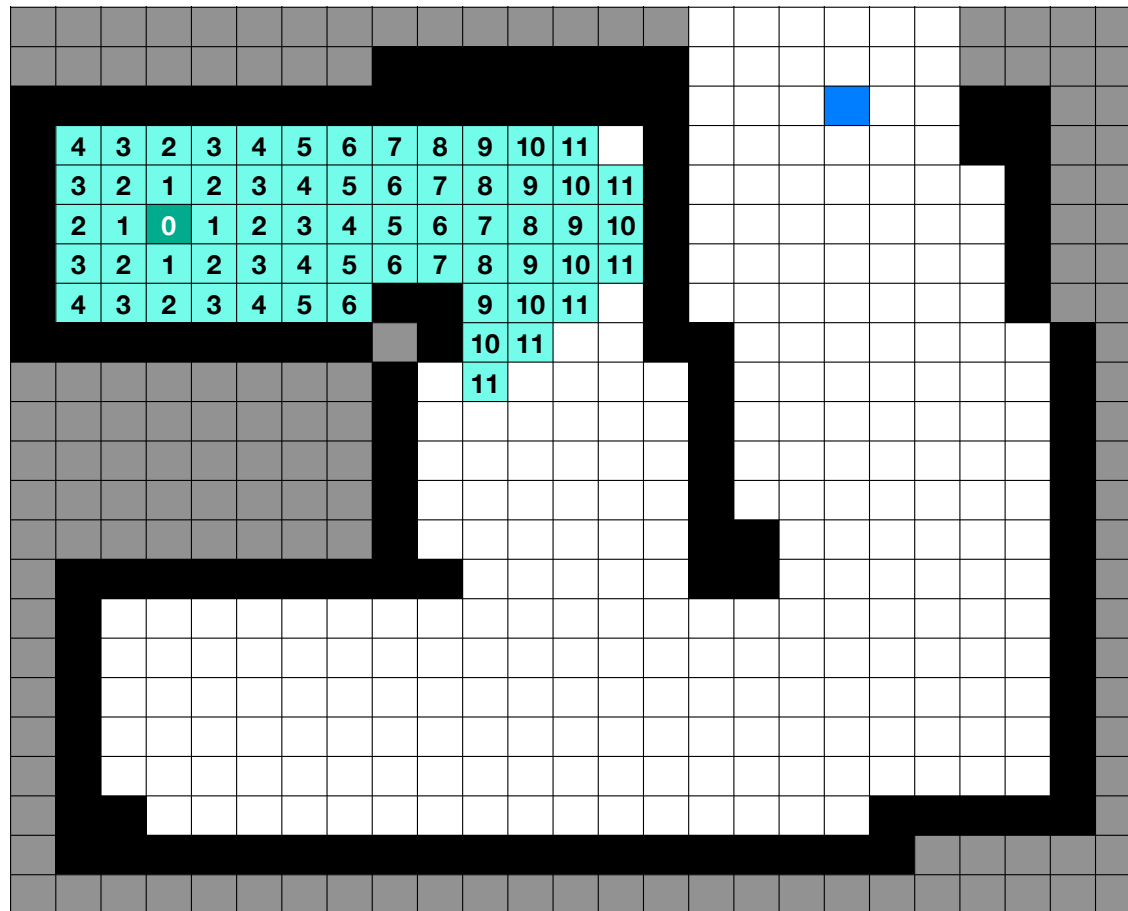
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

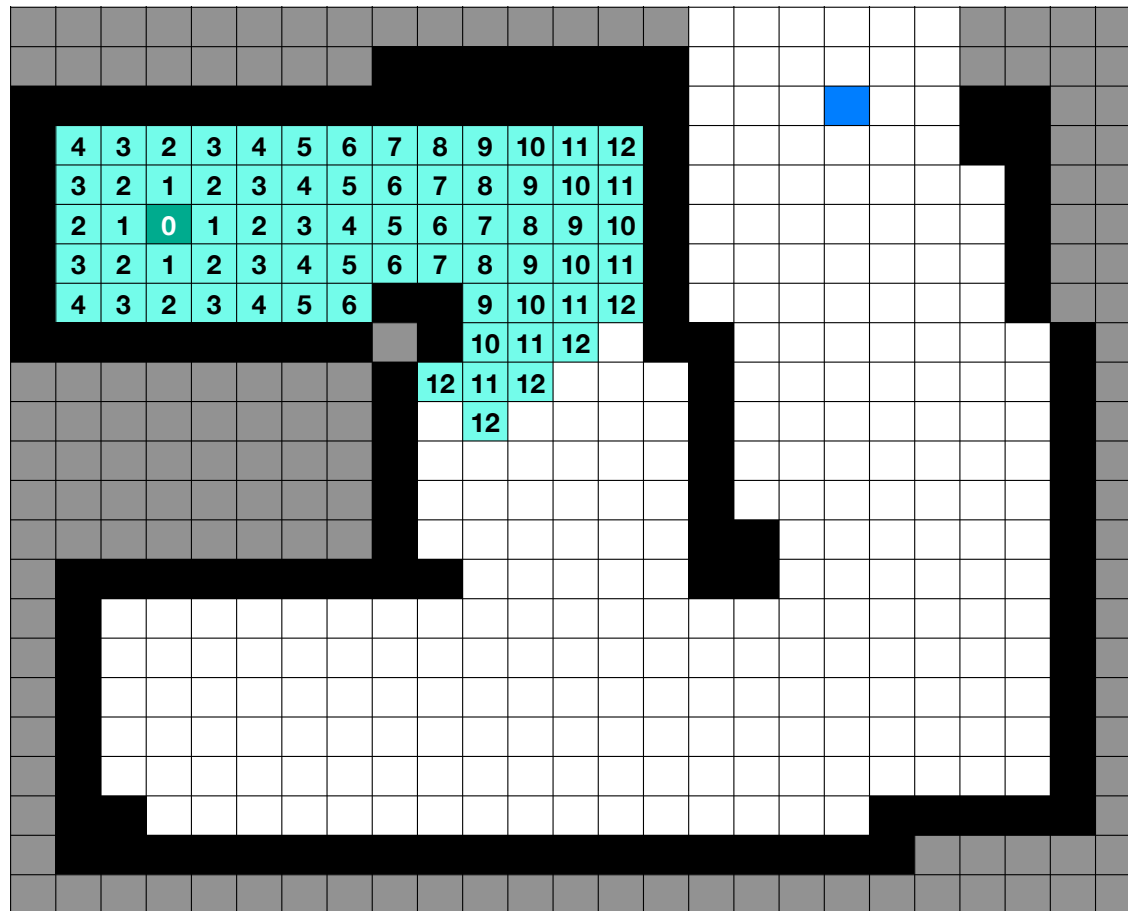
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

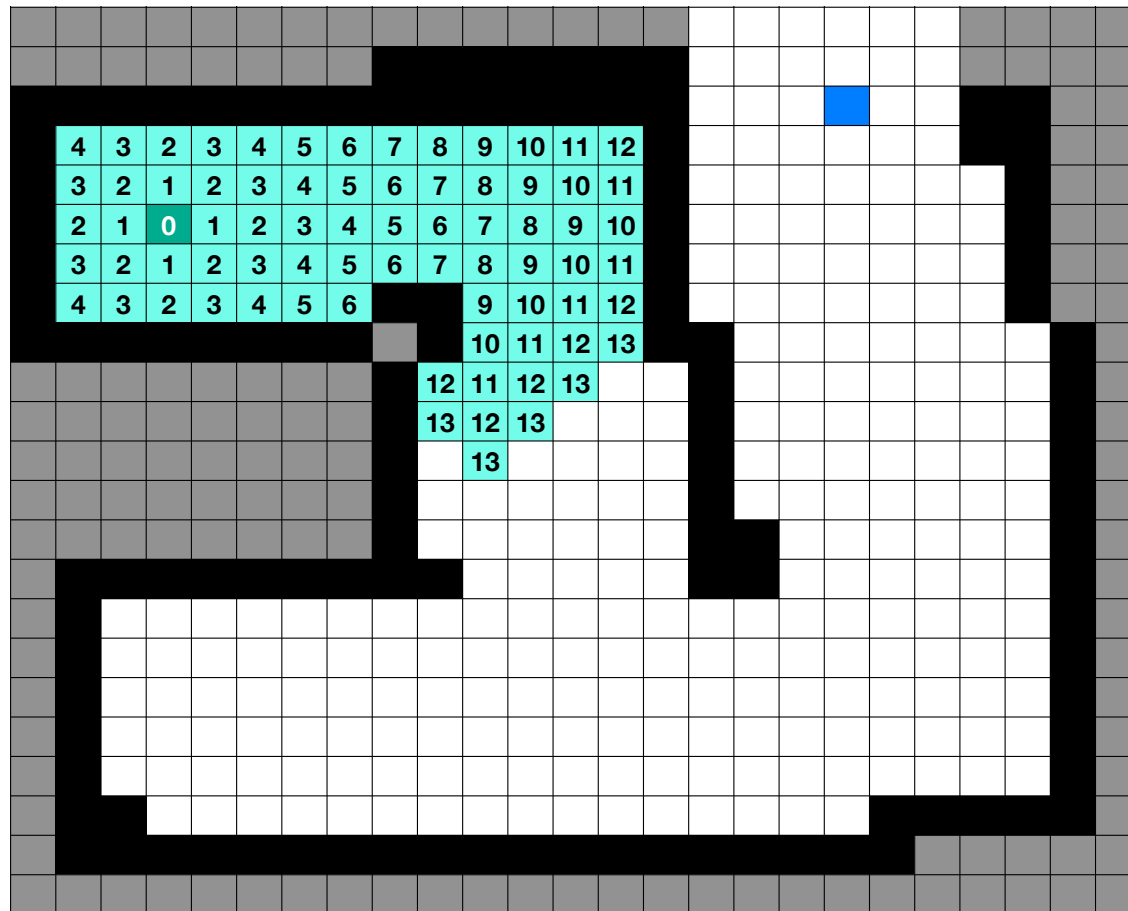
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

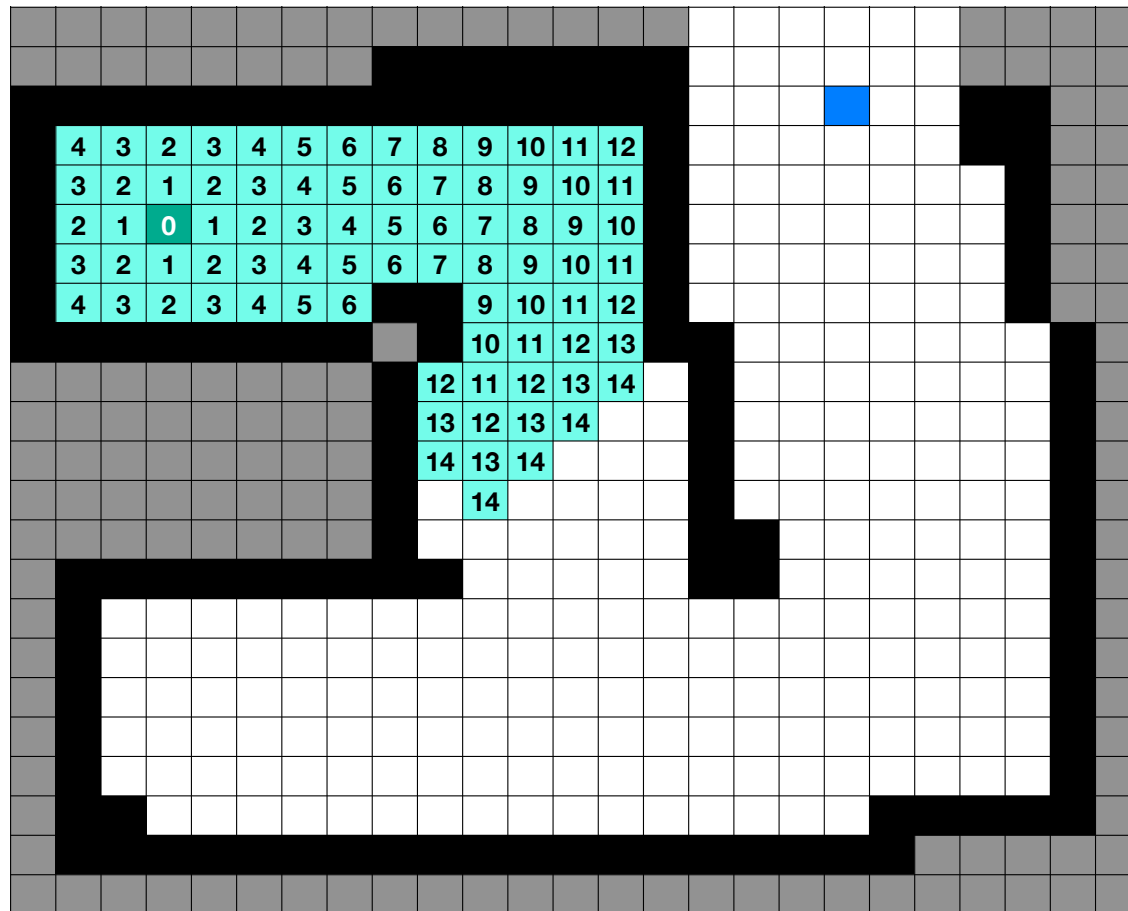
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

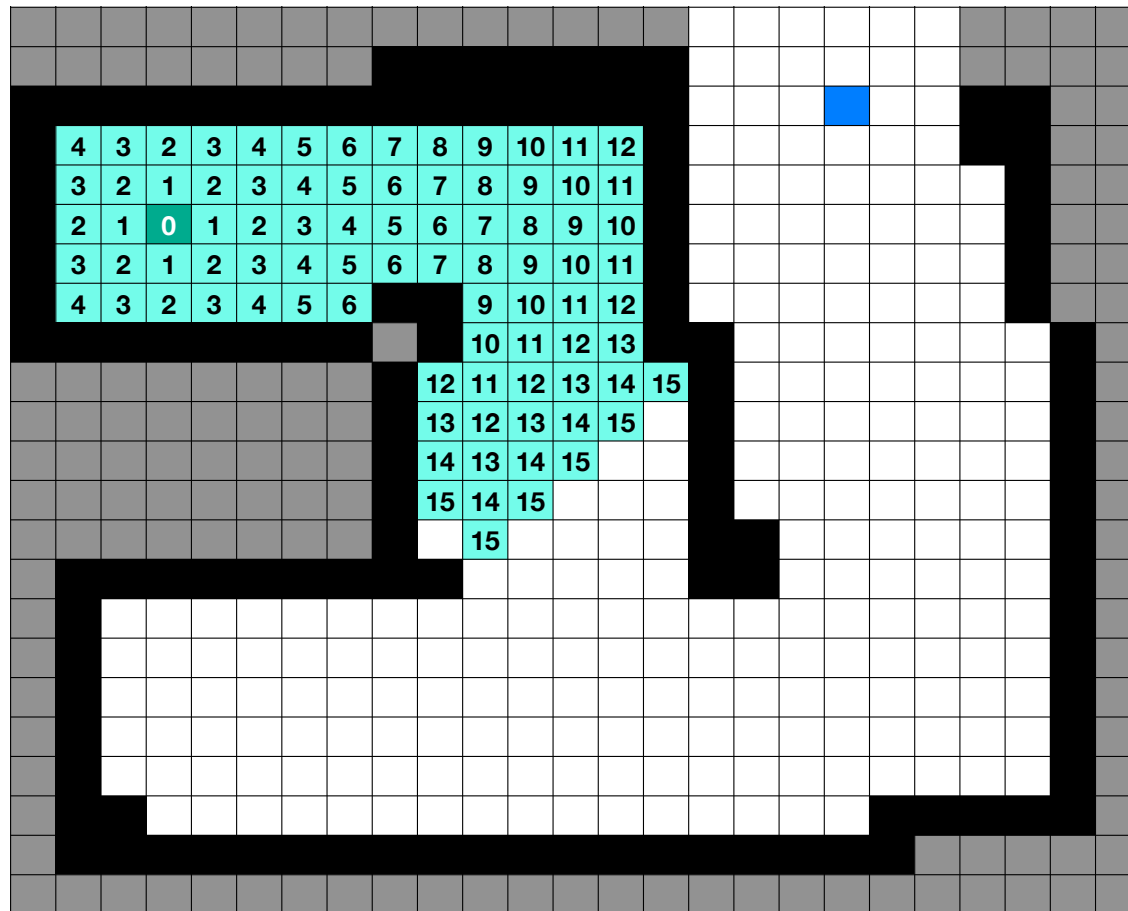
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

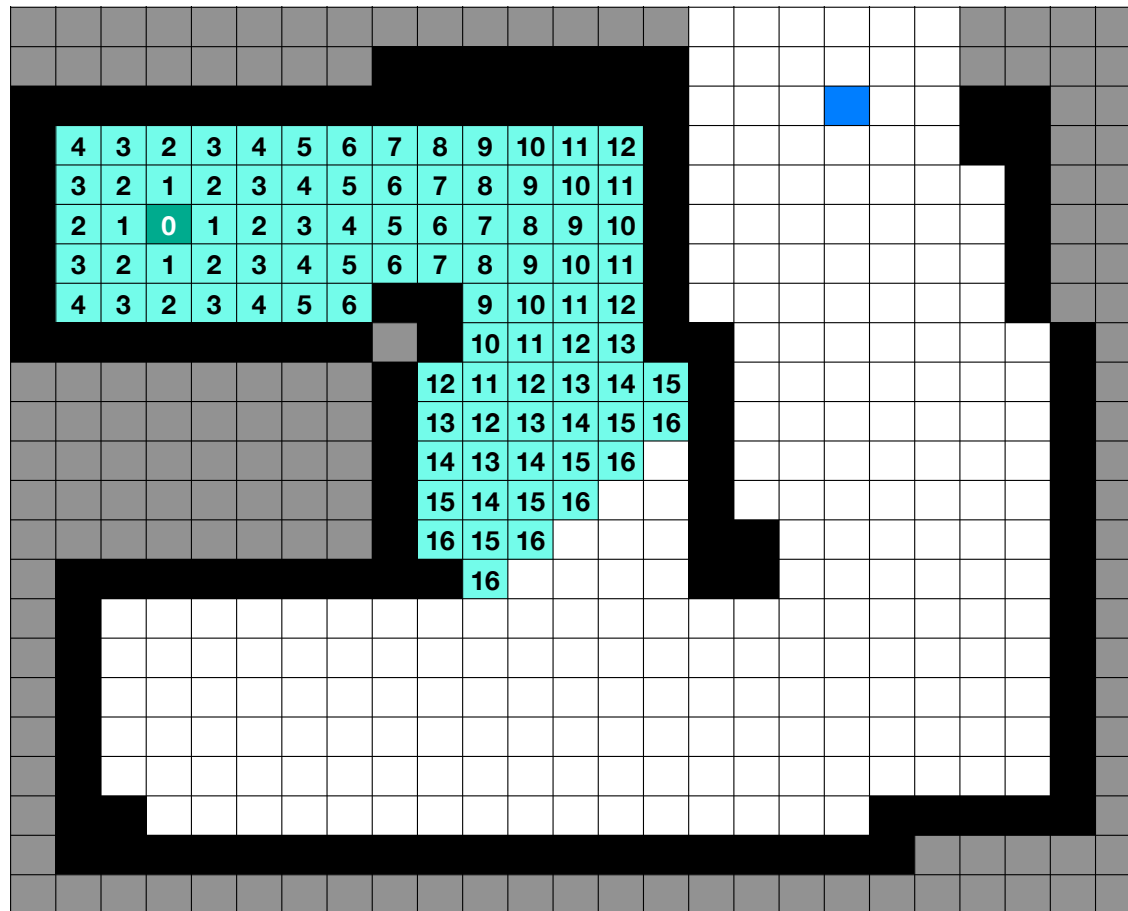
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

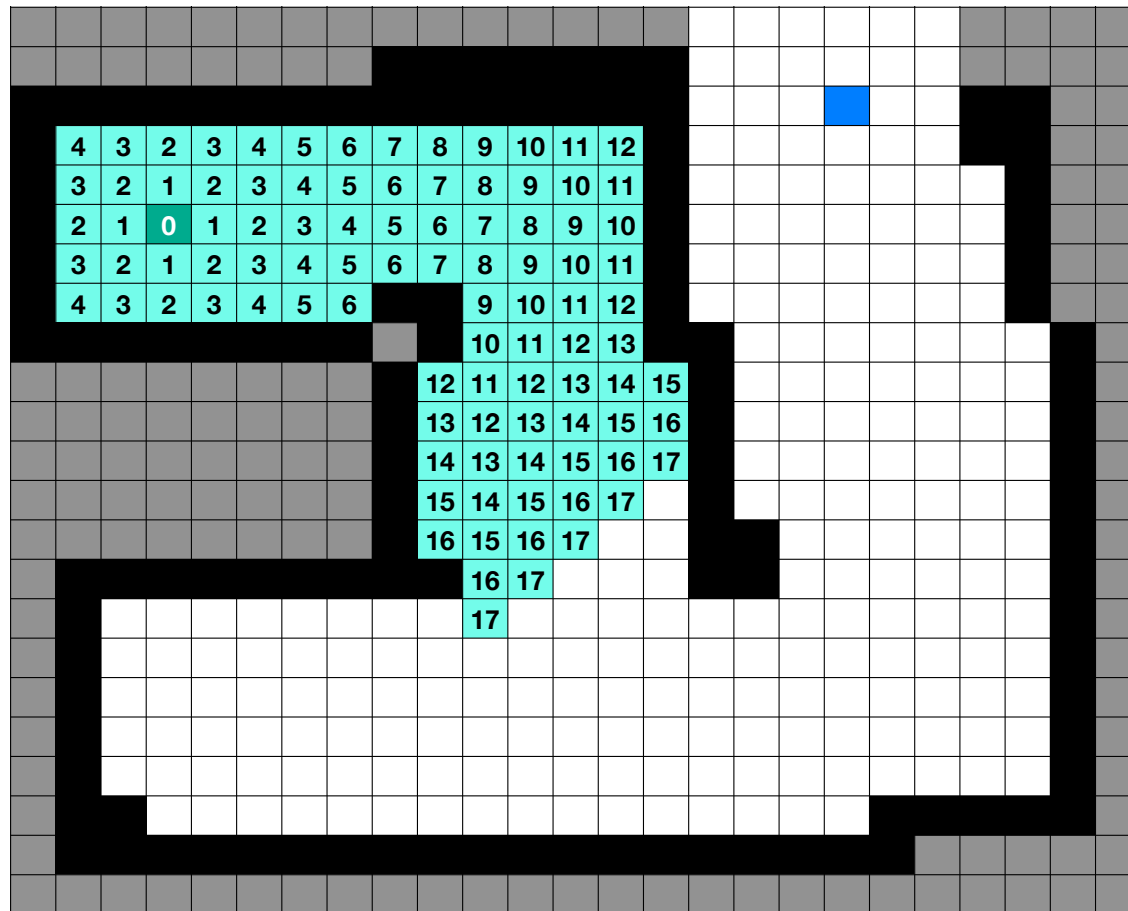
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

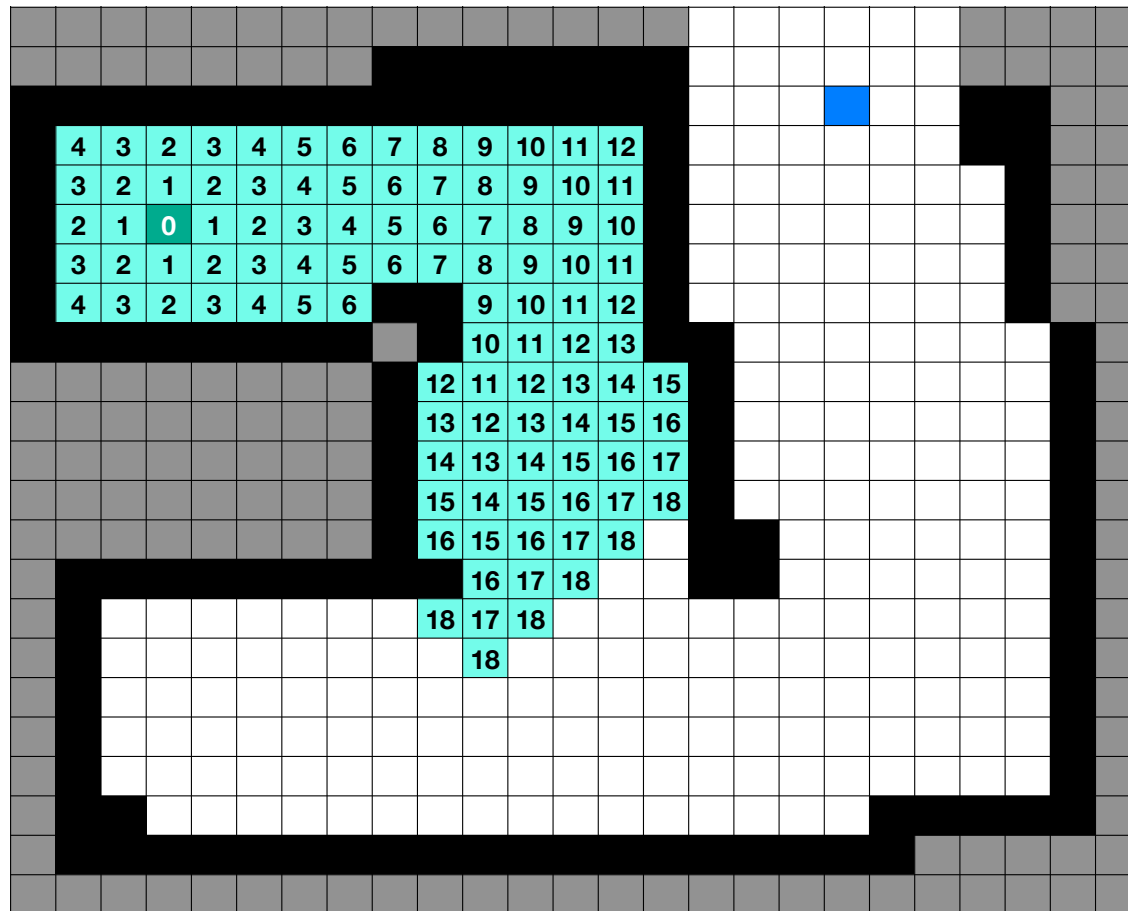
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

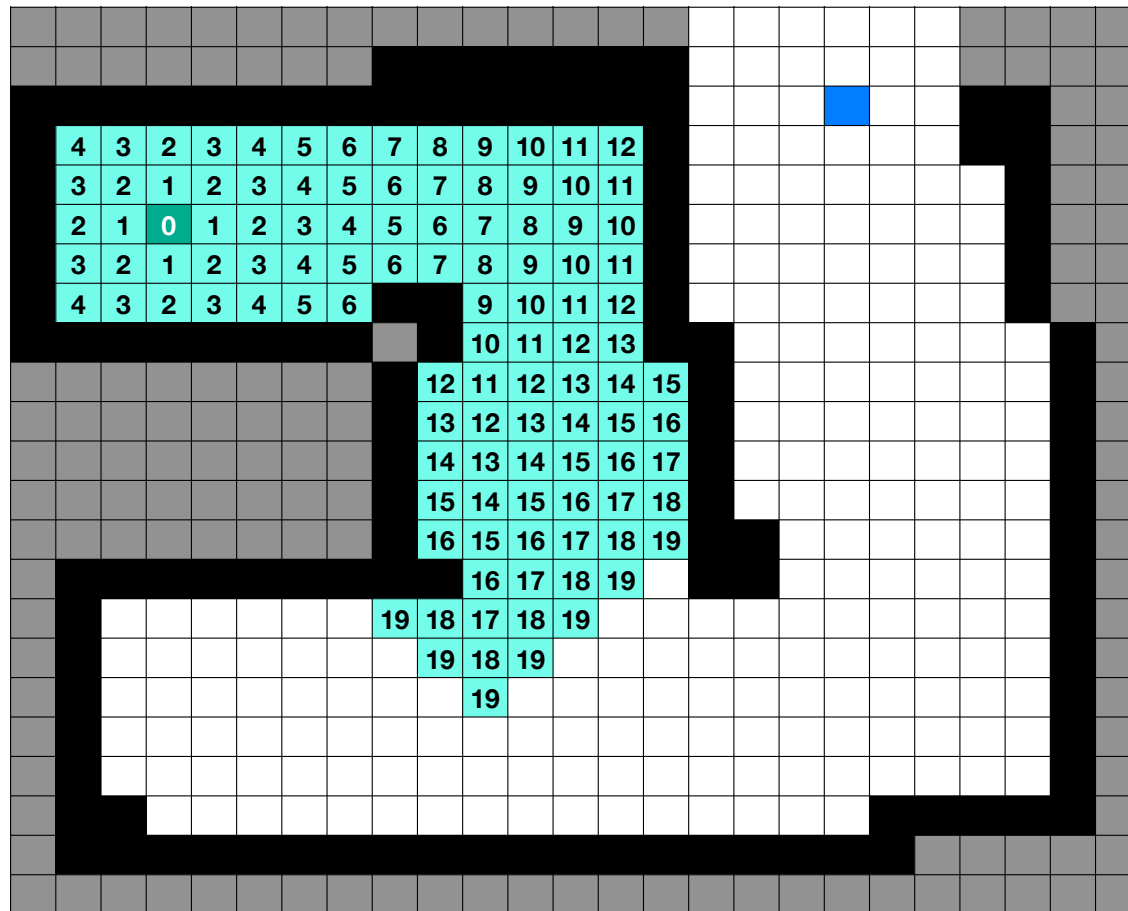
Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

Then, visit the neighbors of nodes just visited



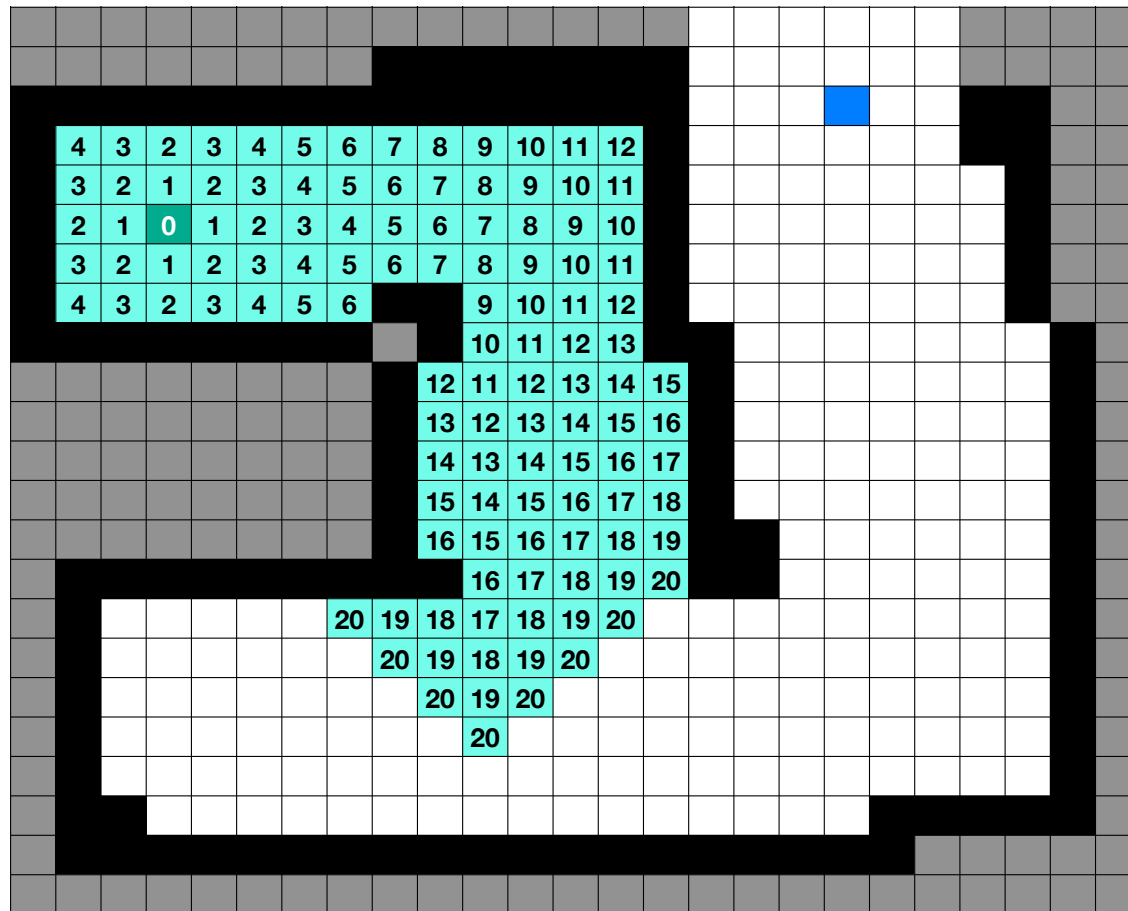
Assign each one plus the smallest distance

Repeat for next set of neighbors

Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

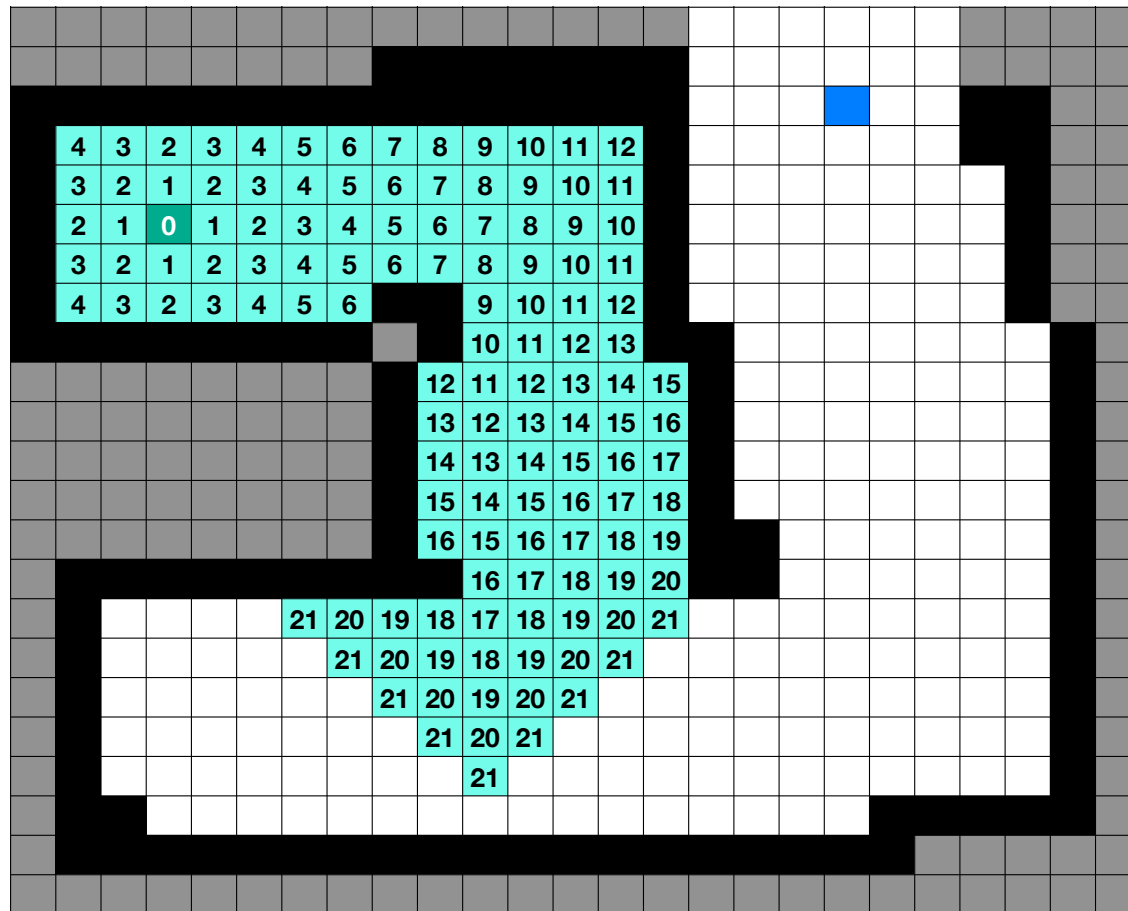
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

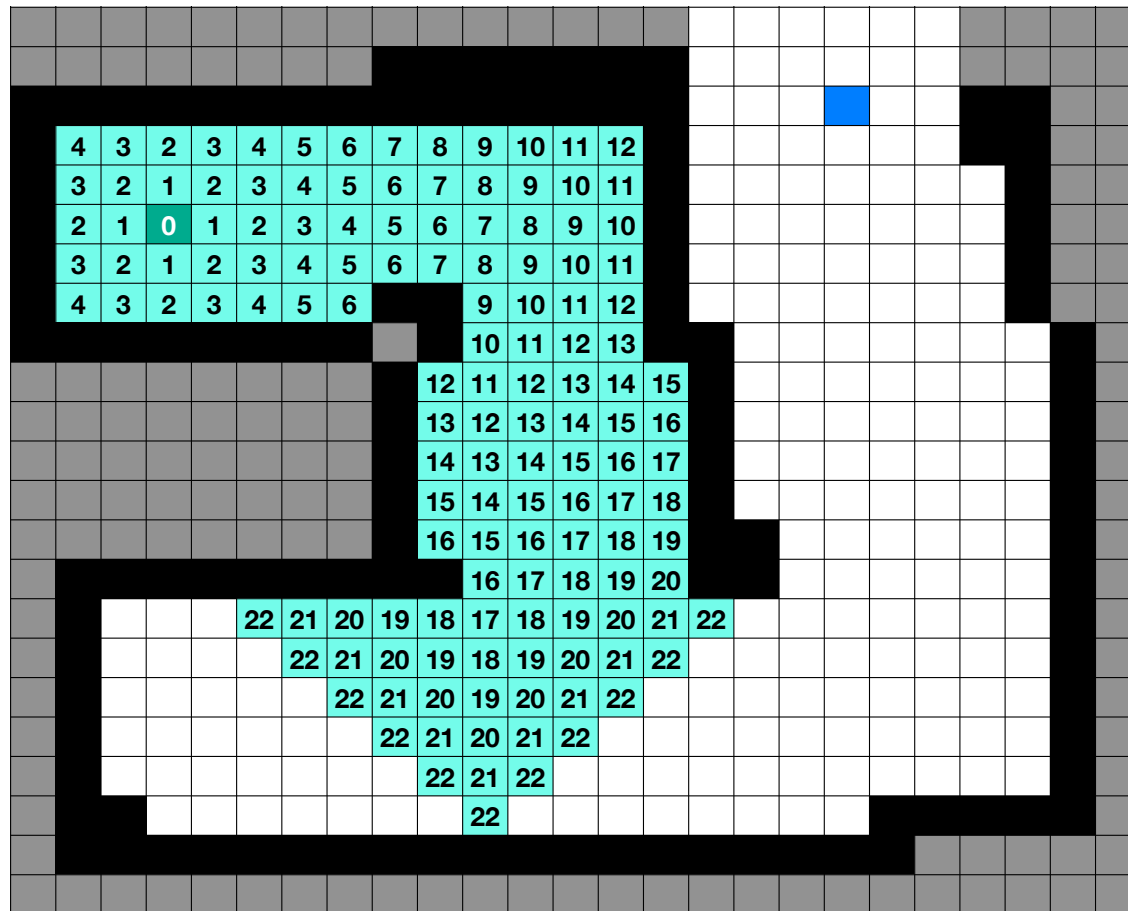
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

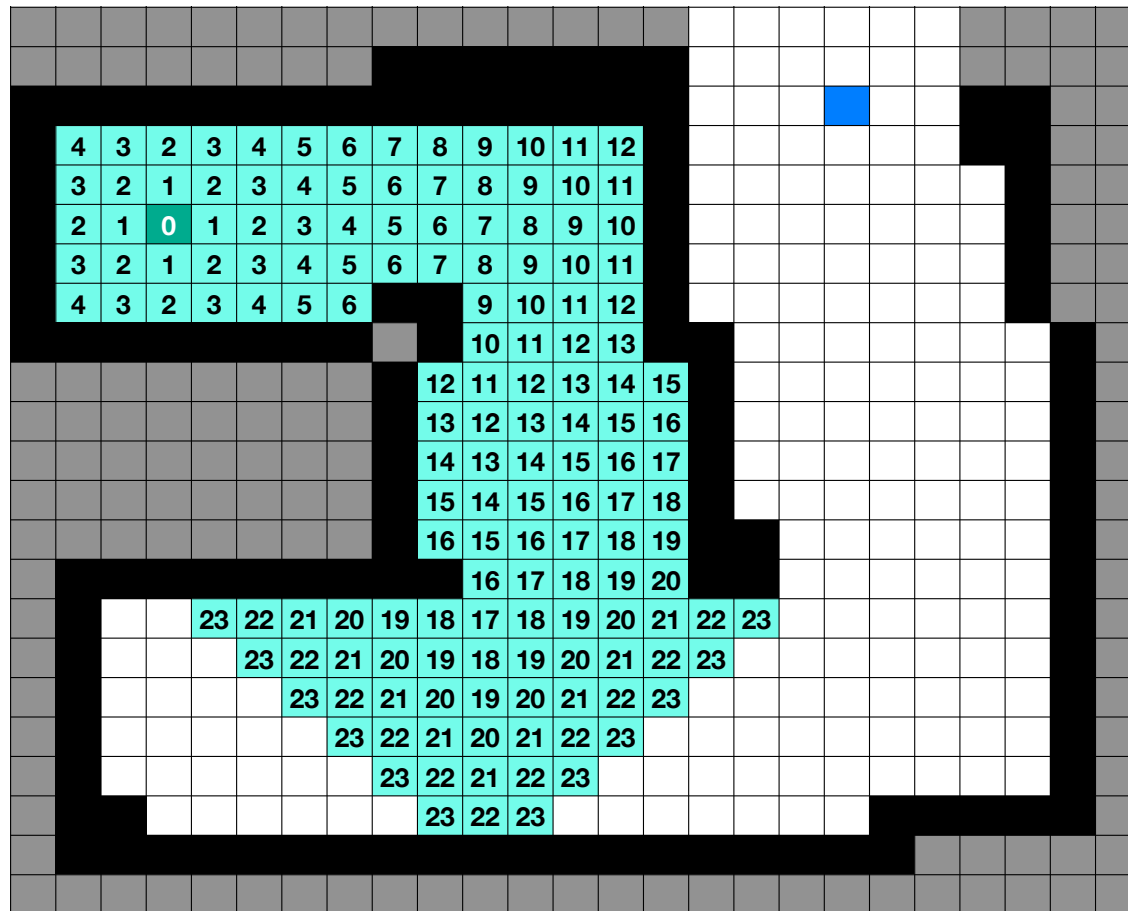
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

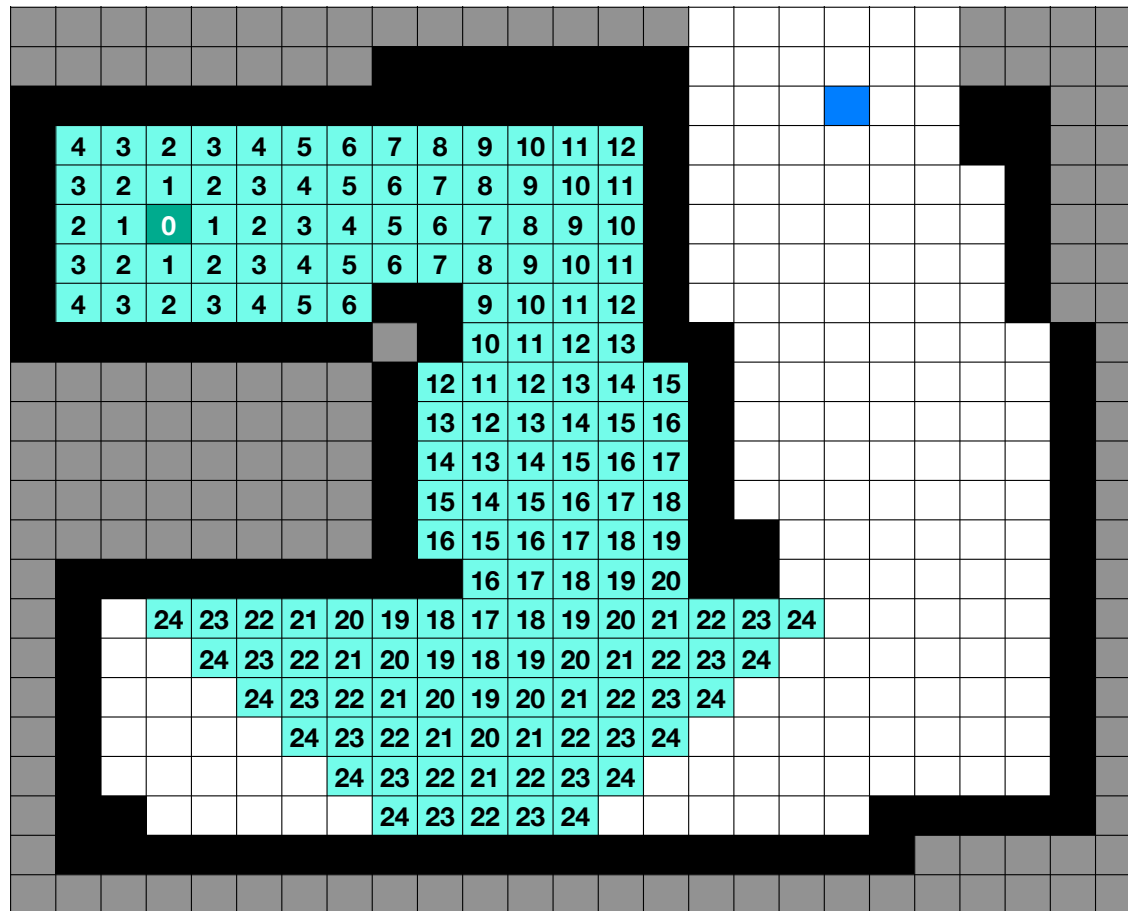
Repeat for next set of neighbors



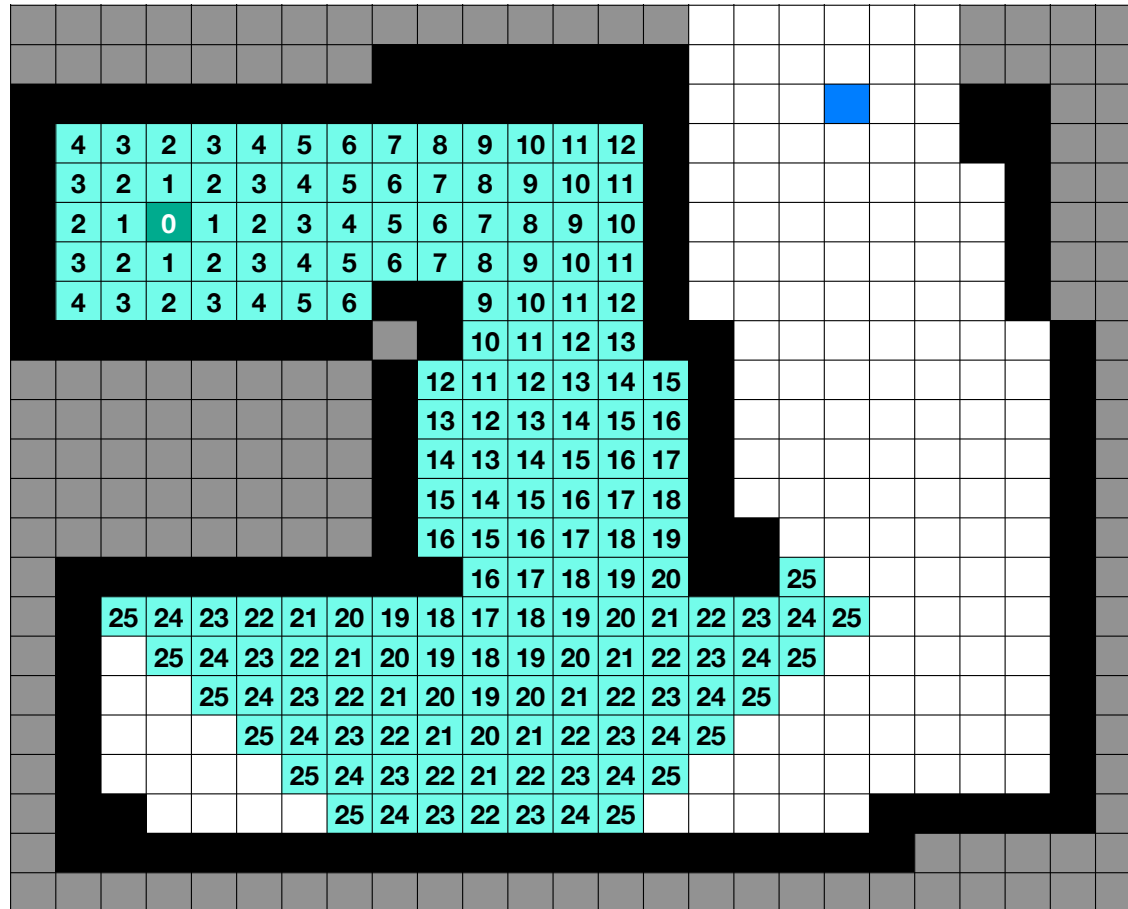
Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited



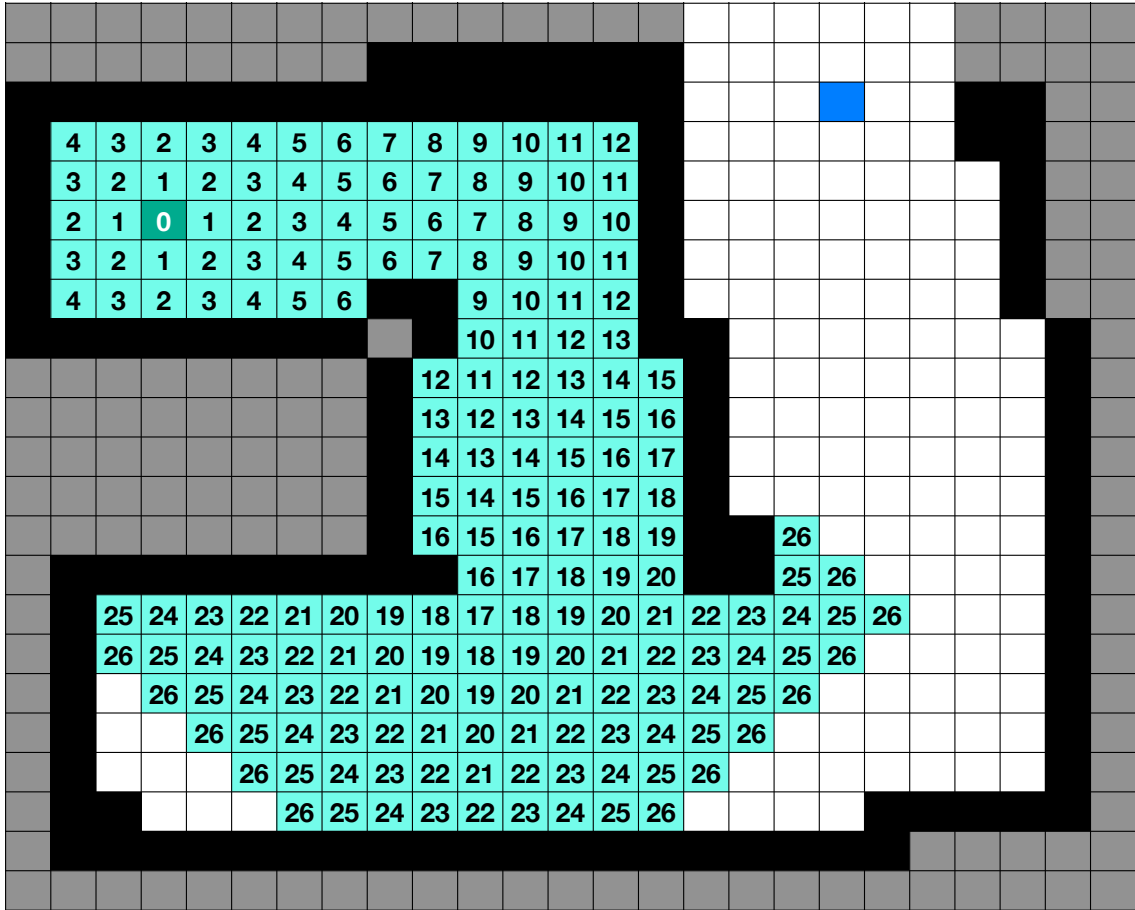
Assign each one plus the smallest distance

Repeat for next set of neighbors

Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

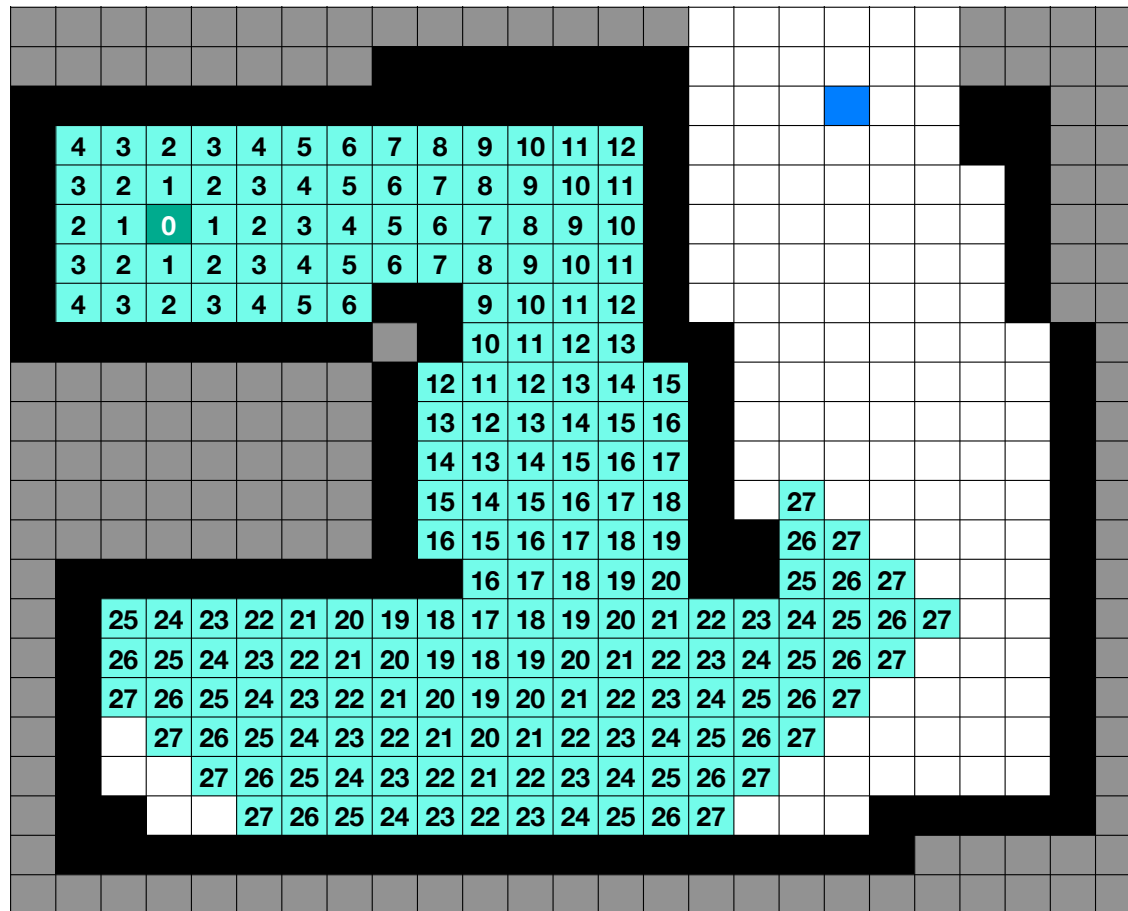
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

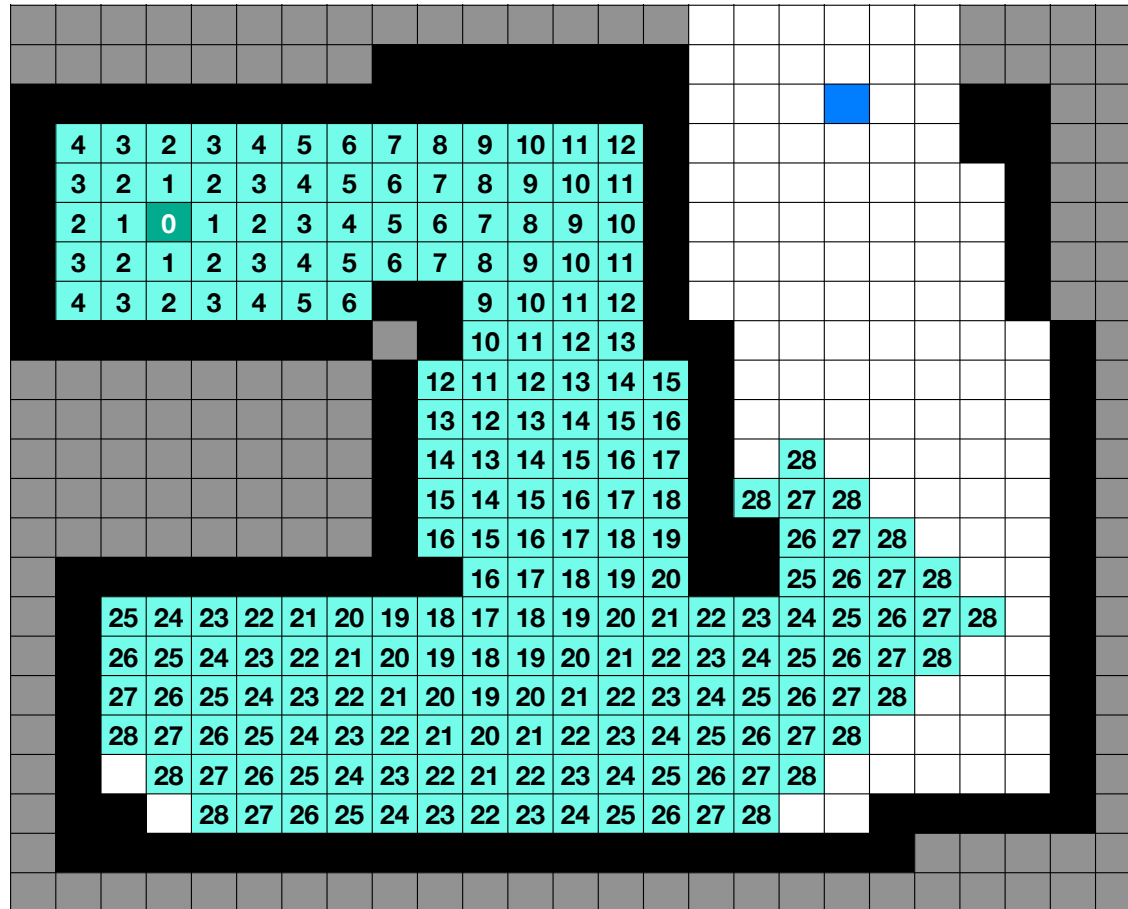
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

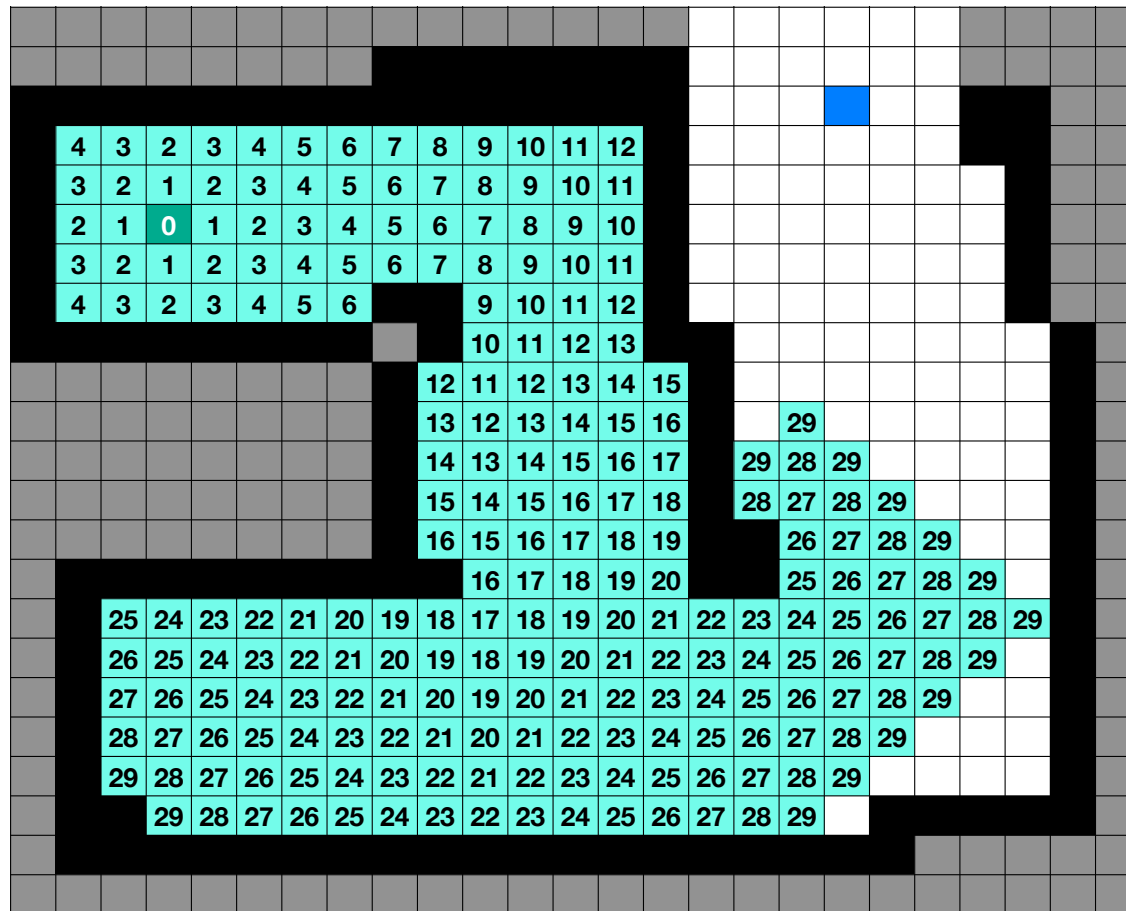
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

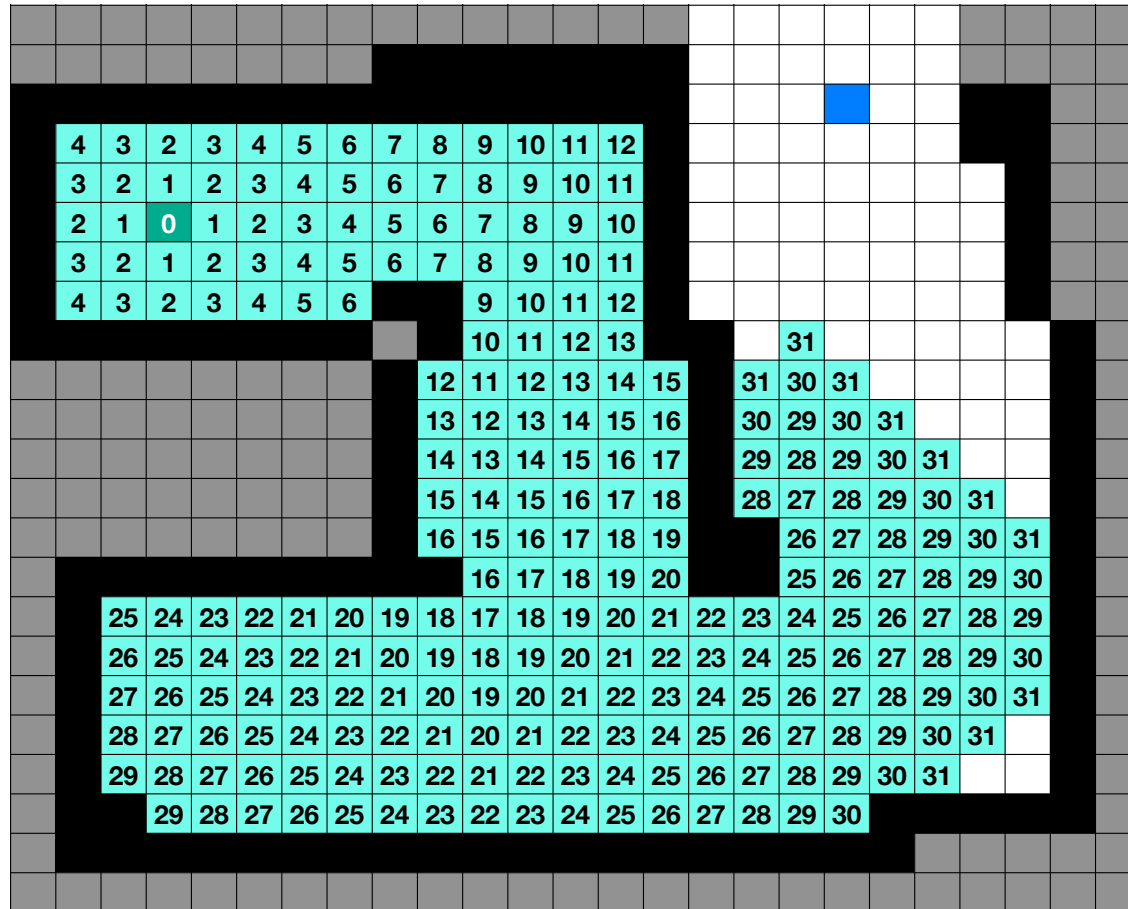
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

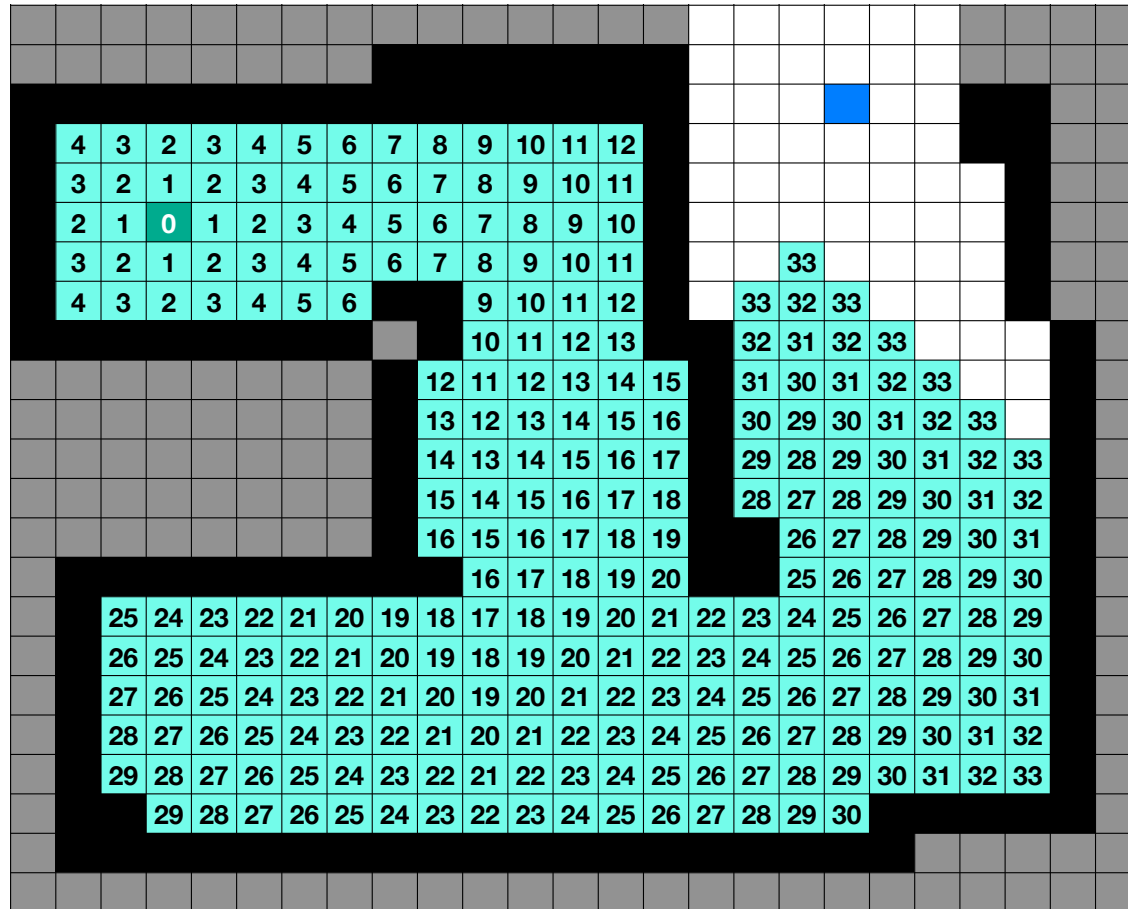
Repeat for next set of neighbors



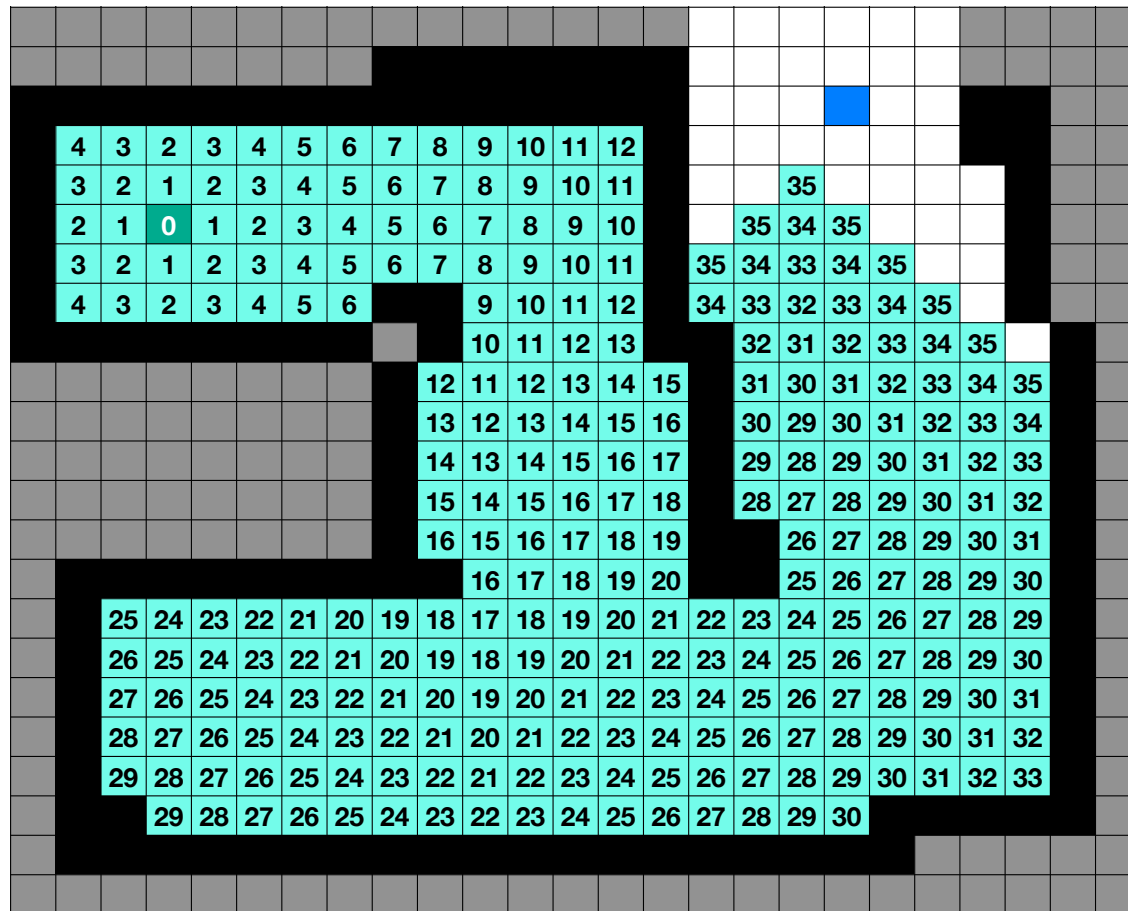
Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited



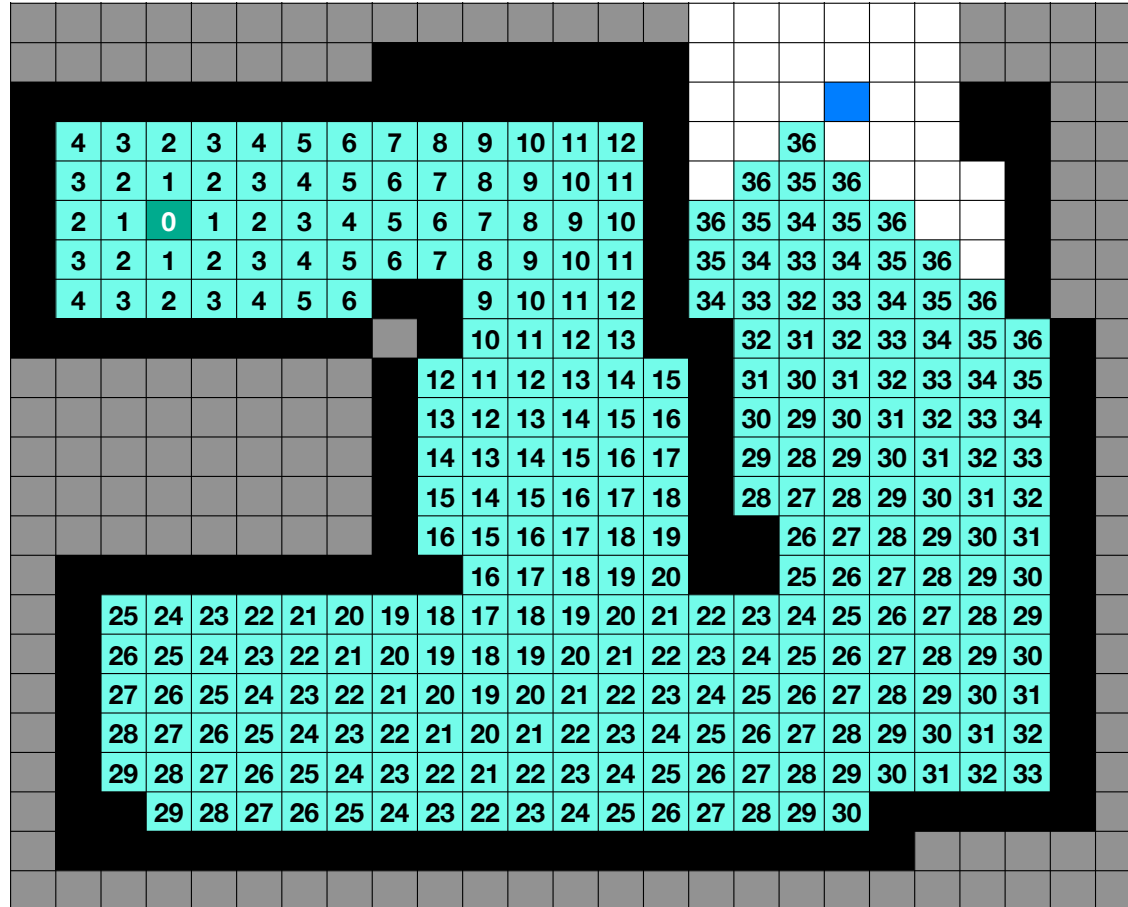
Assign each one plus the smallest distance

Repeat for next set of neighbors

Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

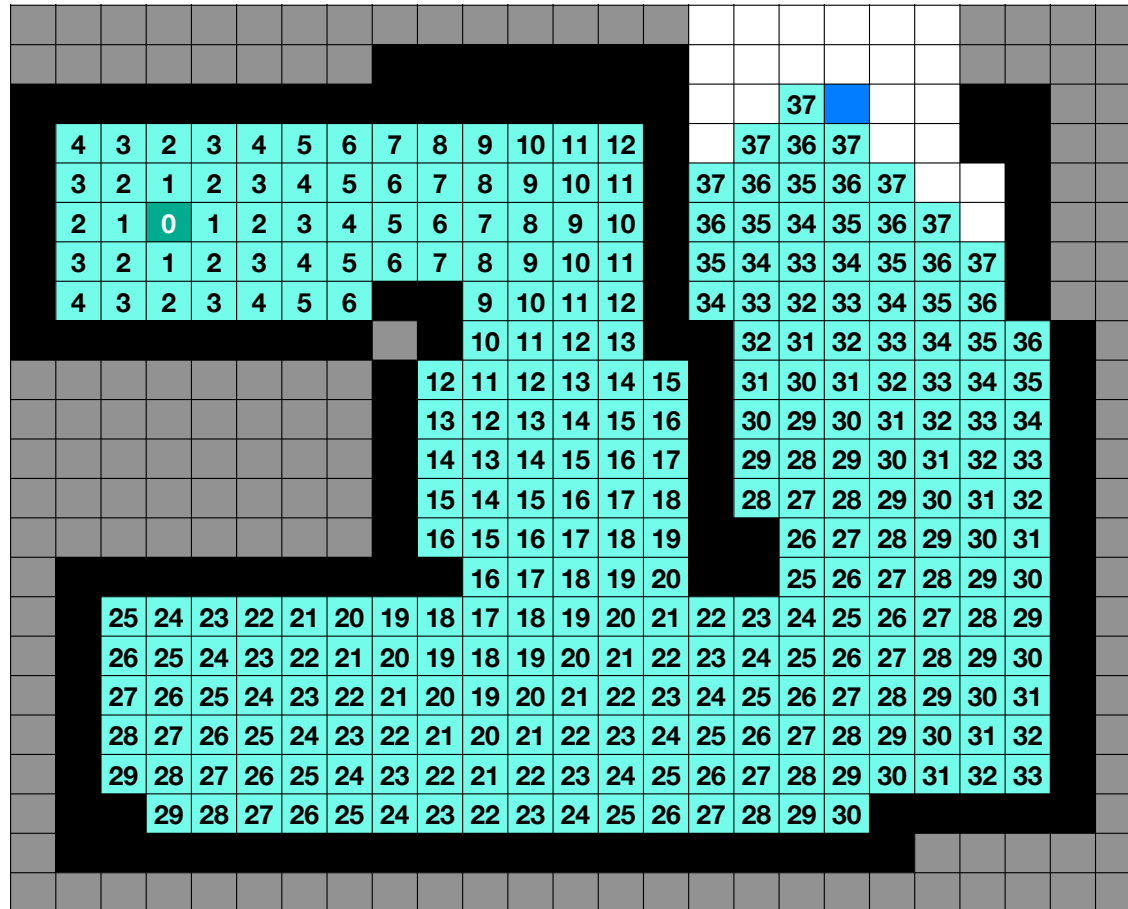
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

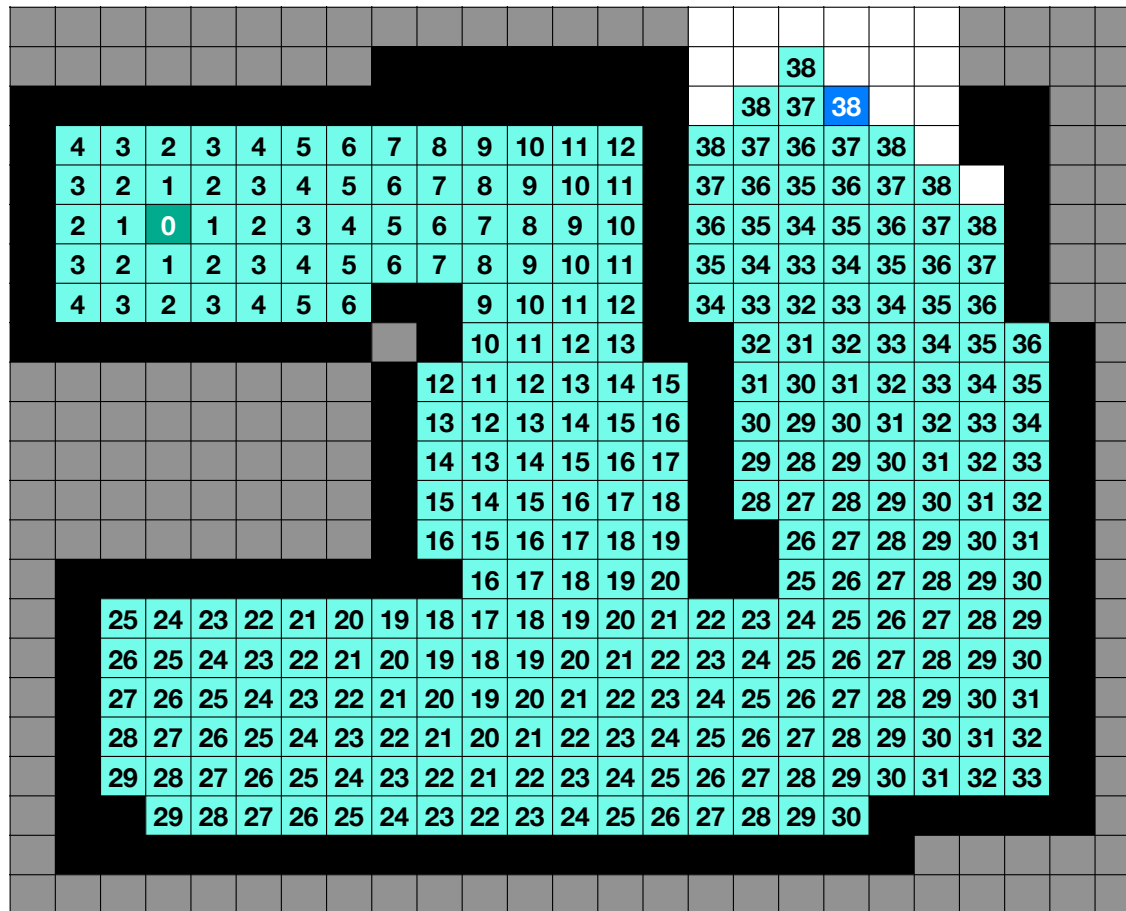
Repeat for next set of neighbors



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

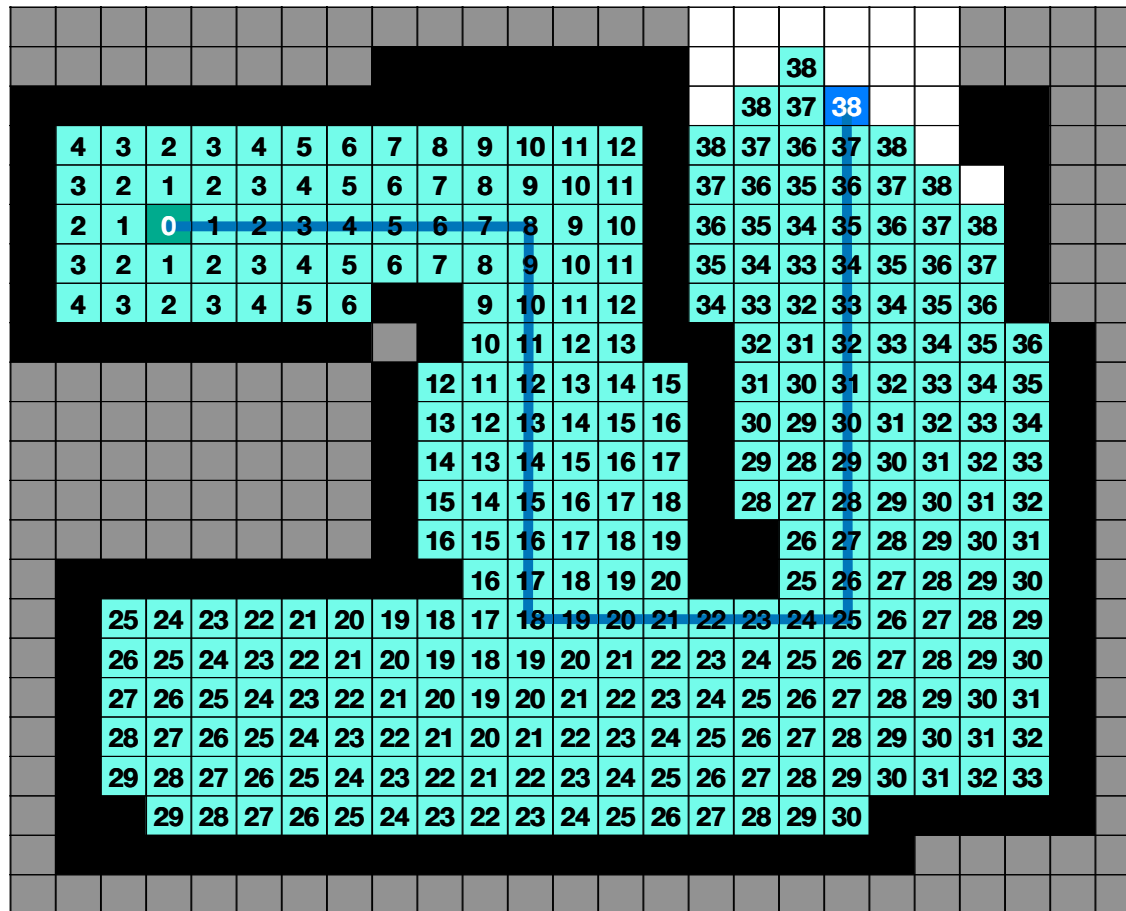


Once goal node reached, perform local search back to start

Then, visit the neighbors of nodes just visited

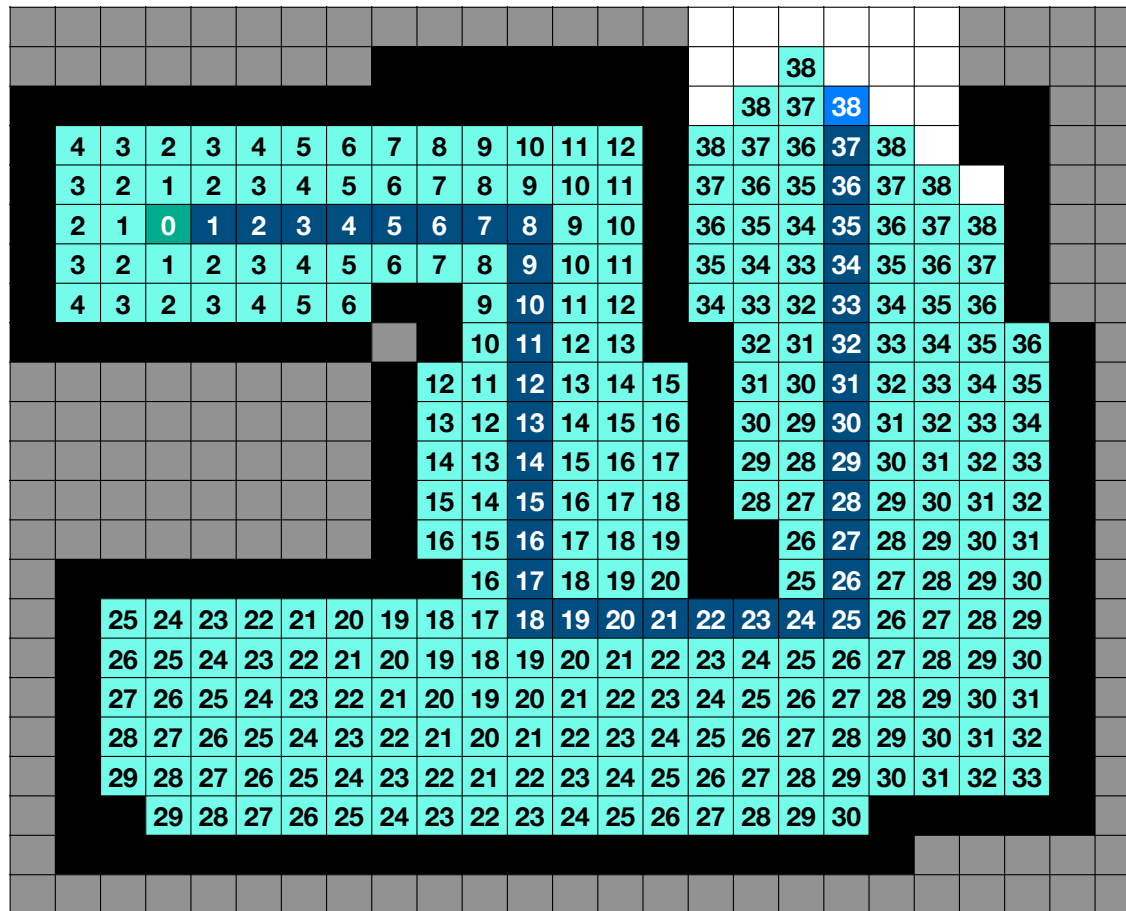
Assign each one plus the smallest distance

Repeat for next set of neighbors



Once goal node reached, perform local search back to start

Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

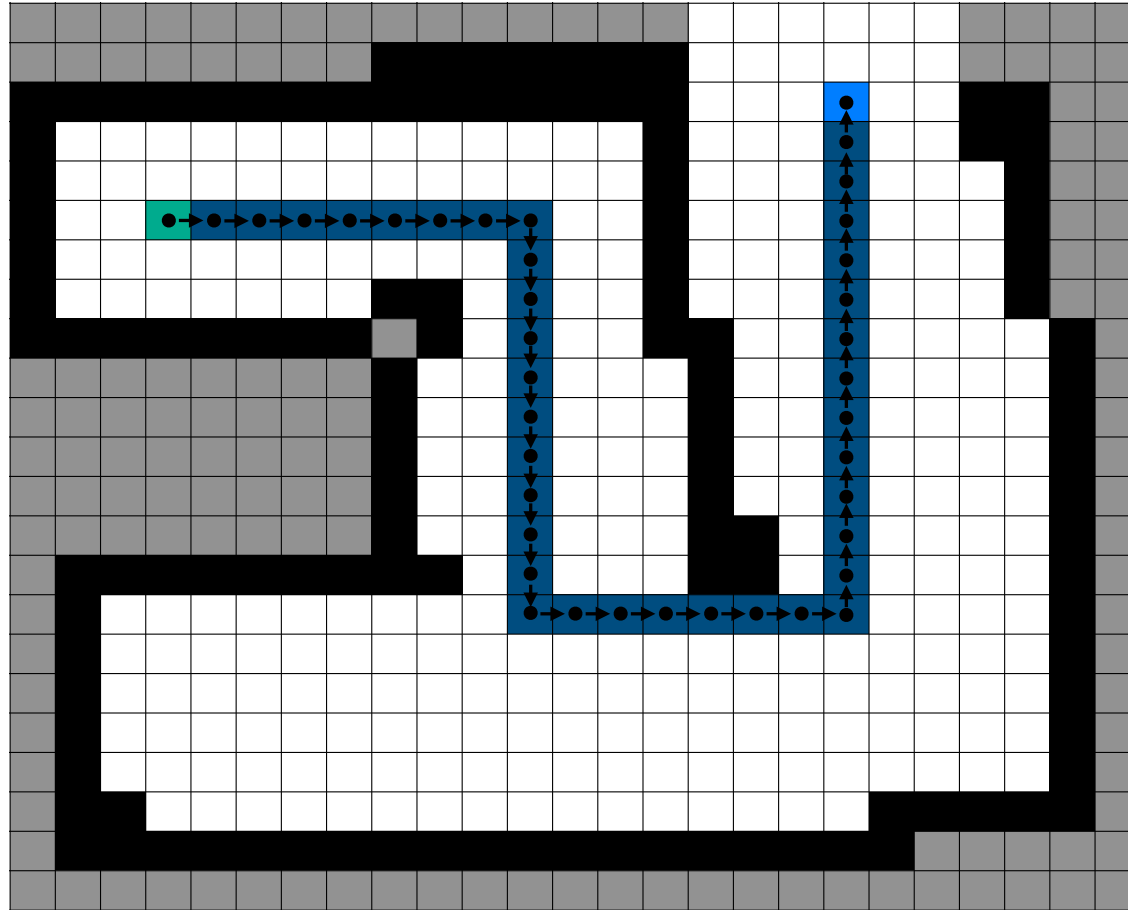
Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

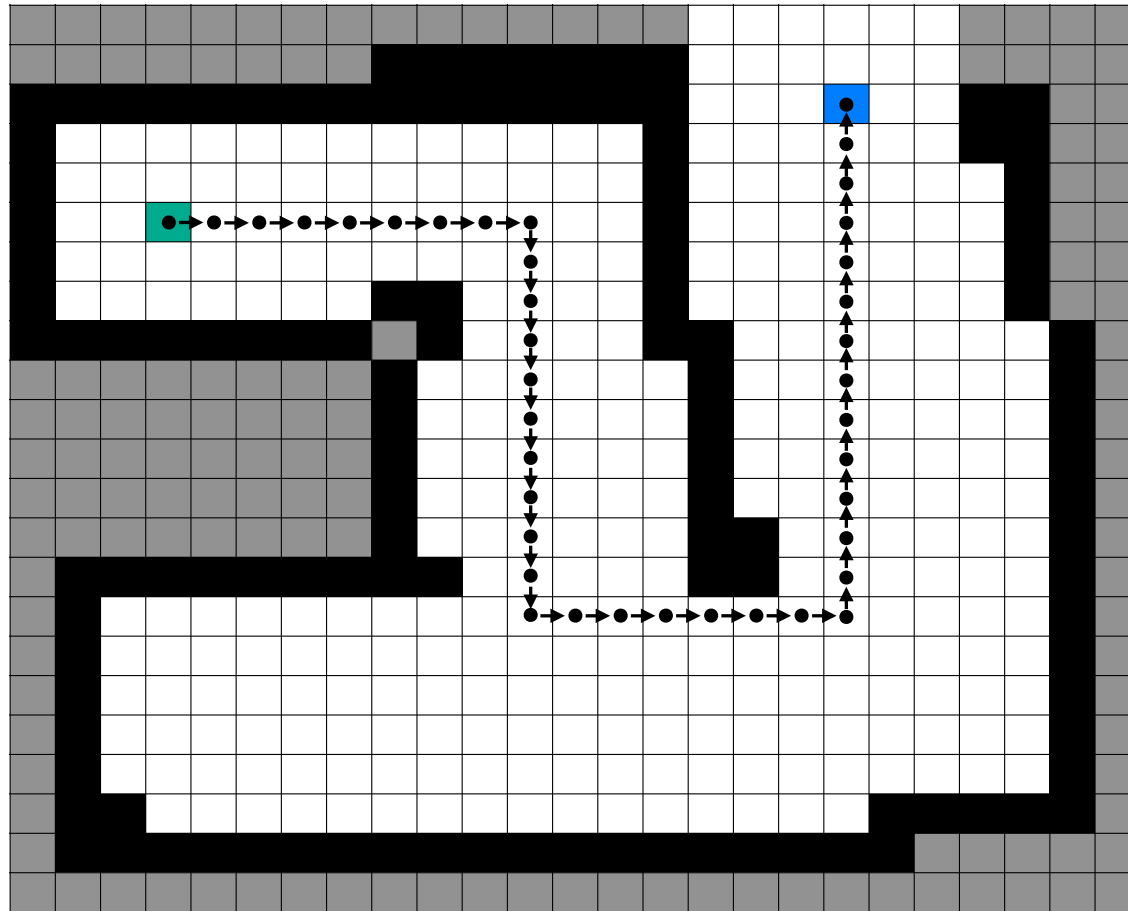


Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

Form list of navigation waypoints

Then, visit the neighbors of nodes just visited



Assign each one plus the smallest distance

Repeat for next set of neighbors

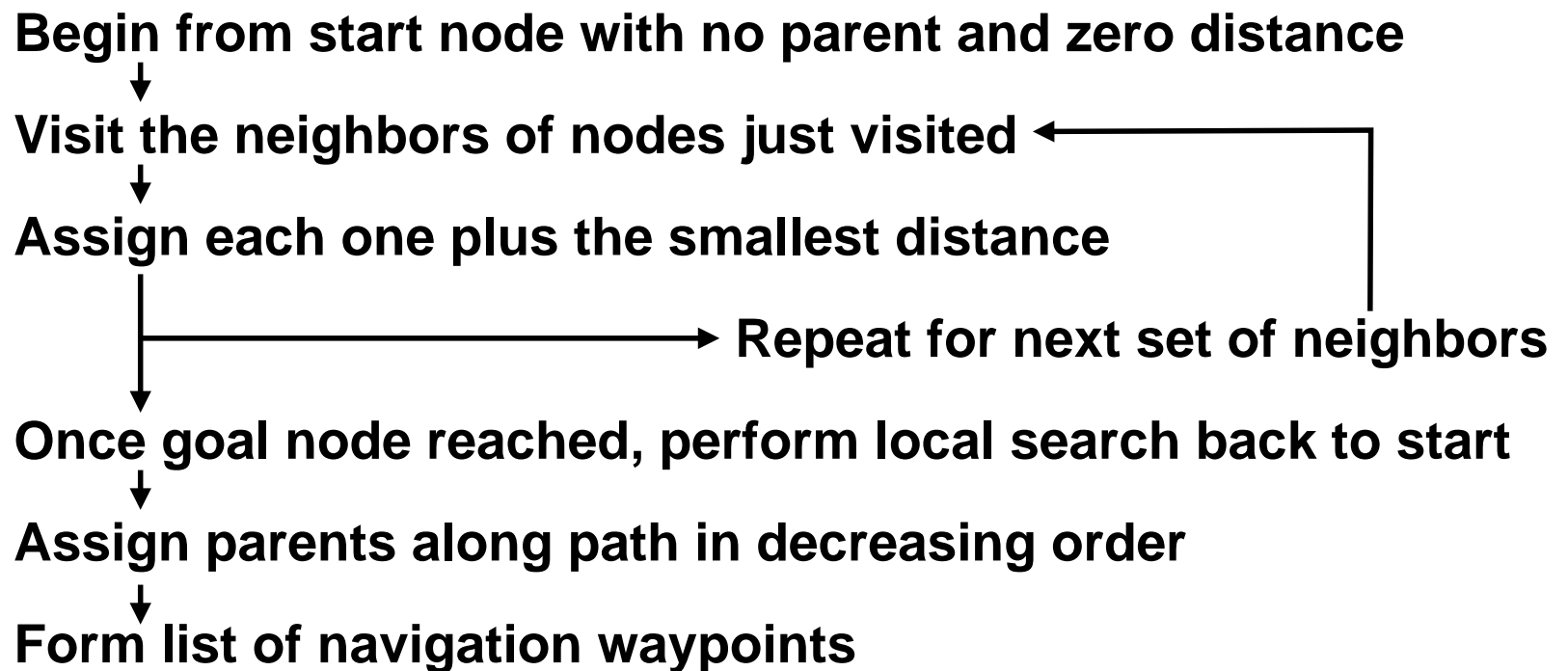
Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

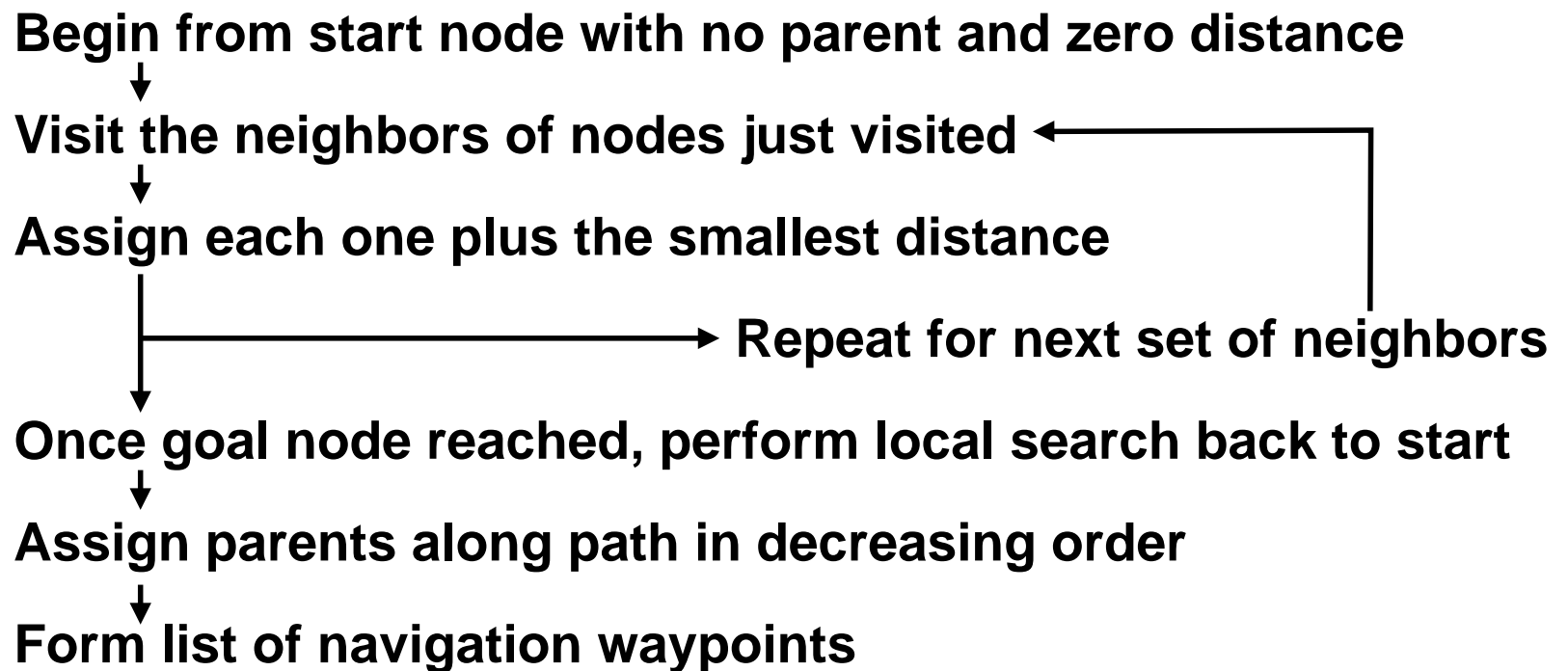
Form list of navigation waypoints

Global search to find routing

***Does this search algorithm
have a name ?***

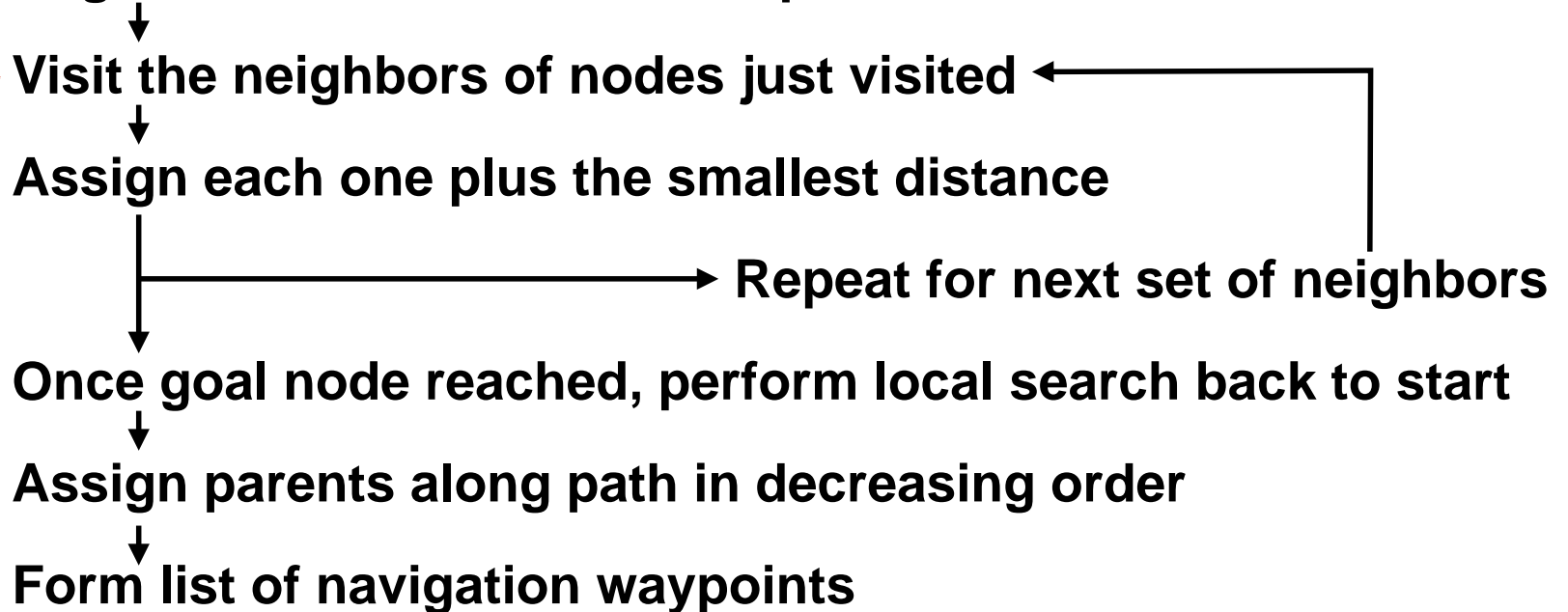


Brushfire Algorithm



Brushfire Algorithm

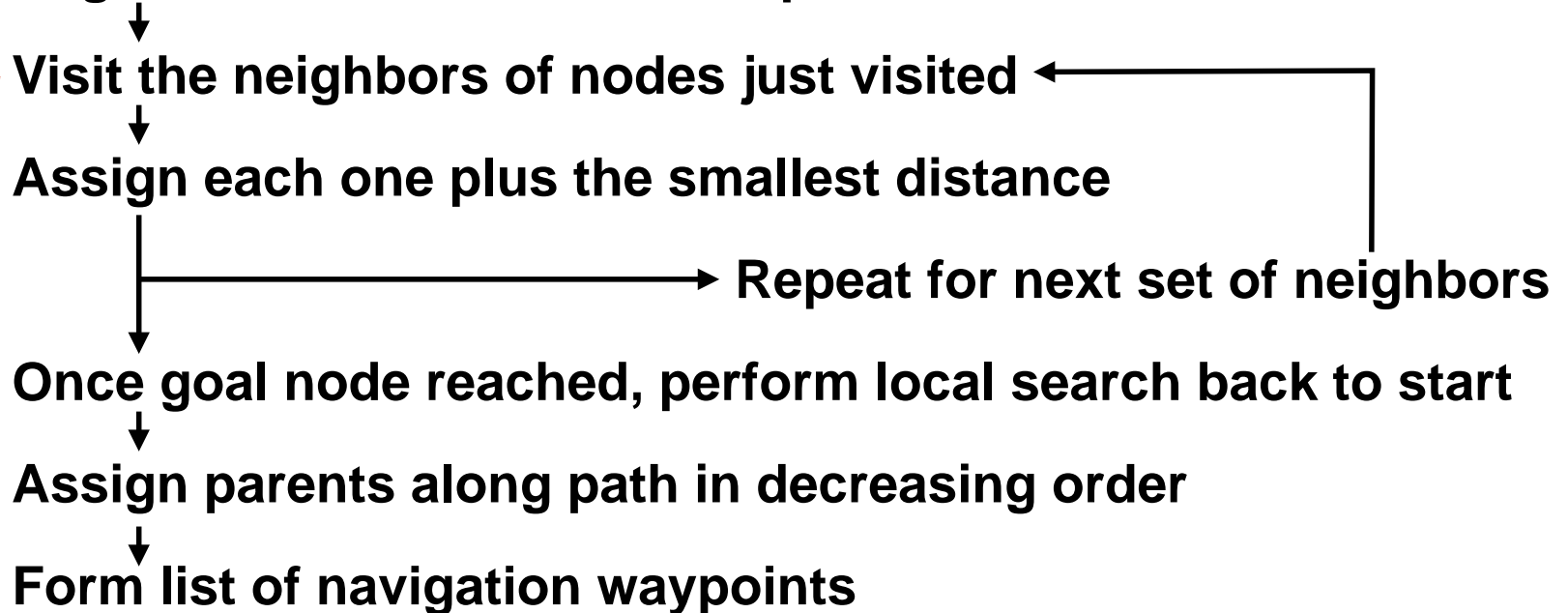
Begin from start node with no parent and zero distance



How to keep track of visited nodes?

Brushfire Algorithm

Begin from start node with no parent and zero distance

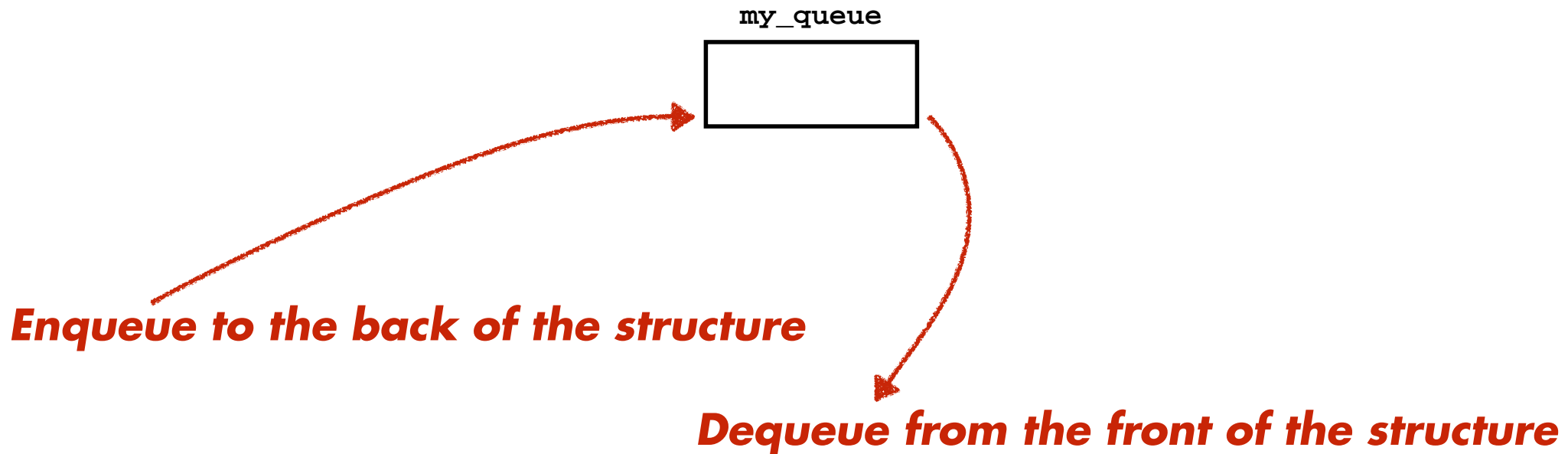


How to keep track of visited nodes?

Queue data structure

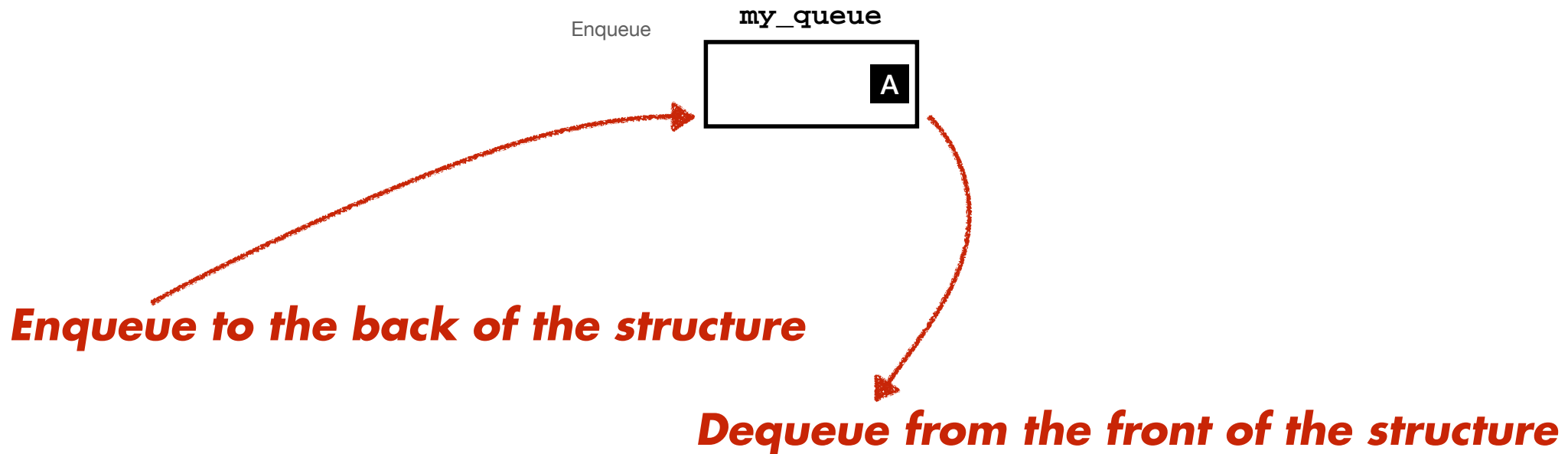
Queue data structure

“First in, first out” (FIFO) data structure



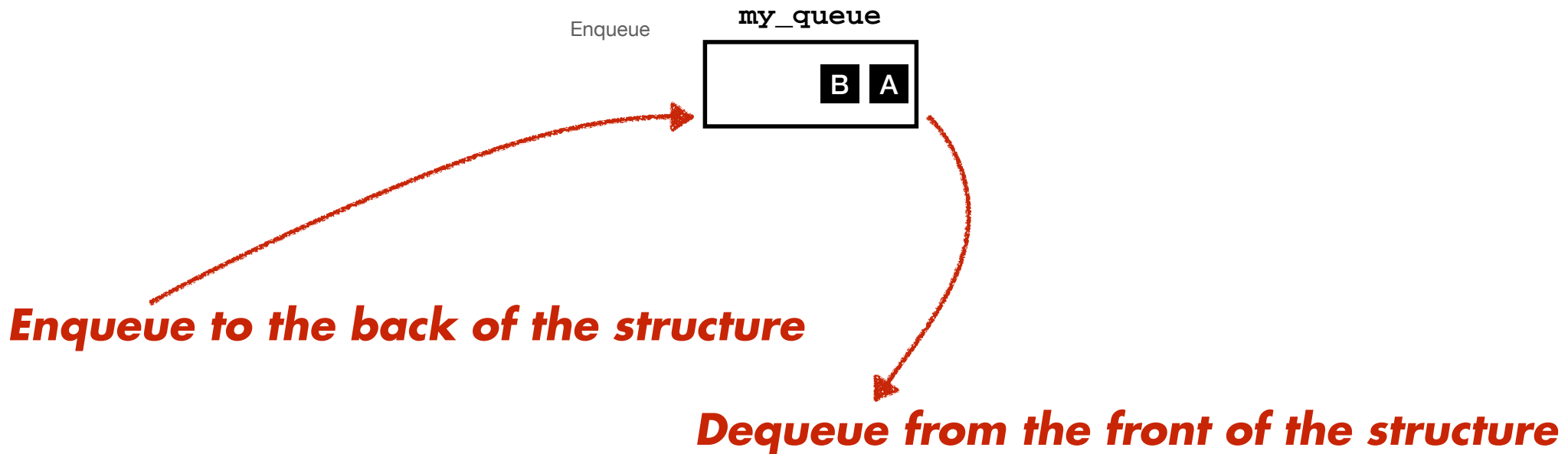
Queue data structure

“First in, first out” (FIFO) data structure



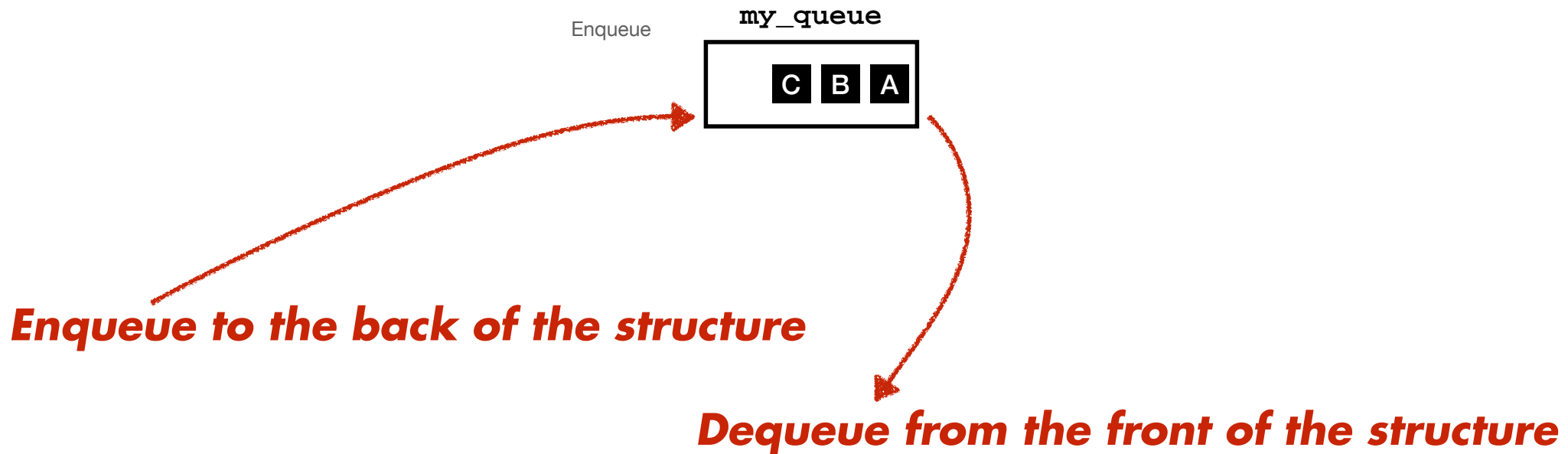
Queue data structure

“First in, first out” (FIFO) data structure



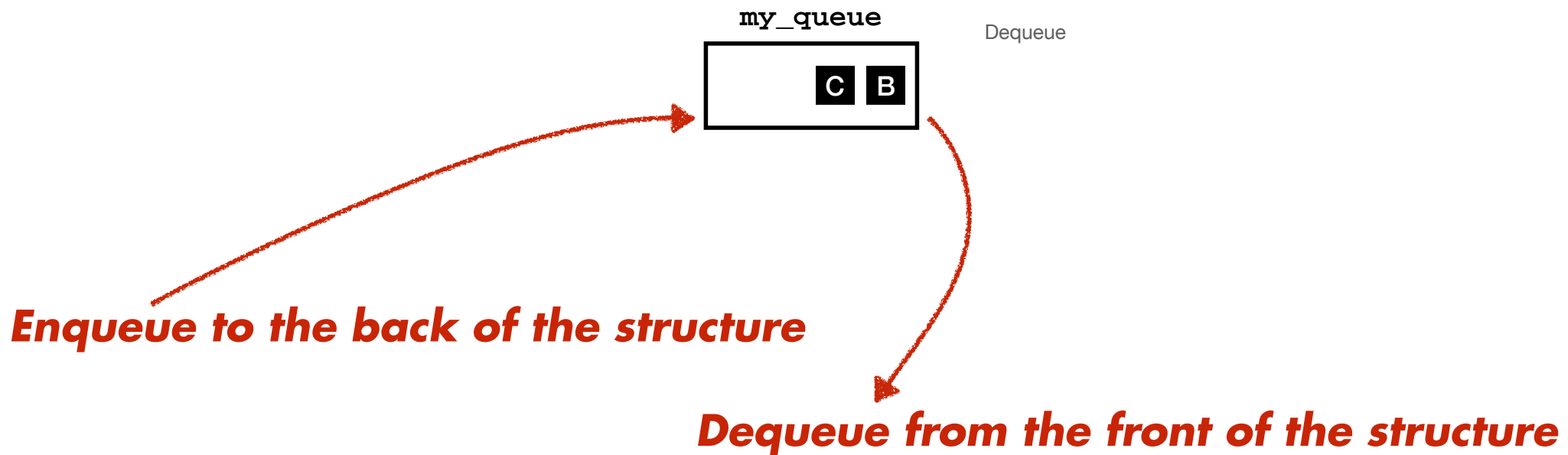
Queue data structure

“First in, first out” (FIFO) data structure



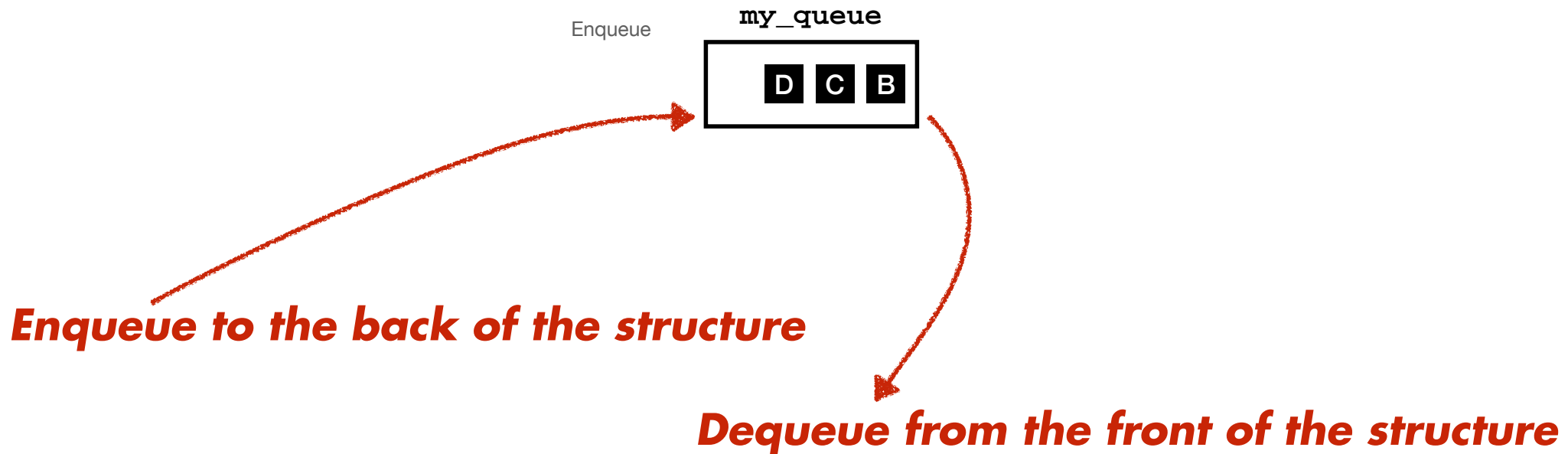
Queue data structure

“First in, first out” (FIFO) data structure



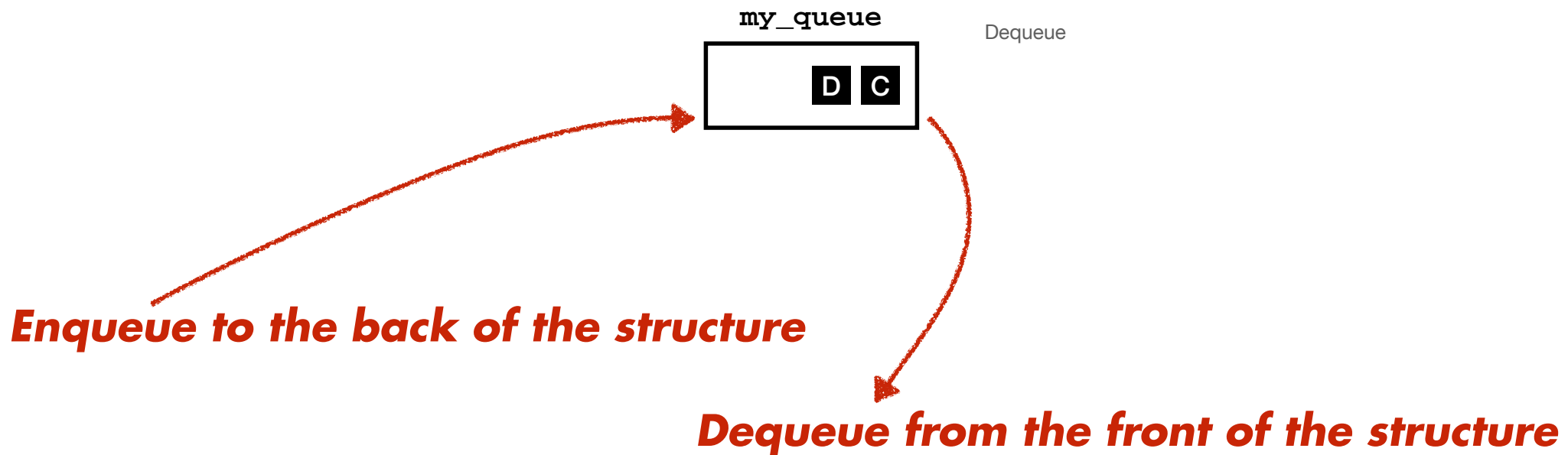
Queue data structure

“First in, first out” (FIFO) data structure



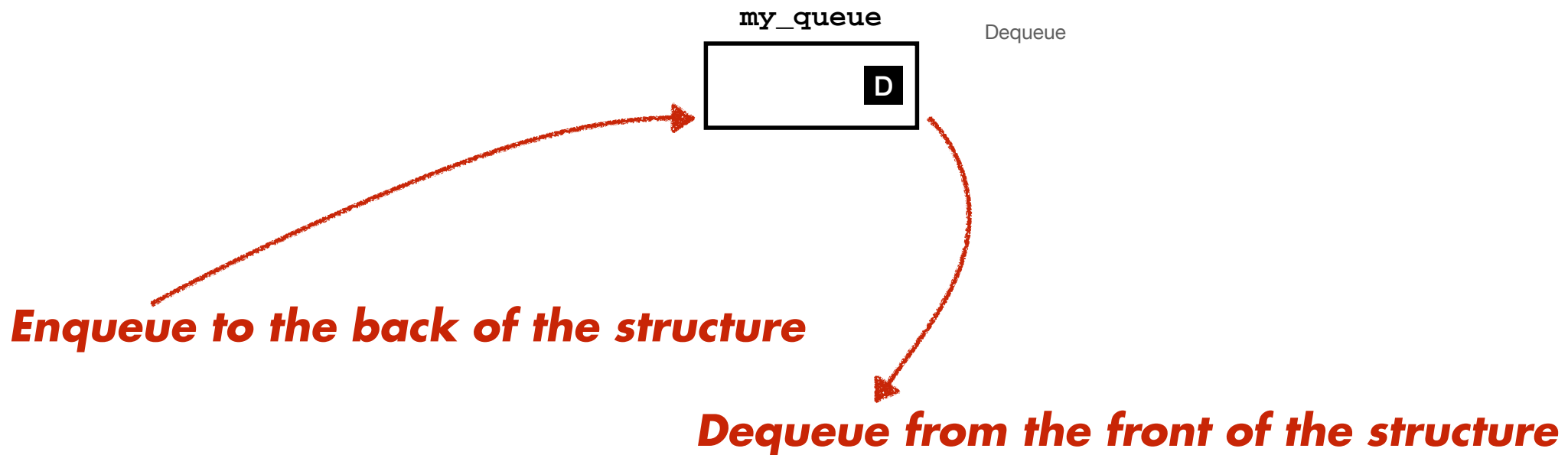
Queue data structure

“First in, first out” (FIFO) data structure



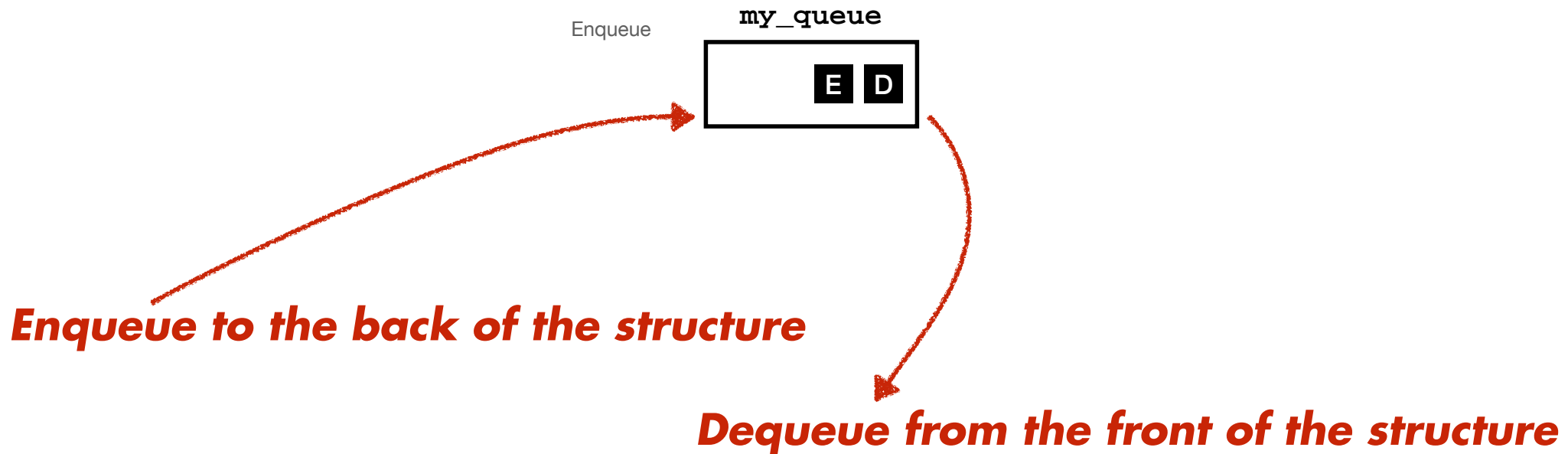
Queue data structure

“First in, first out” (FIFO) data structure



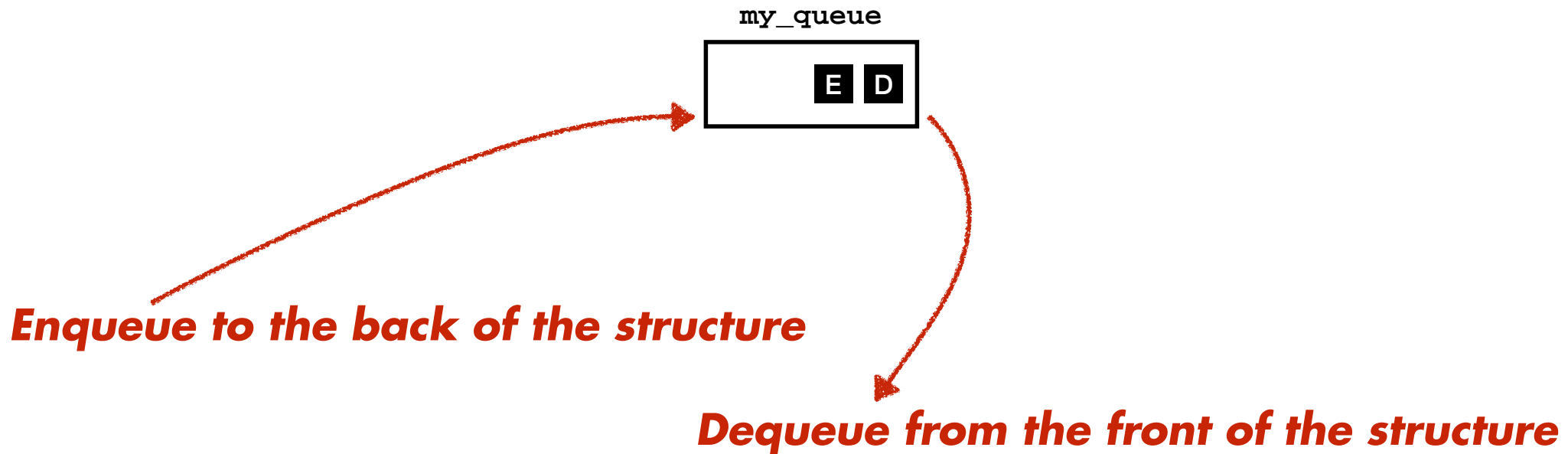
Queue data structure

“First in, first out” (FIFO) data structure



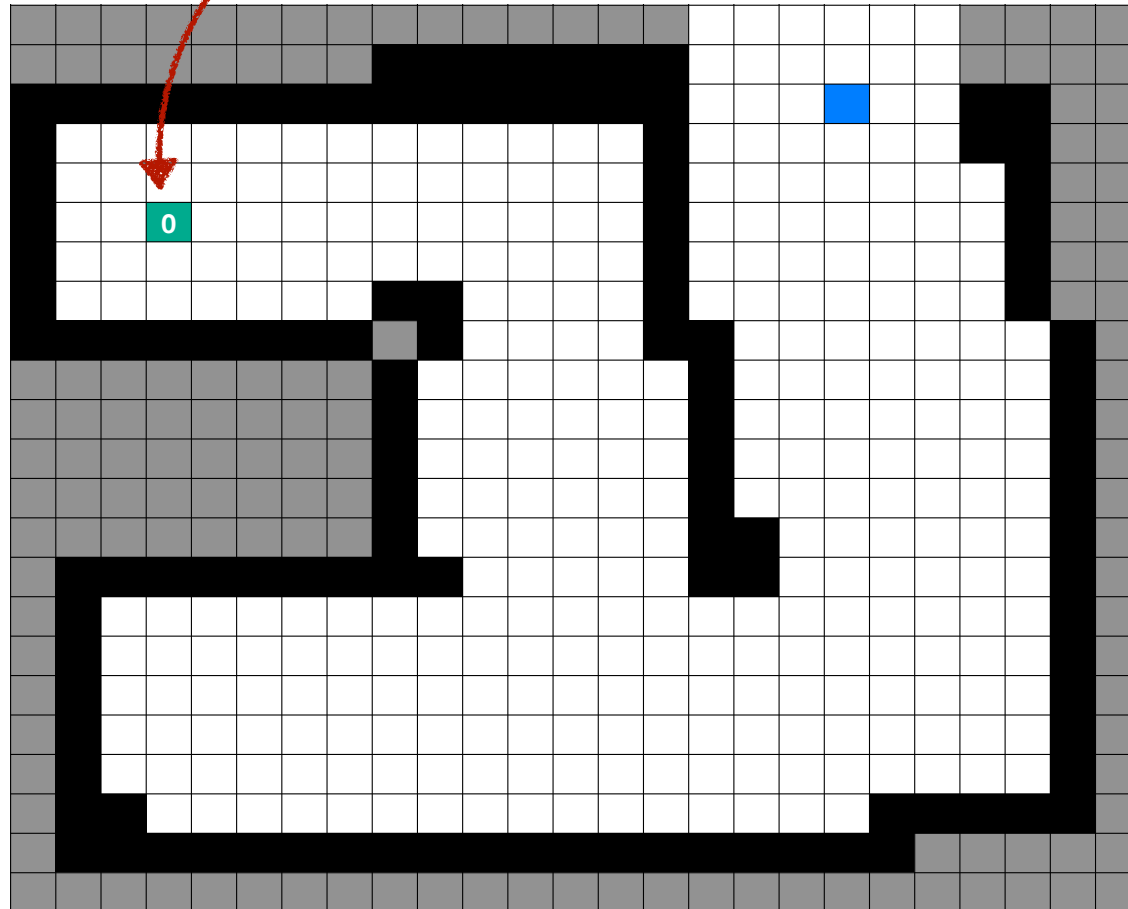
Queue data structure

“First in, first out” (FIFO) data structure



**Begin from
start node
with
no parent and
zero distance**

Going back to our example from the root node

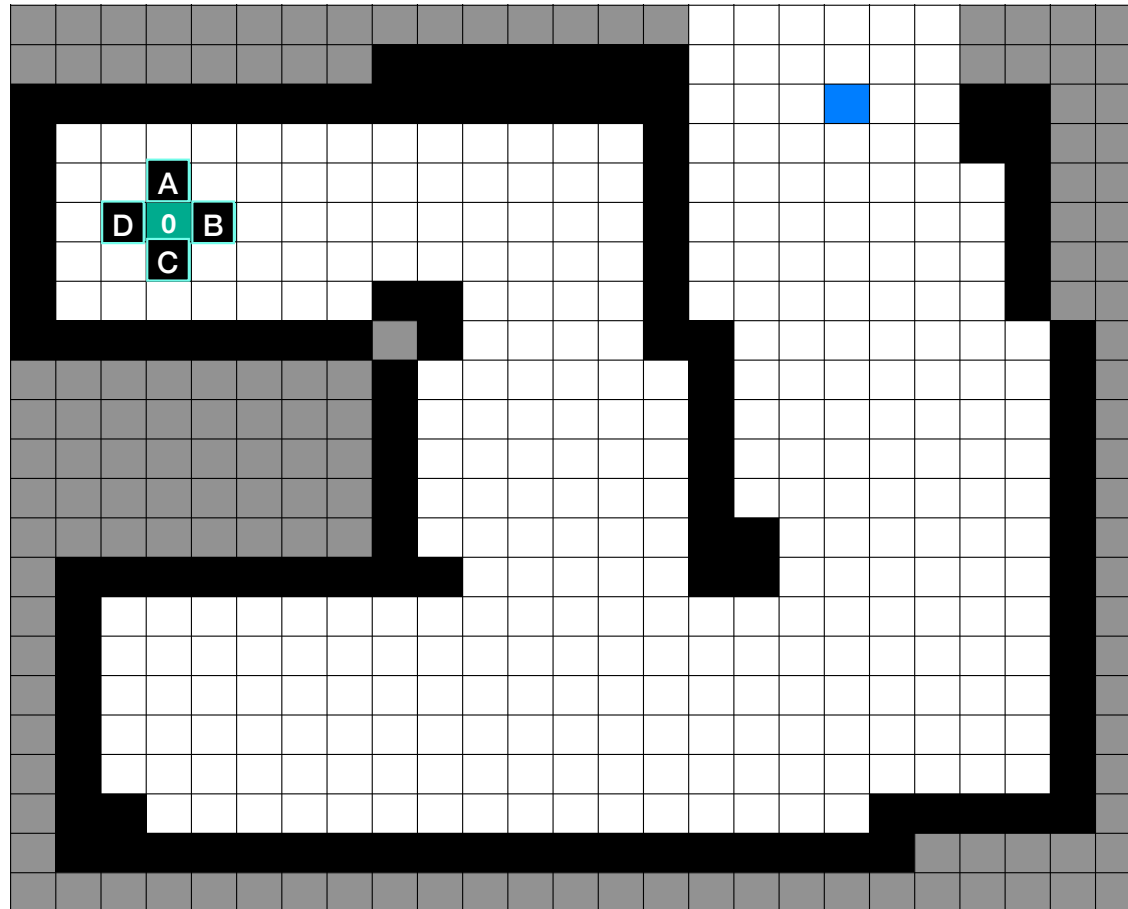


visit_queue



*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*

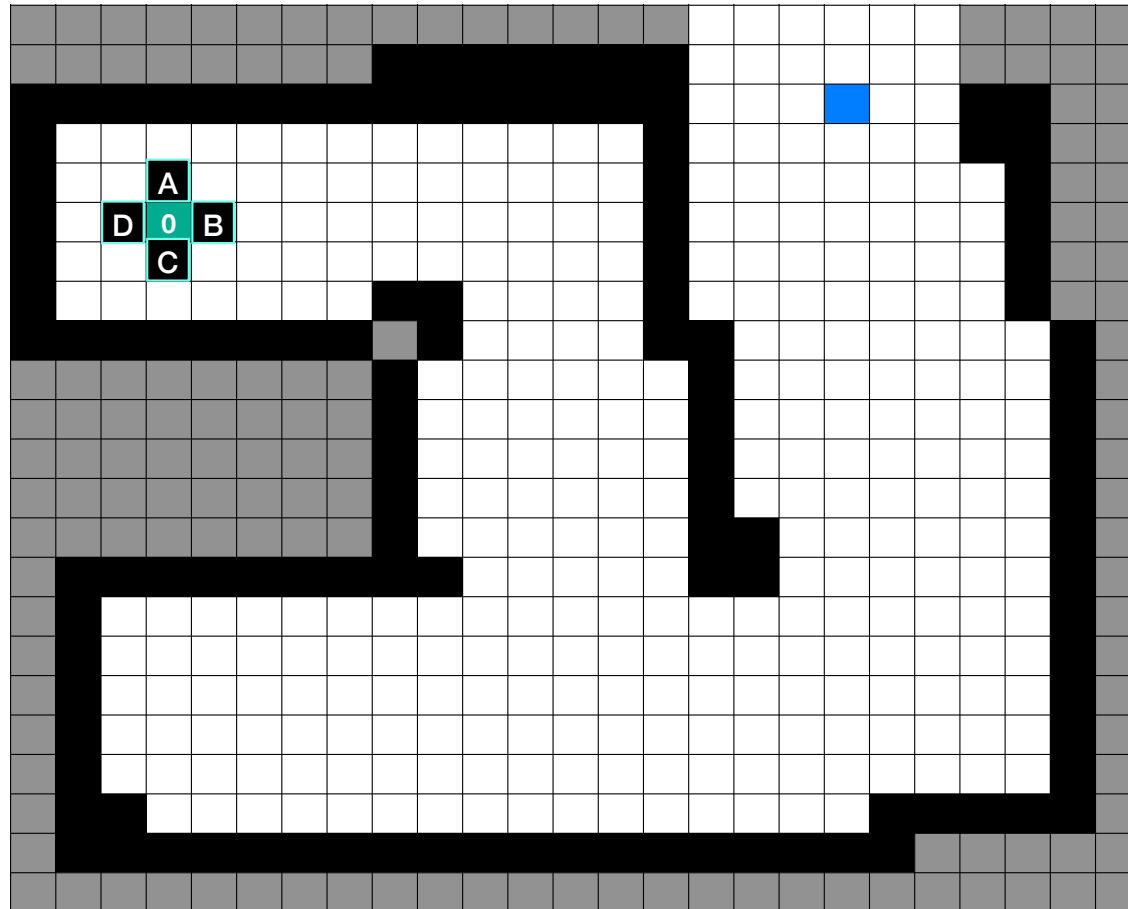


visit_queue



*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*

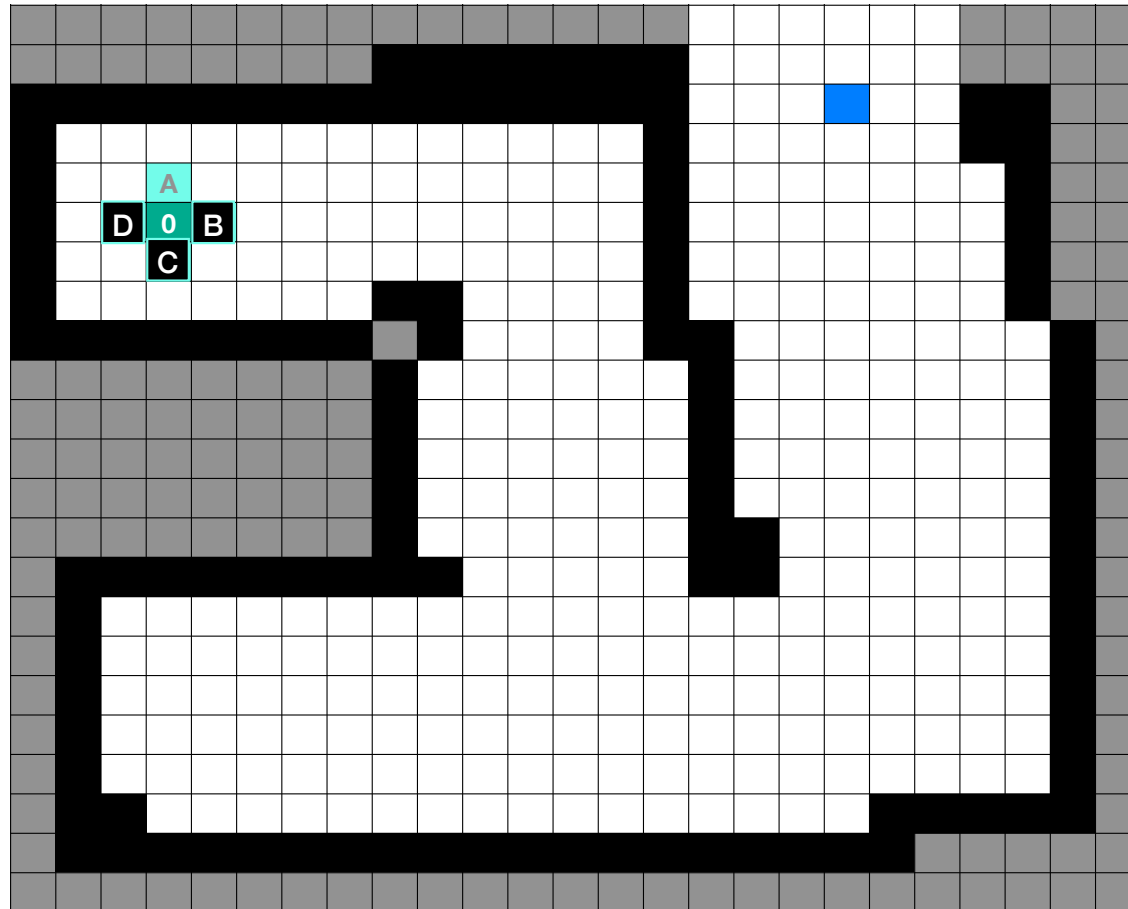


visit_queue



*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*



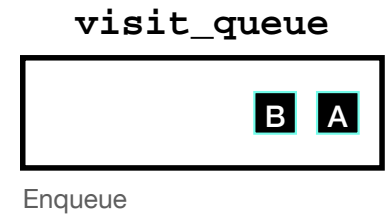
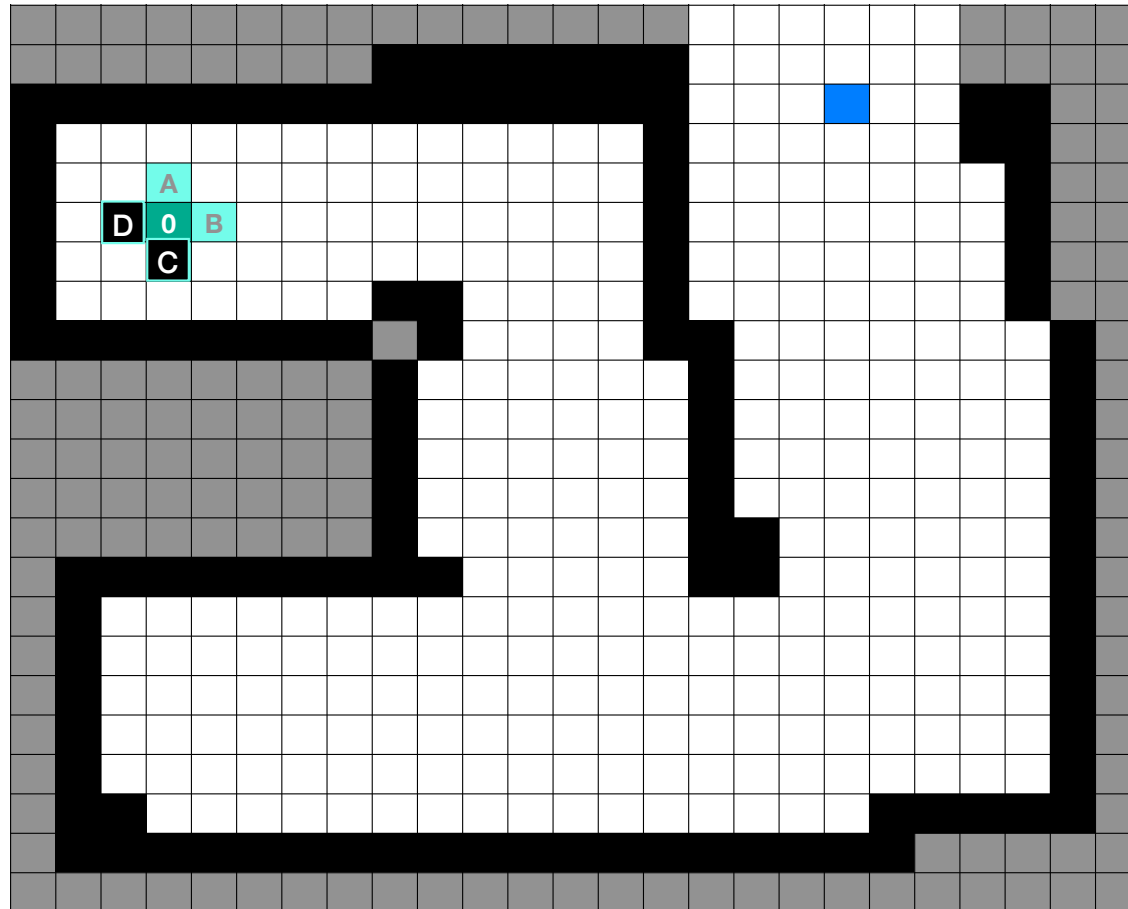
visit_queue



Enqueue

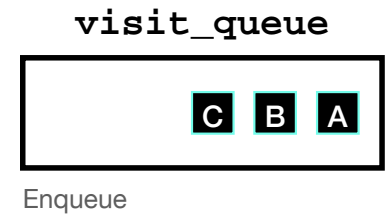
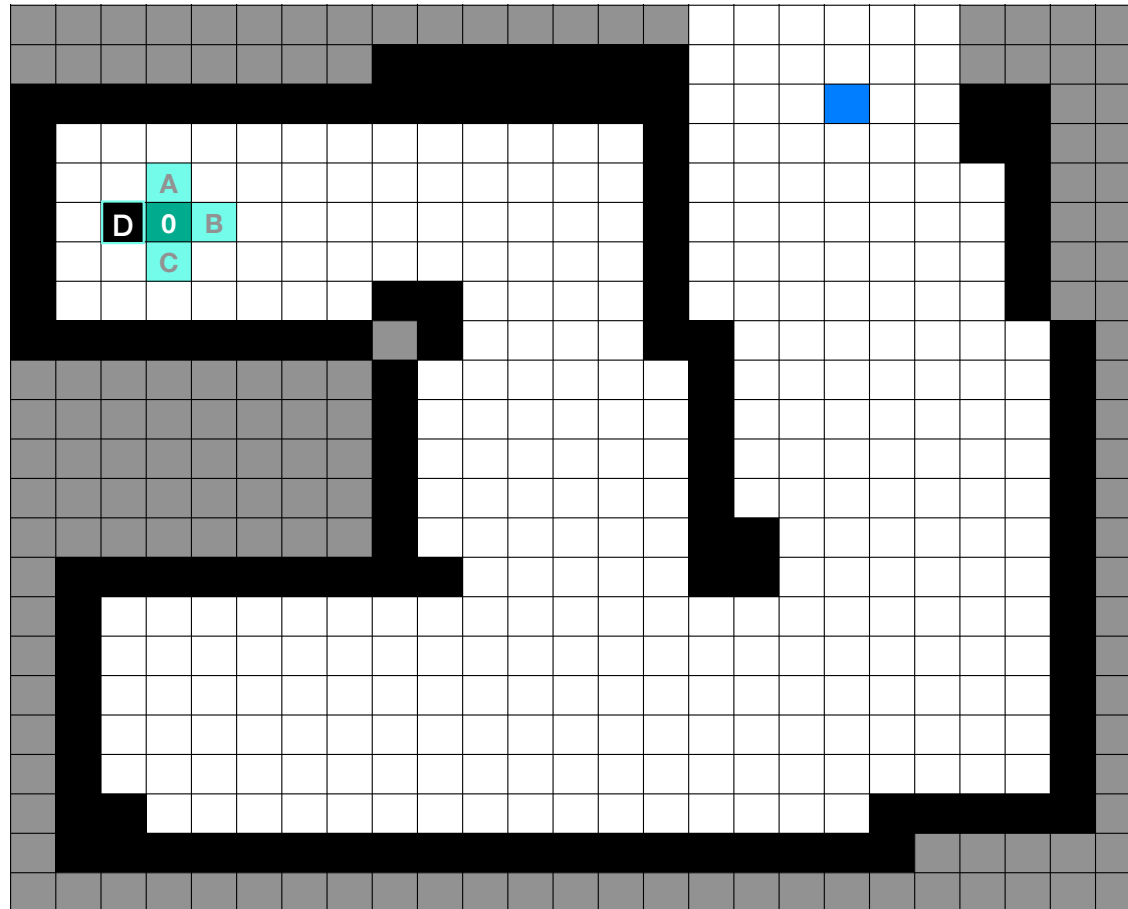
*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*



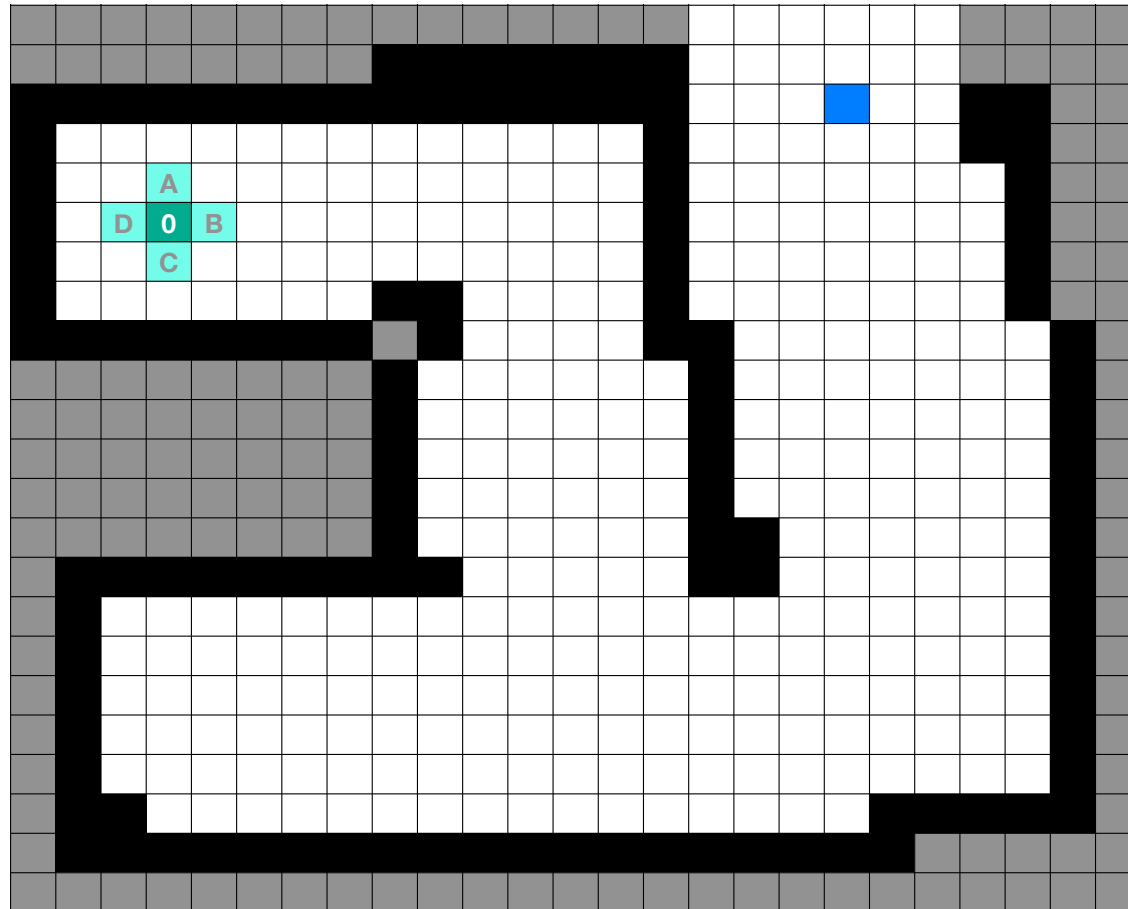
*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*

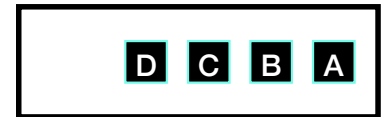


*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*



visit_queue

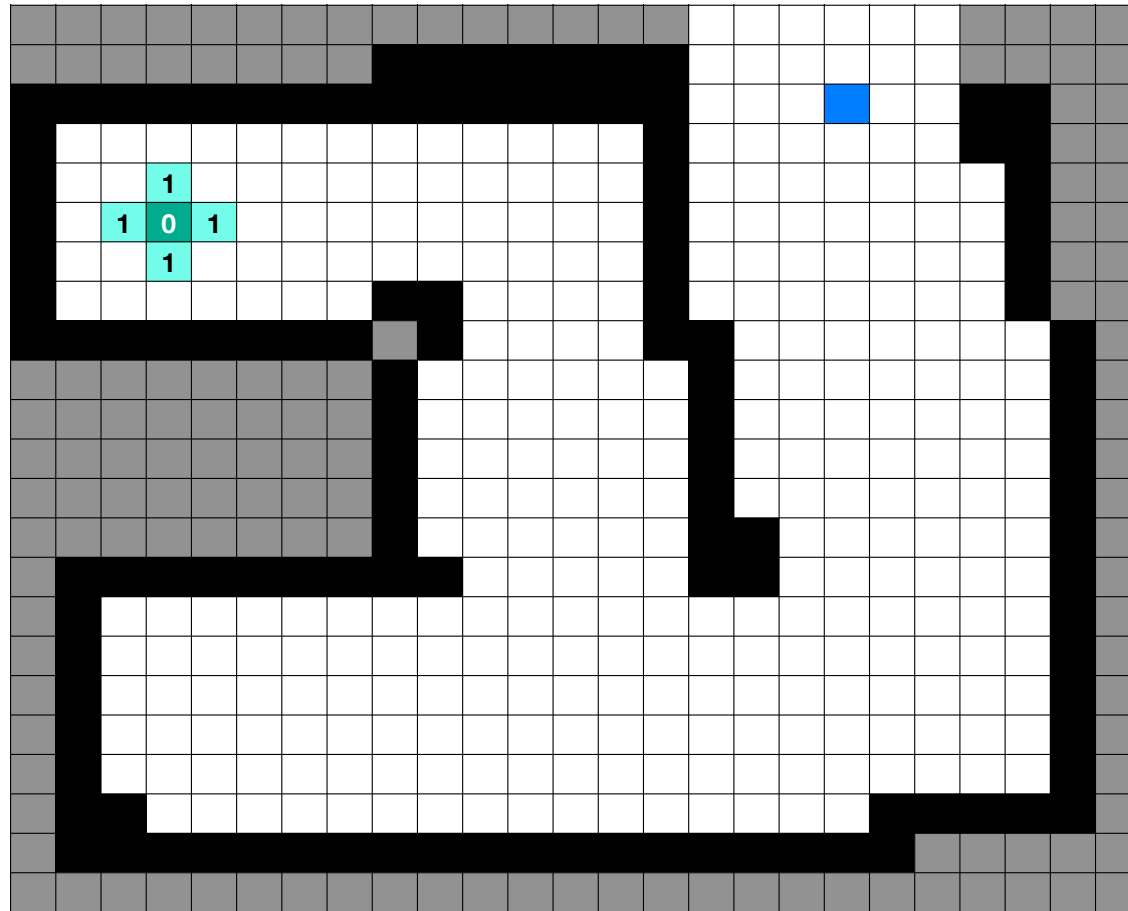


Enqueue

*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
"queued"*

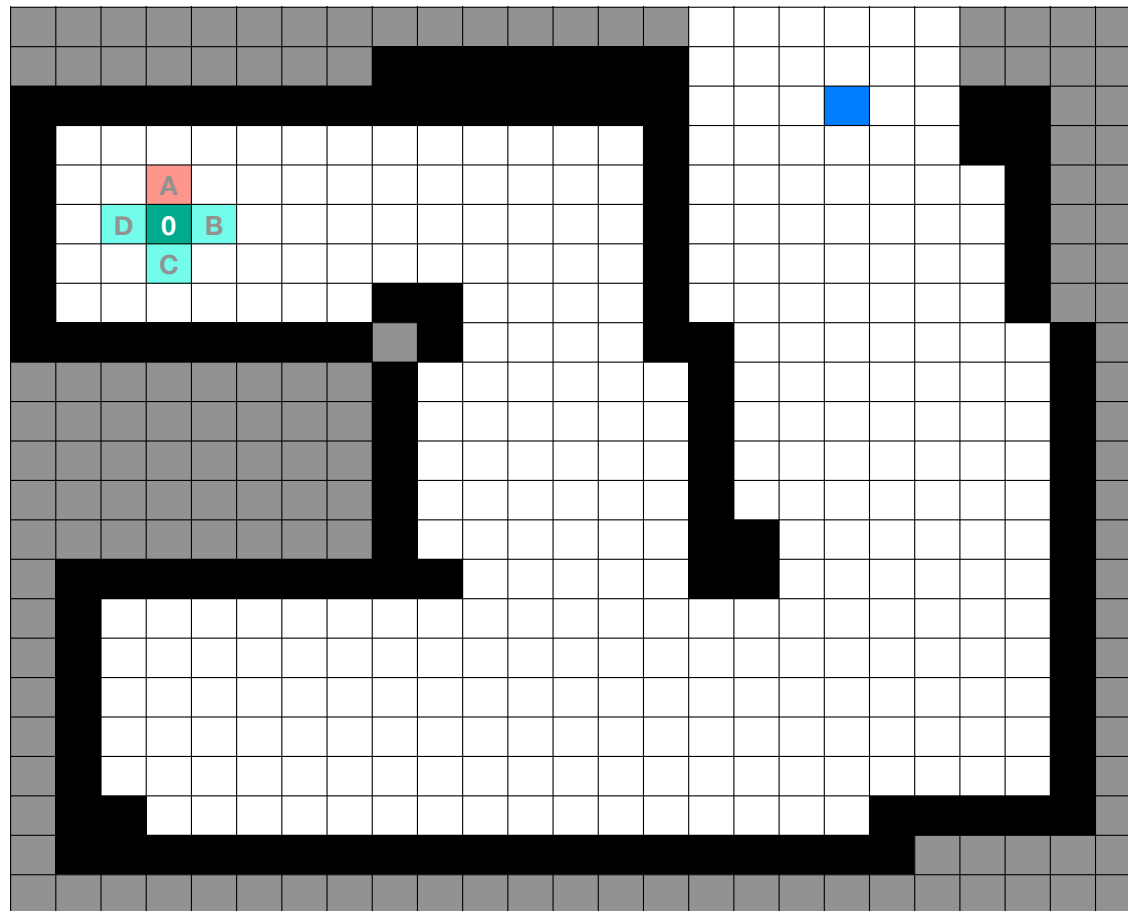
*and assigned
distance as
one plus start
node distance*



visit_queue

D C B A

**Repeat for
next node in
the queue**



visit_queue



Dequeue

A

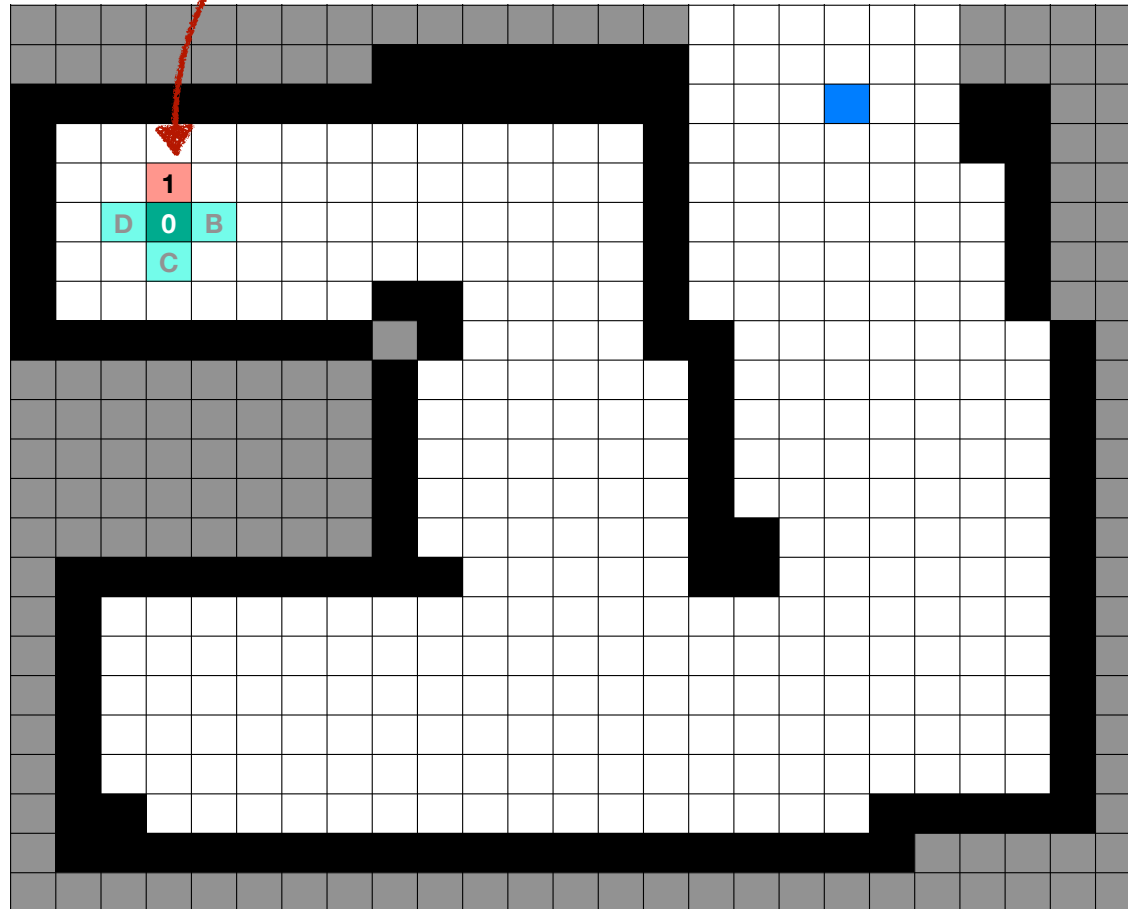
current_node

*All neighbors
of current node
are "queued"*

*and assigned
distance as one
plus current
node distance*

Path distance at current node was already assigned in previous iteration

Repeat for next node in the queue



All neighbors of current node are "queued"

and assigned distance as one plus current node distance

visit_queue



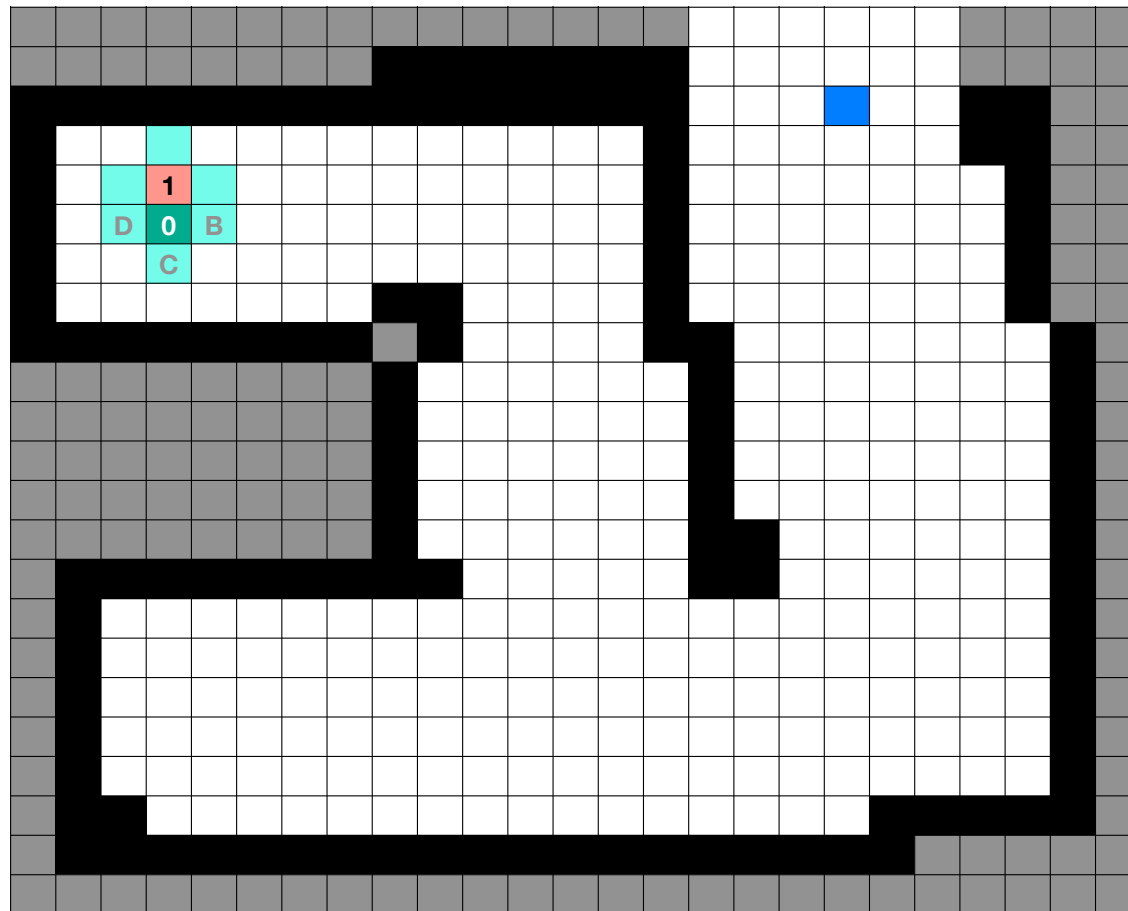
A

current_node

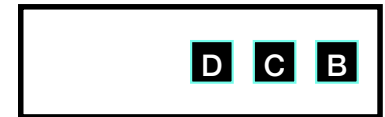
Repeat for next node in the queue

All neighbors of current node are "queued"

and assigned distance as one plus current node distance



visit_queue



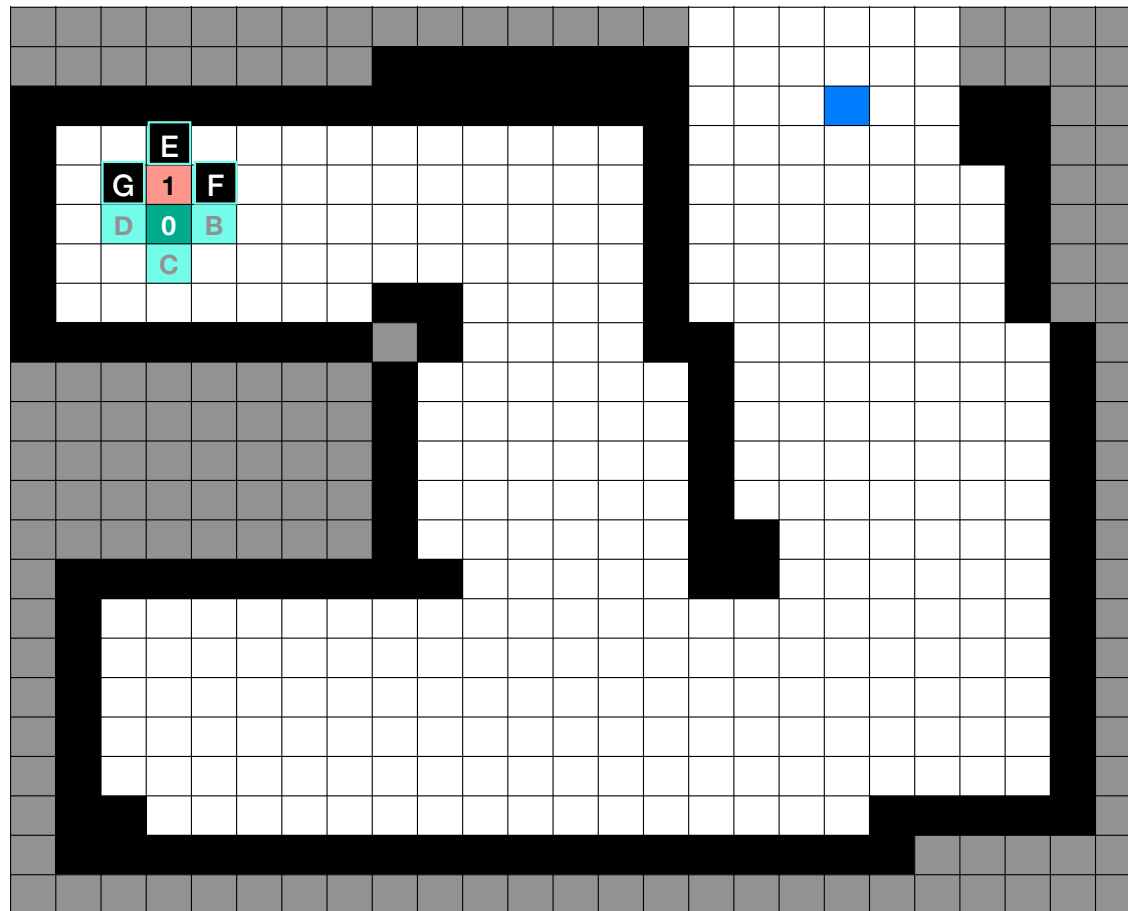
A

current_node

Repeat for next node in the queue

All neighbors of current node are "queued"

and assigned distance as one plus current node distance



visit_queue

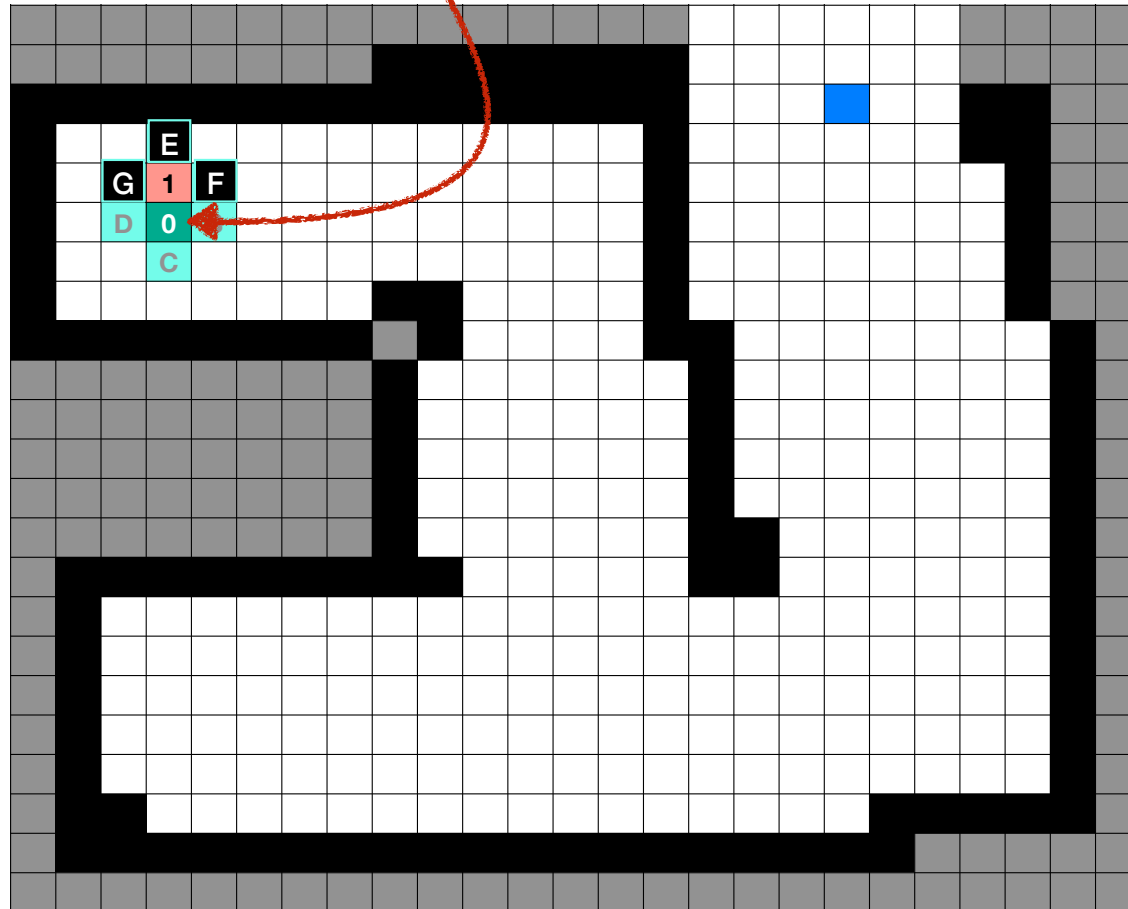


A

current_node

Do not revisit or re-enqueue nodes

Repeat for next node in the queue



All neighbors of current node are "queued"

and assigned distance as one plus current node distance

visit_queue



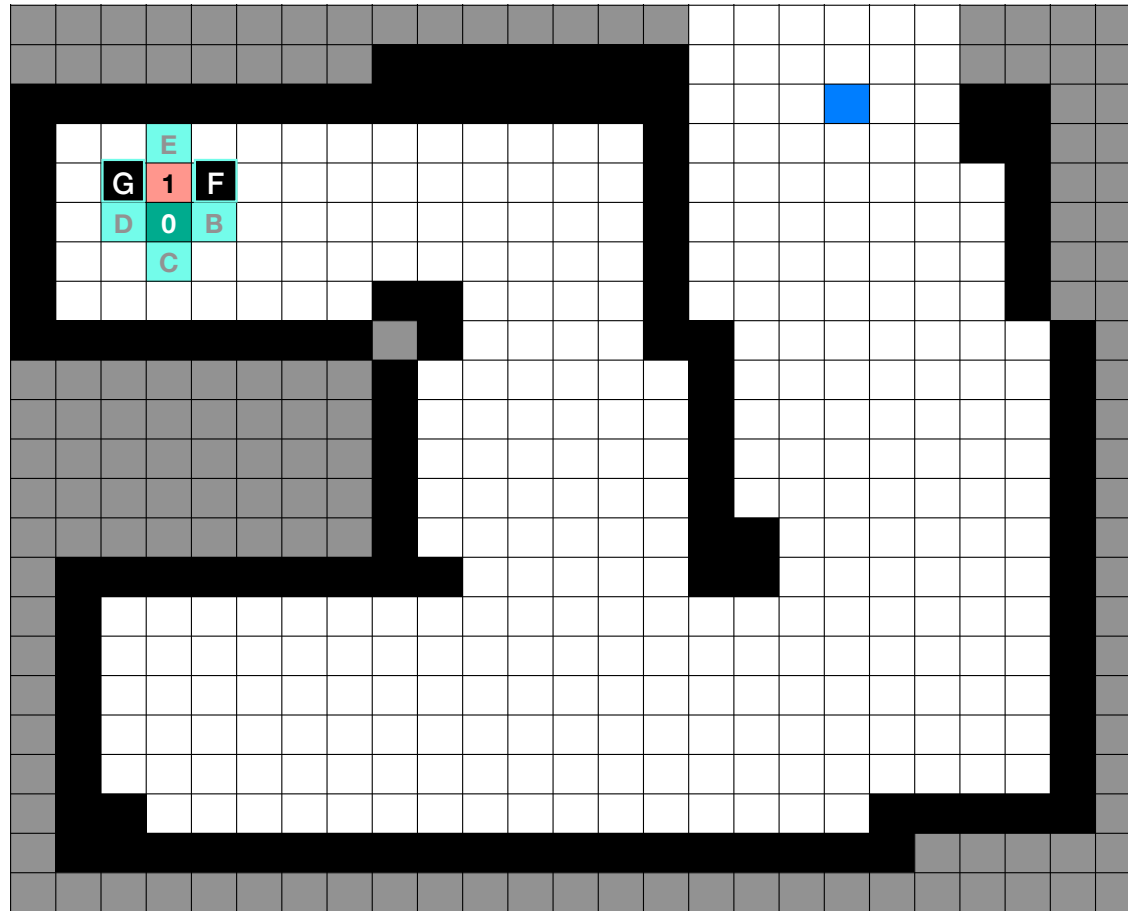
A

current_node

*Repeat for
next node in
the queue*

*All neighbors
of current node
are "queued"*

*and assigned
distance as one
plus current
node distance*



visit_queue



Enqueue

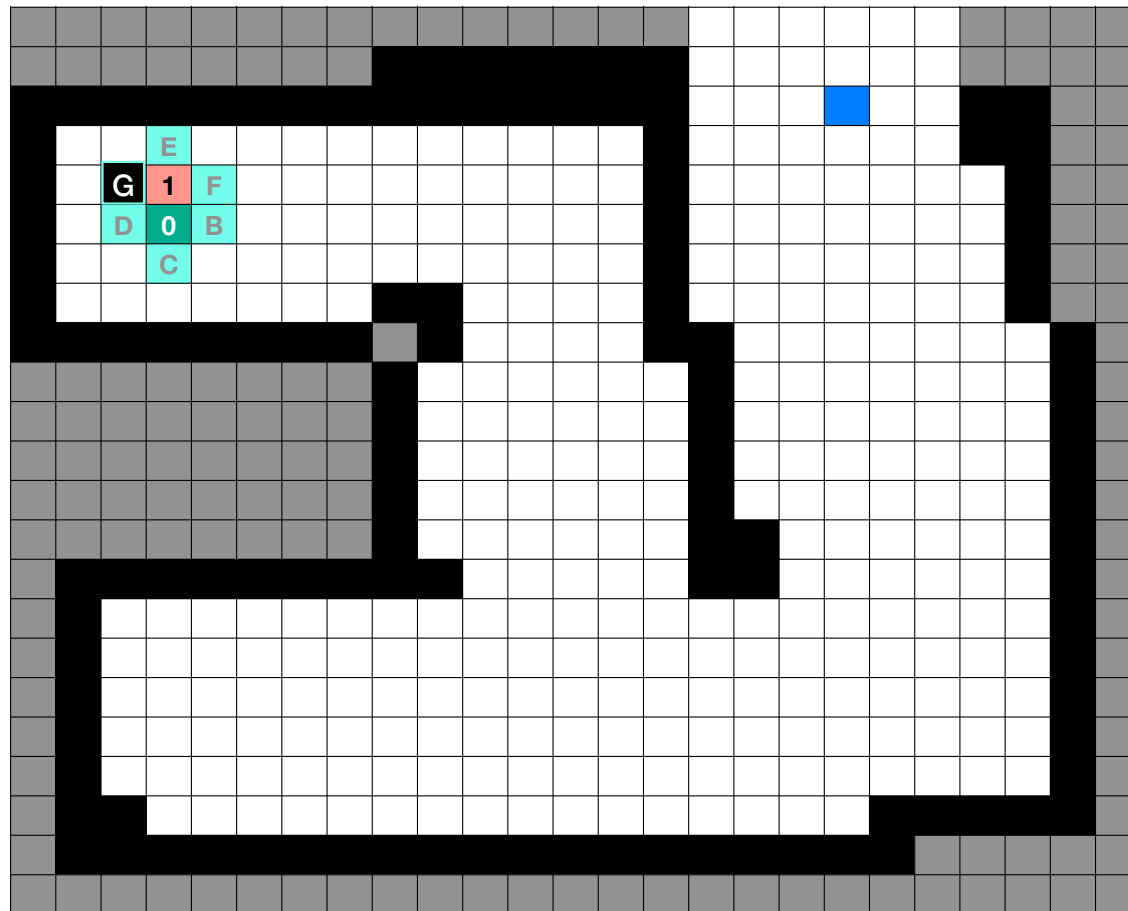
A

current_node

Repeat for next node in the queue

All neighbors of current node are "queued"

and assigned distance as one plus current node distance



visit_queue

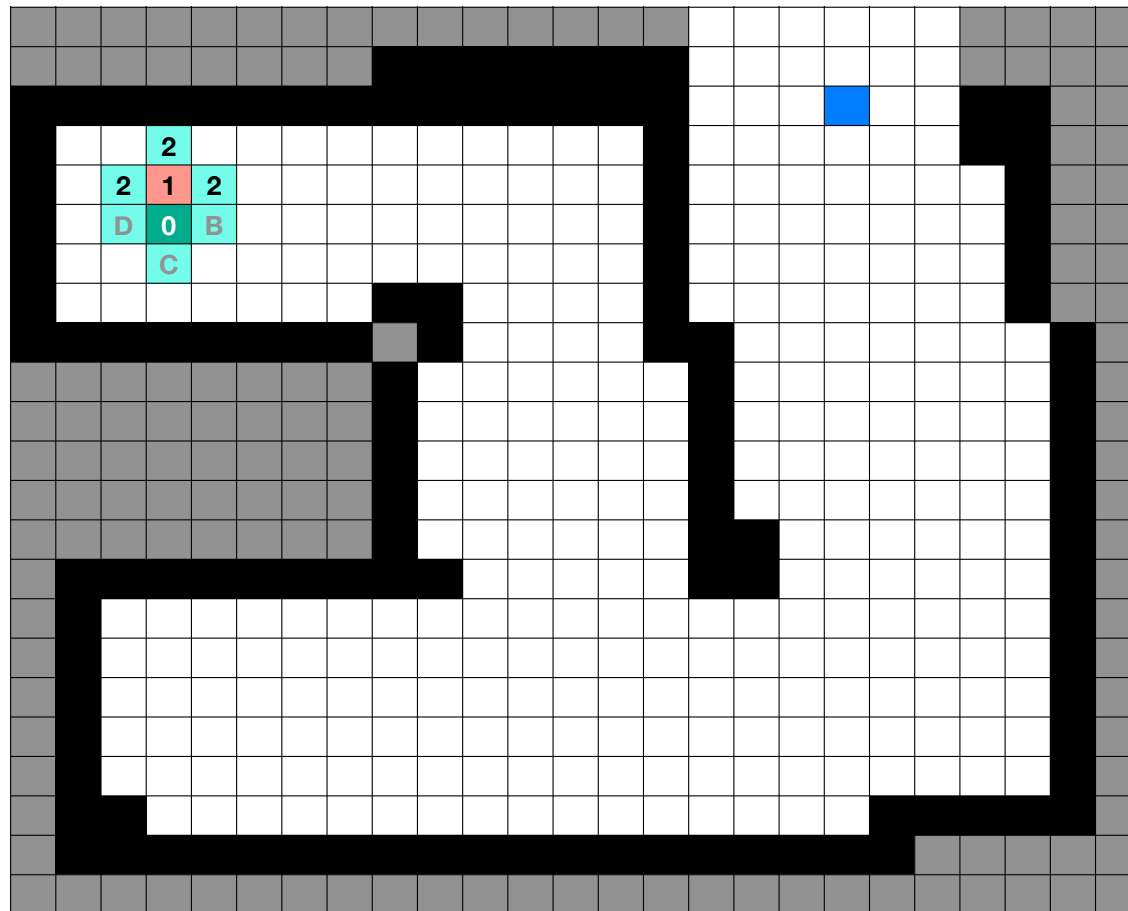


Enqueue

A

current_node

Repeat for next node in the queue



All neighbors of current node are "queued"

and assigned distance as one plus current node distance

visit_queue

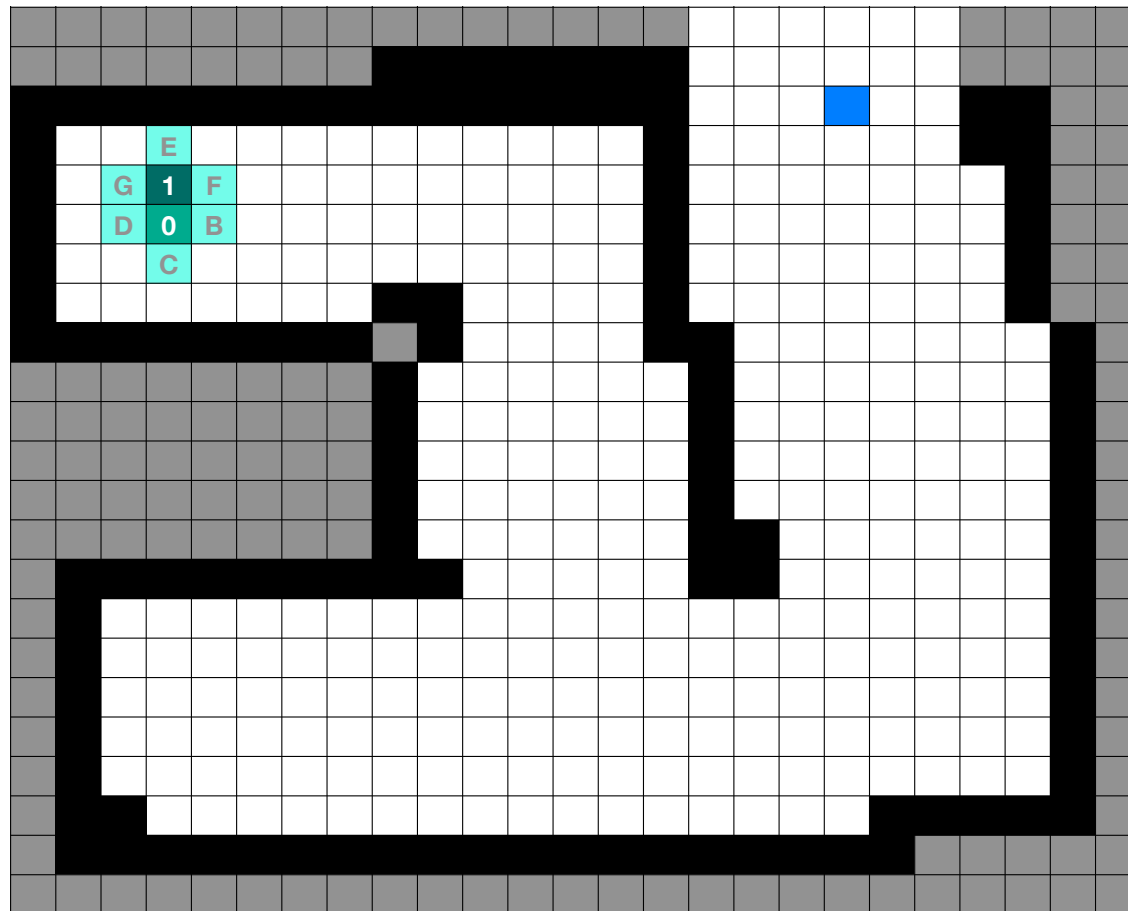


Enqueue

A

current_node

Repeat for next node in the queue



All neighbors of current node are "queued"

and assigned distance as one plus current node distance

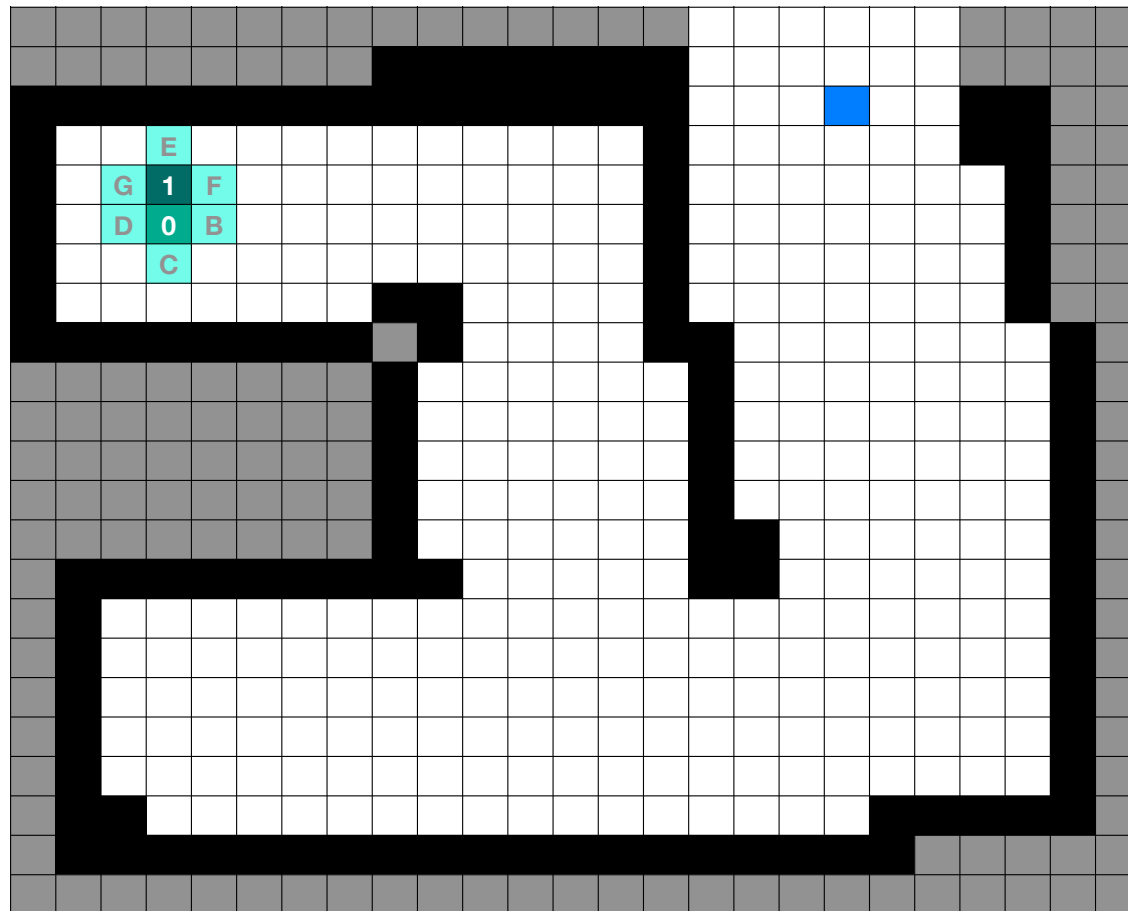
visit_queue



current_node

Node A
done being processed

**Repeat for
next node in
the queue**



visit_queue

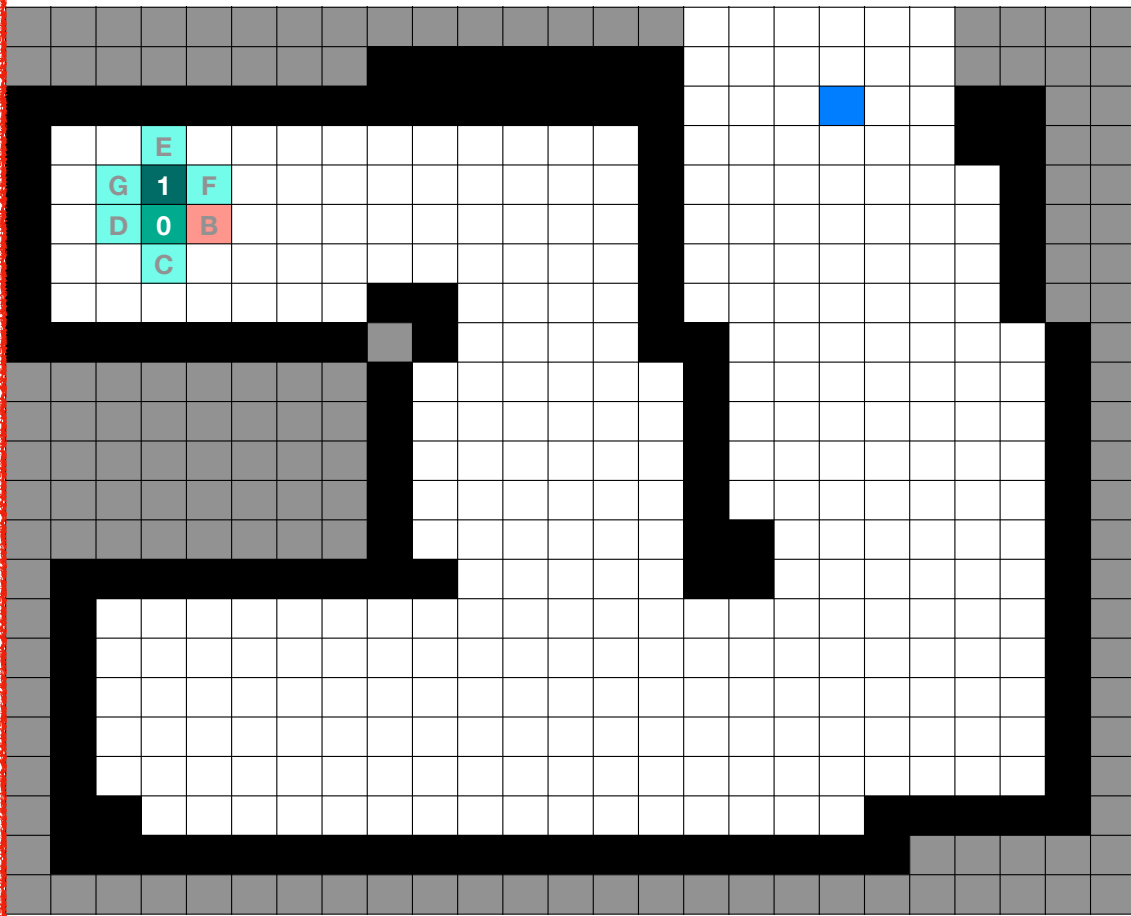


current_node

*All neighbors
of current node
are "queued"*

*and assigned
distance as one
plus current
node distance*

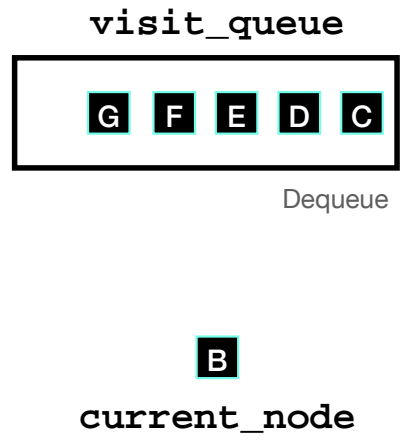
Continue until goal reached or queue is empty



Repeat for next node in the queue

All neighbors of current node are "queued"

and assigned distance as one plus current node distance



How to keep track of visited nodes?

Queue data structure

Begin from start node with no parent and zero distance

↓
Visit the neighbors of nodes just visited

↓
Assign each one plus the smallest distance

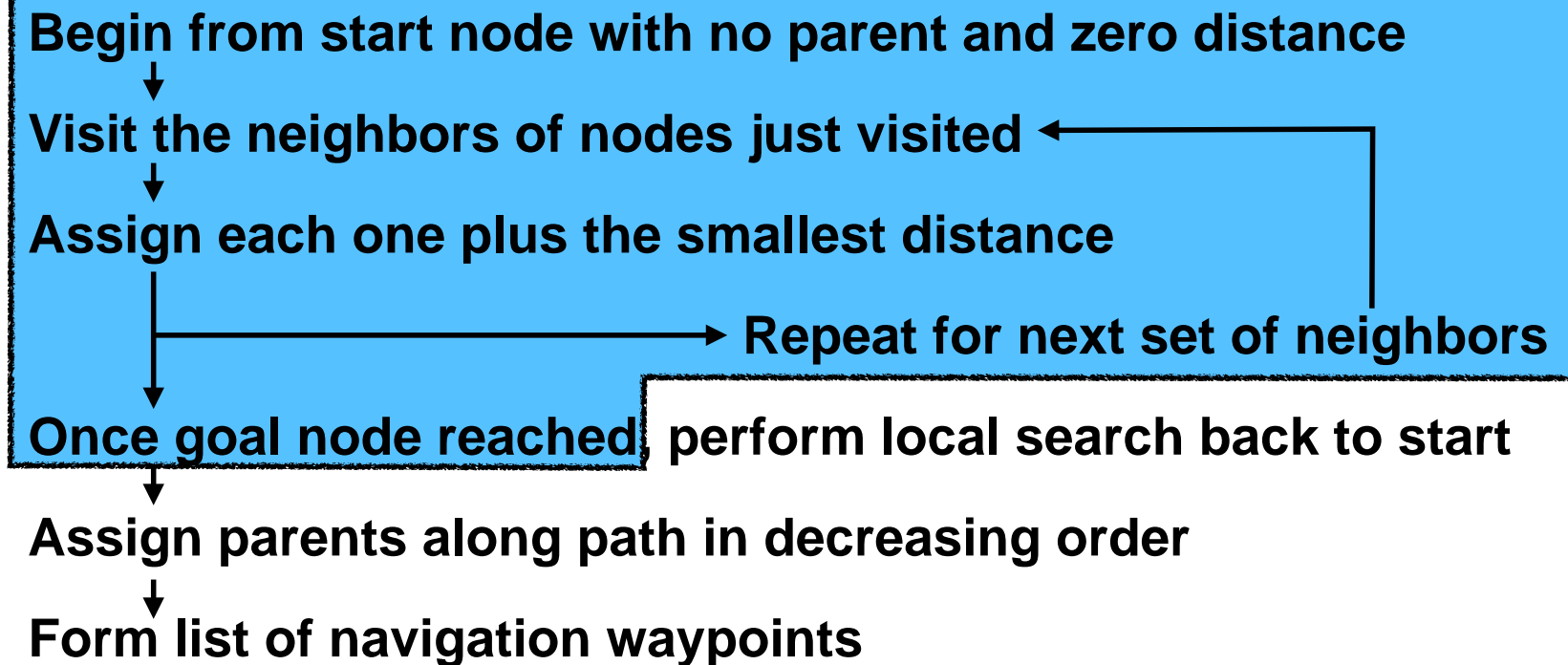
→ Repeat for next set of neighbors

↓
Once goal node reached, perform local search back to start

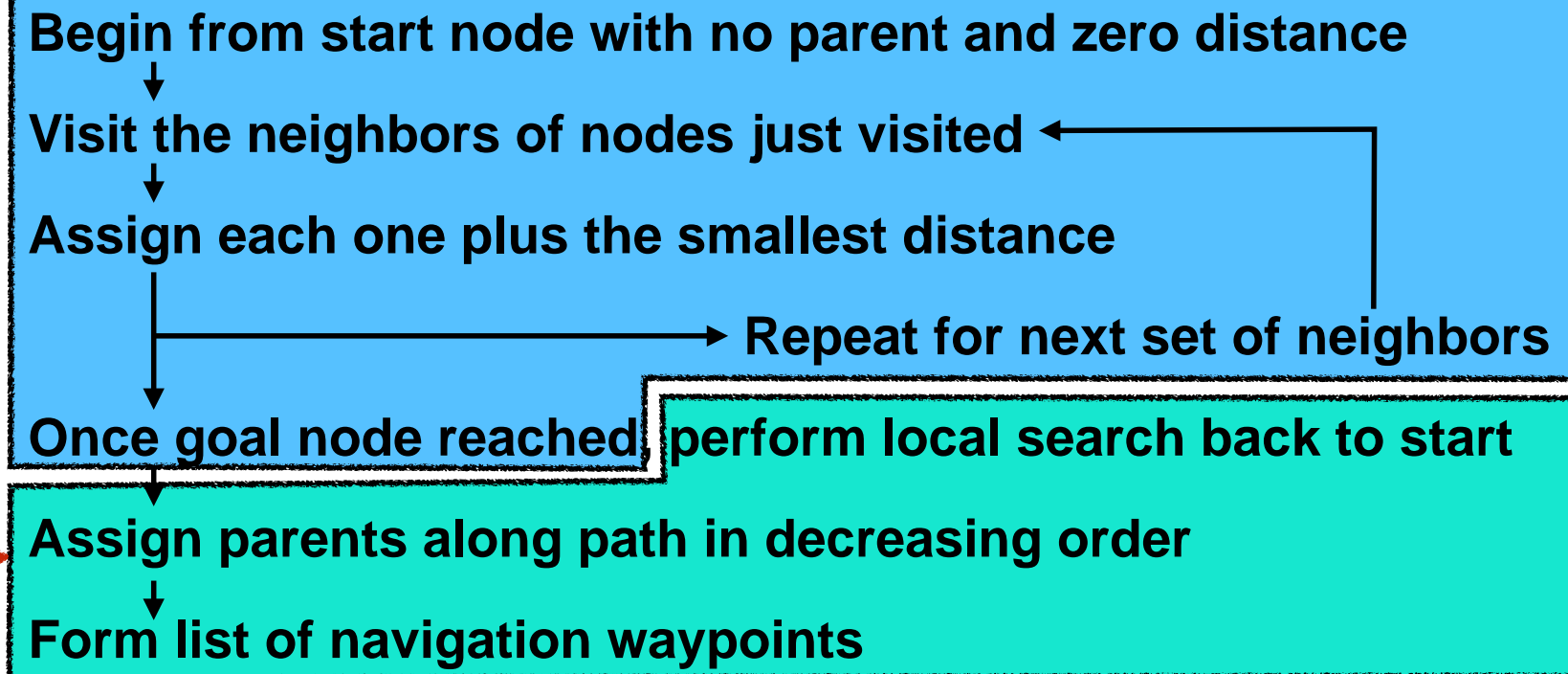
↓
Assign parents along path in decreasing order

↓
Form list of navigation waypoints

Global search to find routing

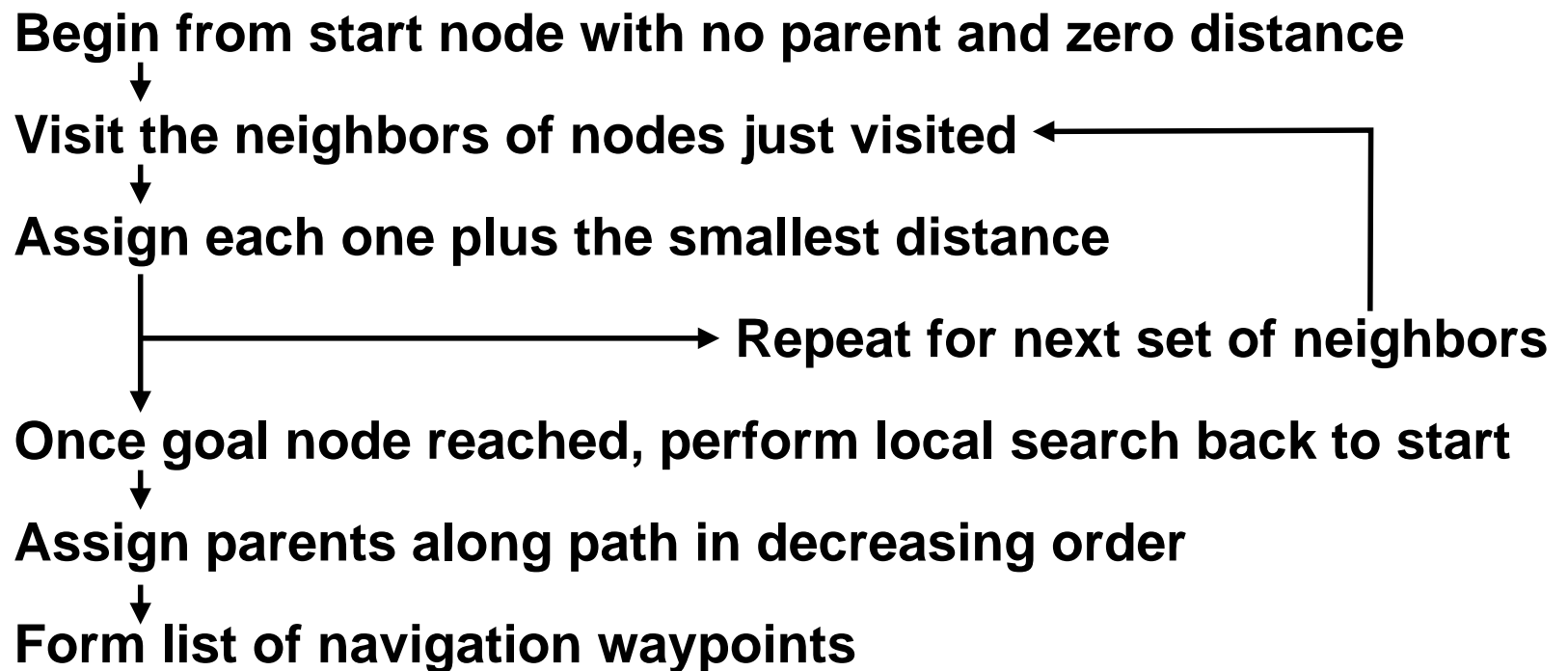


Global search to find routing



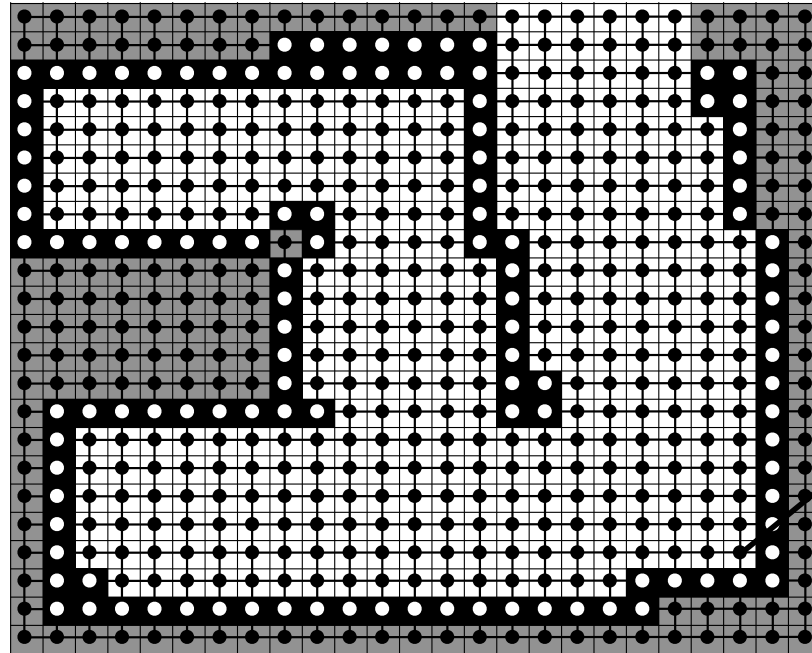
Is this local search necessary?

Brushfire is one of several algorithms that perform a "floodfill"



Breadth-first Search

For Breadth-first Search, each cell needs to keep track of whether it has been visited and queued



origin_x: 2.2
origin_y: 0.3
occupied: false
parent: ??
distance: ??
visited: false
queued: false

A graph node stores a struct of information about the cell

Breadth-first Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor $>$ Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

Breadth-first Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor $>$ Distance of current node + ...

Cost to move from current node to neighbor

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Initialize :

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***Iterate :* While visit list not empty and currently visited node is not the goal**

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

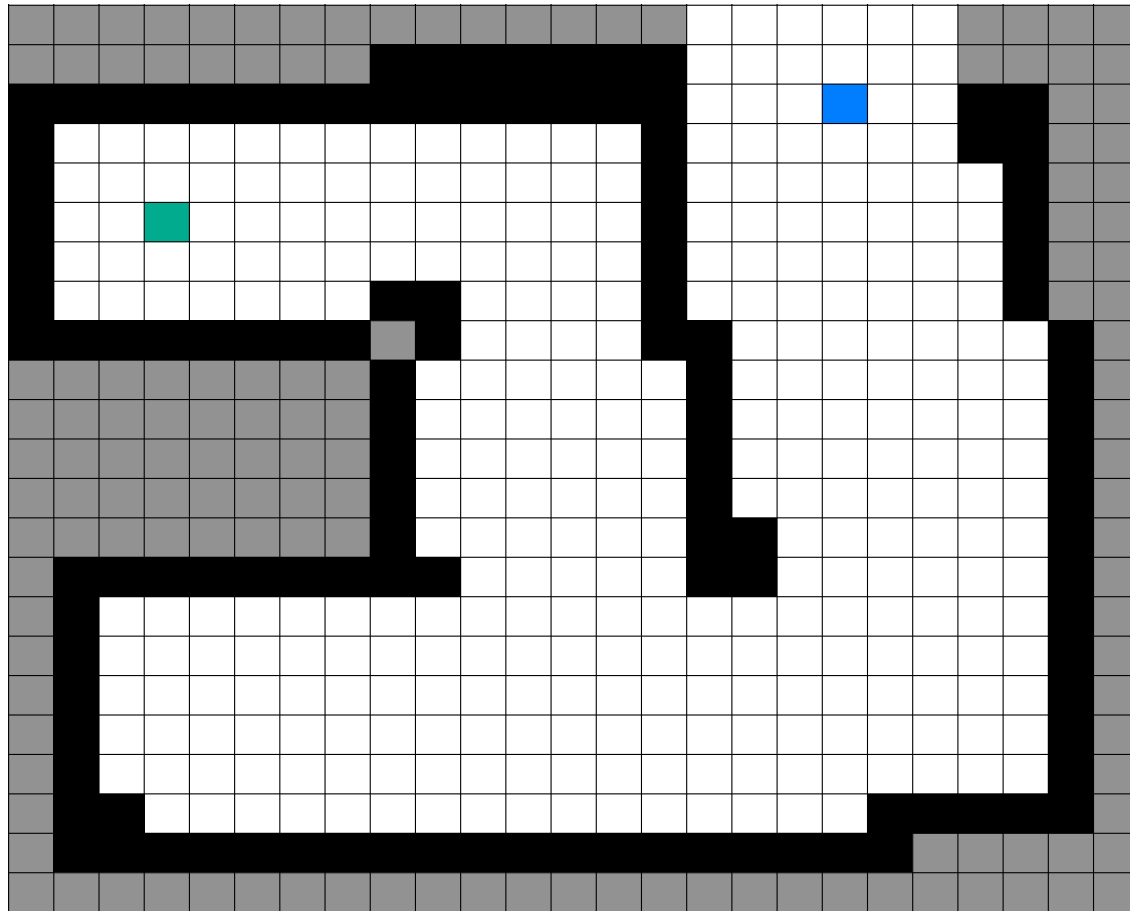
If Distance of neighbor $>$ Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

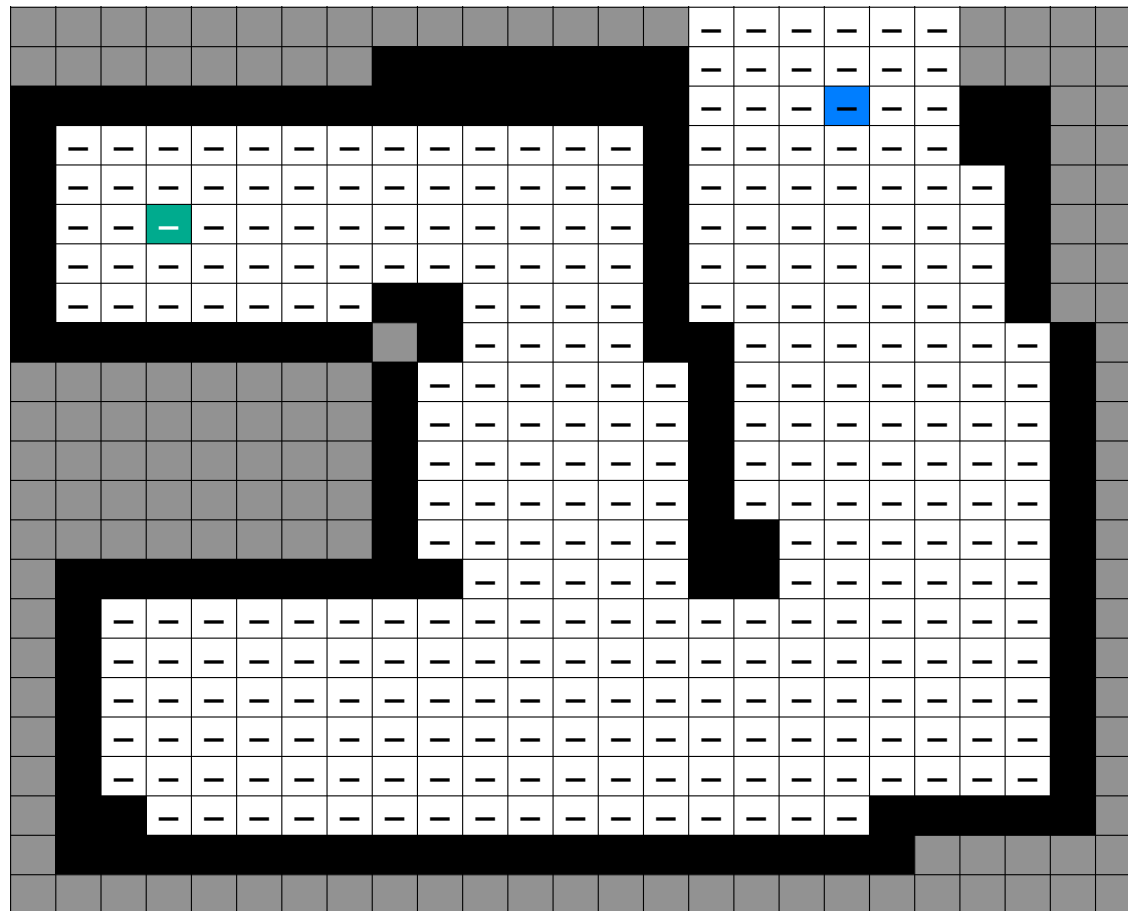
distance to be distance of current node + cost to move

All nodes to have no parent, max distance, and as unvisited



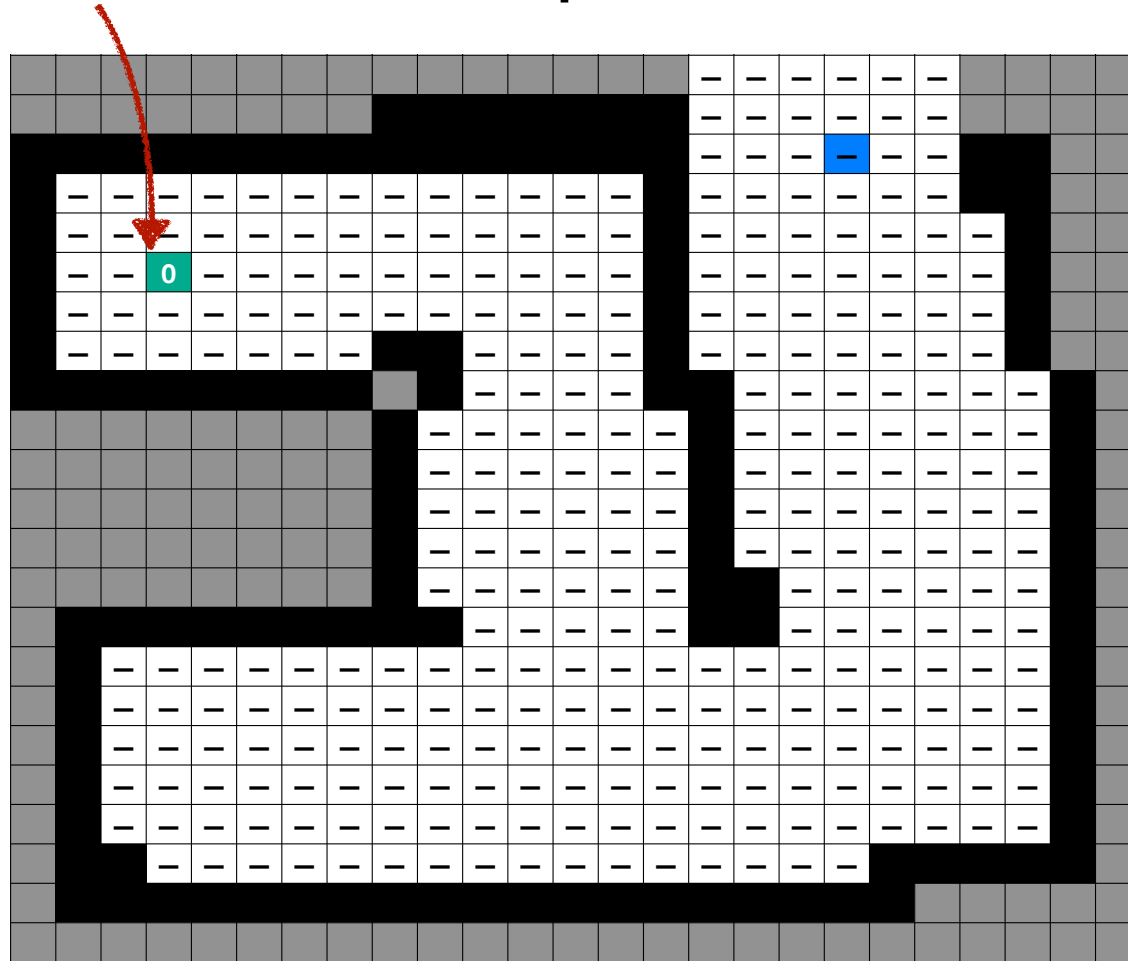
- is some very large number

All nodes to have no parent, max distance, and as unvisited

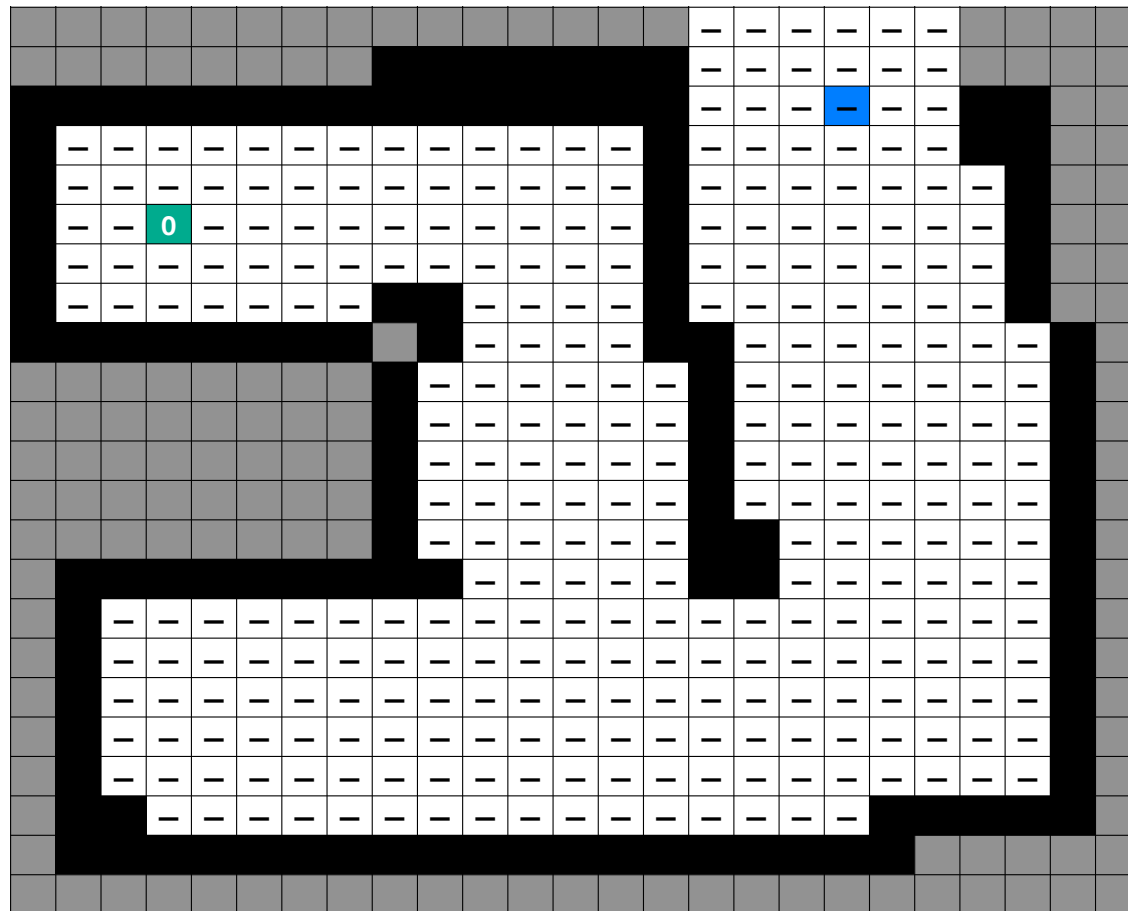


- is some very large number

Start node to have no parent and zero distance



Visit queue with start node as its only enqueued element



visit_queue



Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

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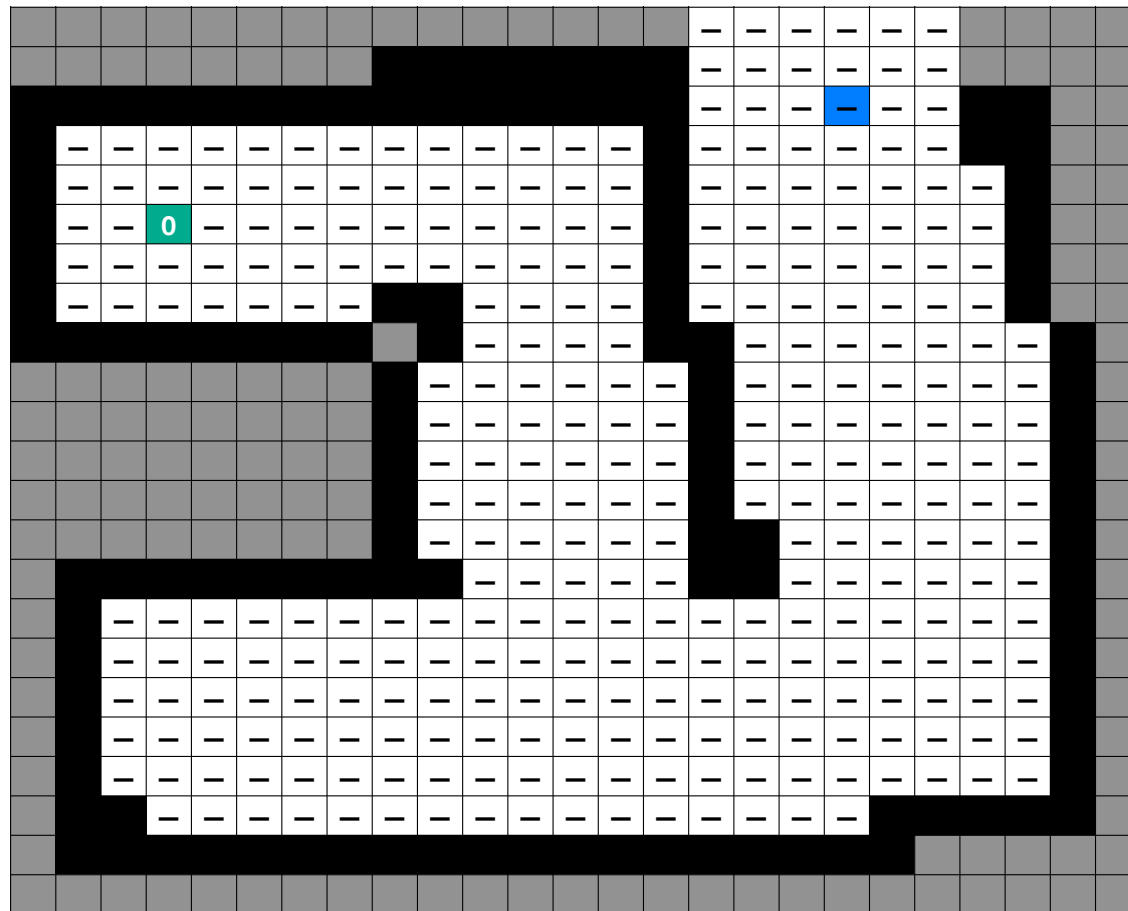
If Distance of neighbor $>$ Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

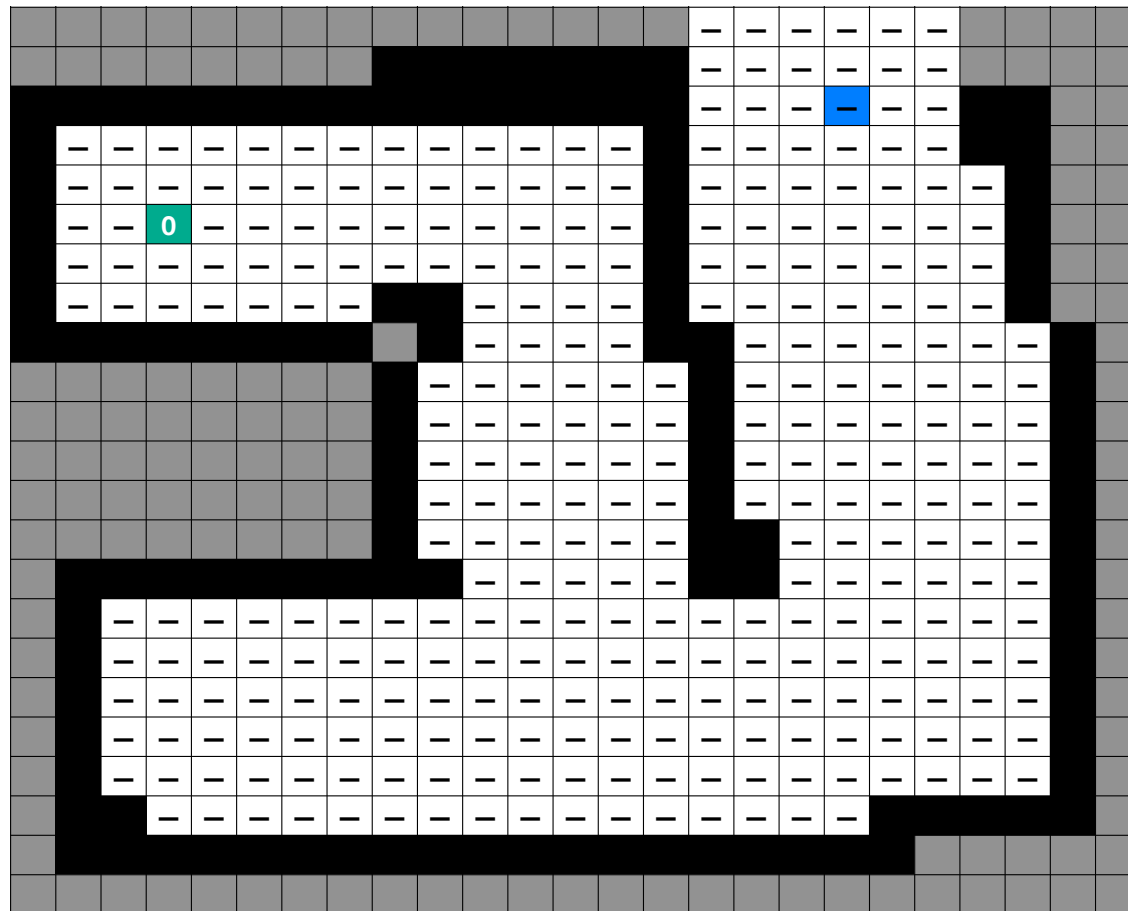
Dequeue new current node to visit and mark it as visited



visit_queue



Dequeue new current node to visit and mark it as visited



`visit_queue`



`current_node`

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

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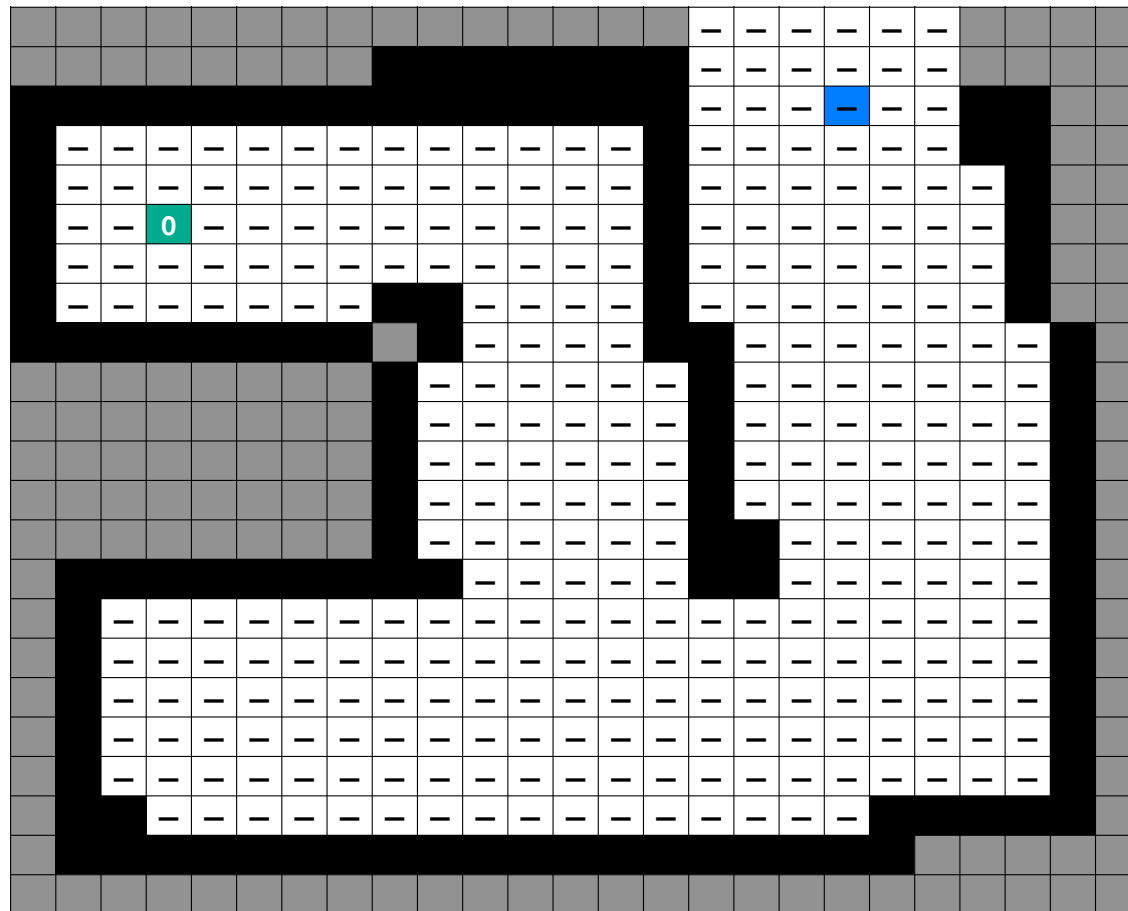
If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

Add to visit queue, if not previously visited or queued



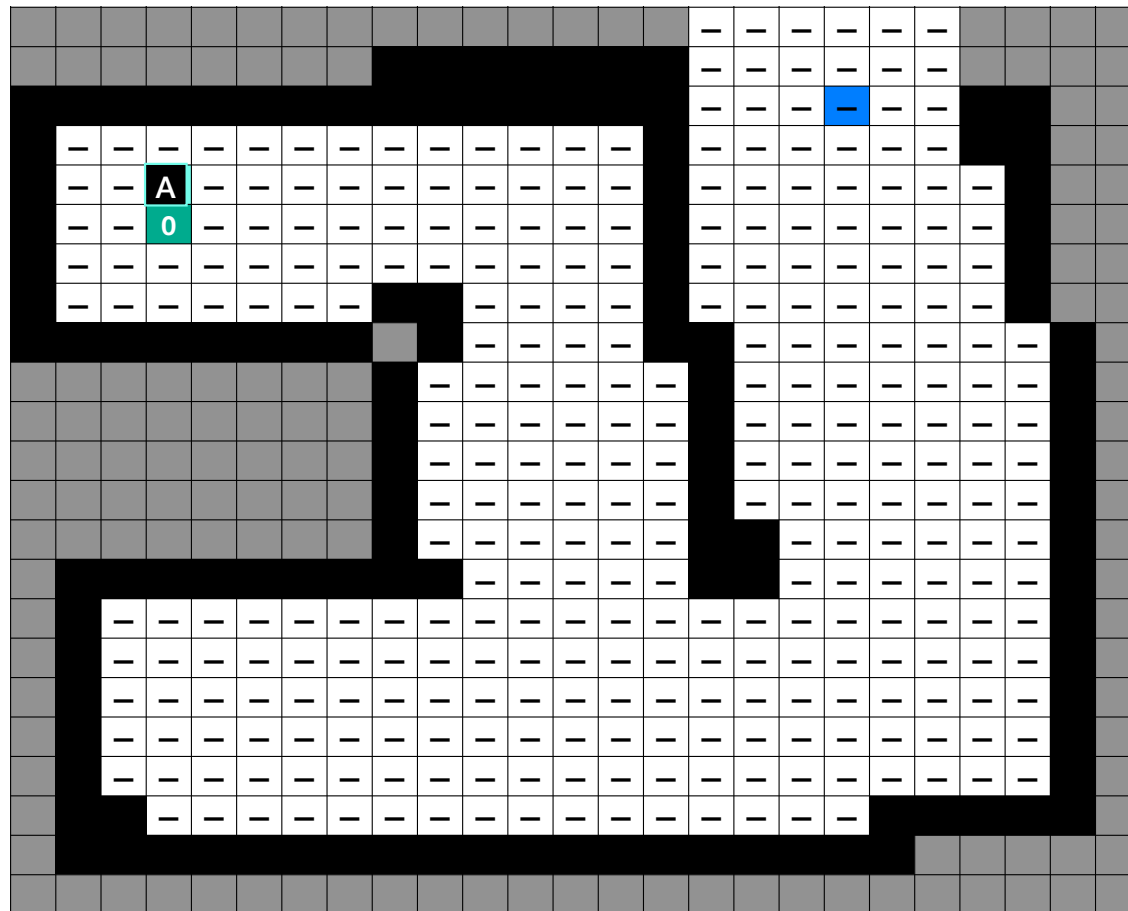
visit_queue



current_node

Add to visit queue, if not previously visited or queued

Queue first neighbor



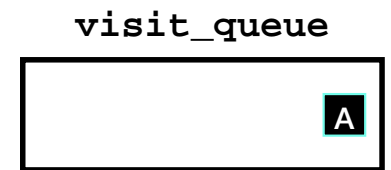
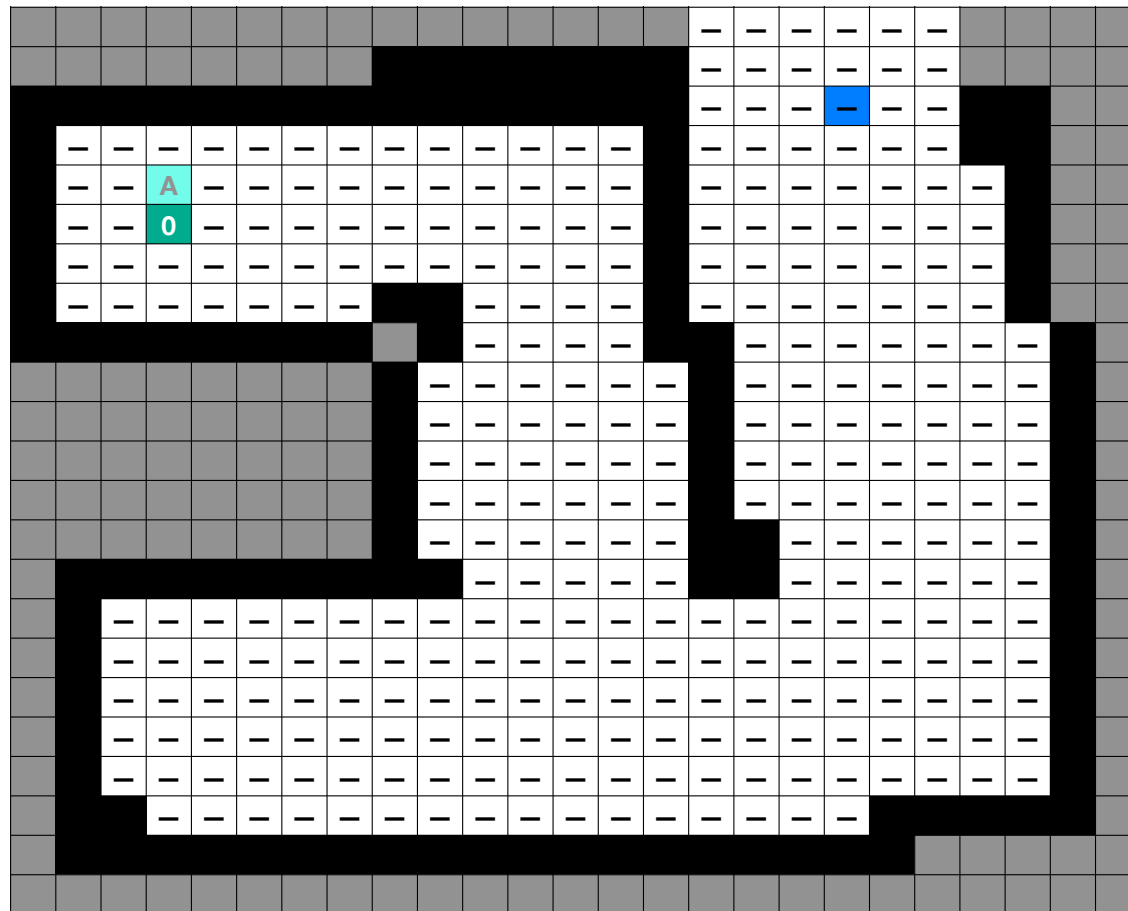
visit_queue



current_node

Add to visit queue, if not previously visited or queued

**Queue first
neighbor**



Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

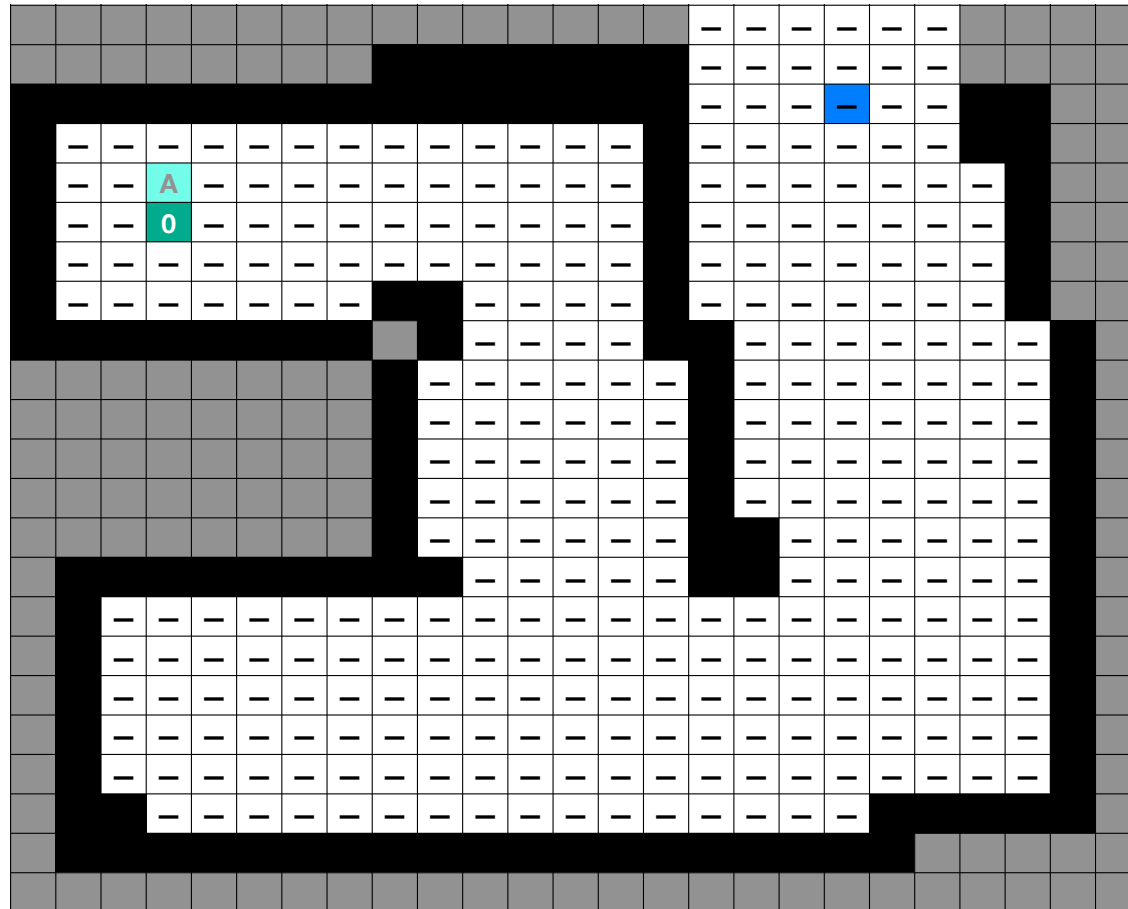
distance to be distance of current node + cost to move

If Distance of neighbor > Distance of current node + ...

-

0

Cost to move from current node to neighbor



1

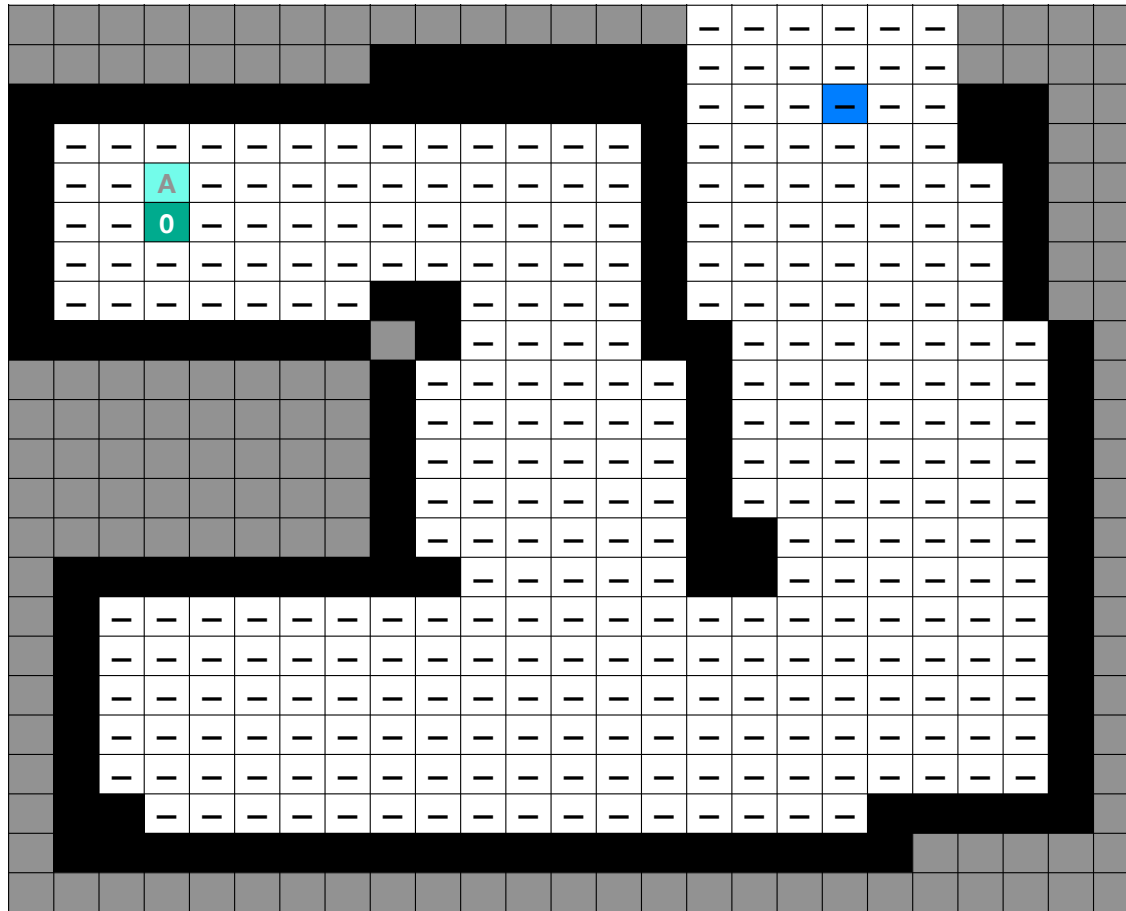
visit_queue



current_node

$$- > 0 + 1$$

true




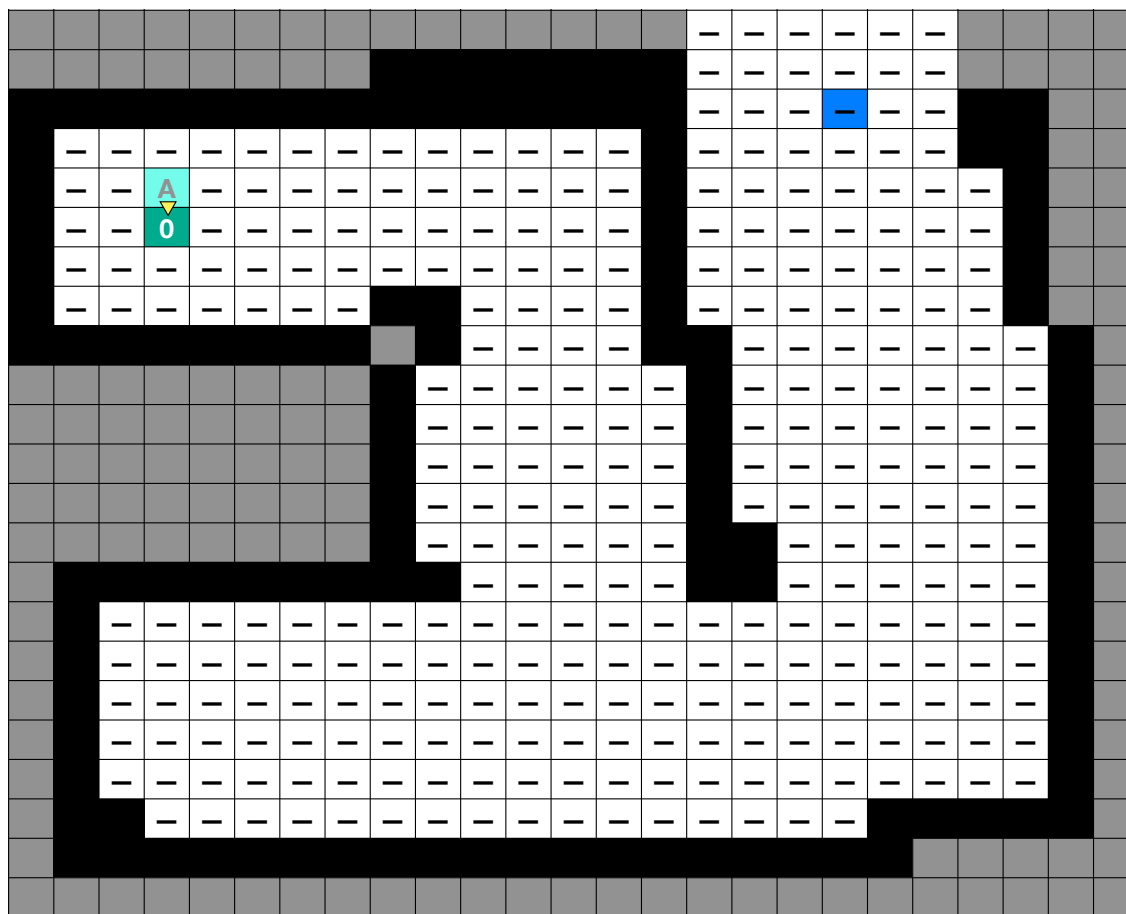
visit_queue




current_node

Then Update neighbor's parent to be current node and ...


true

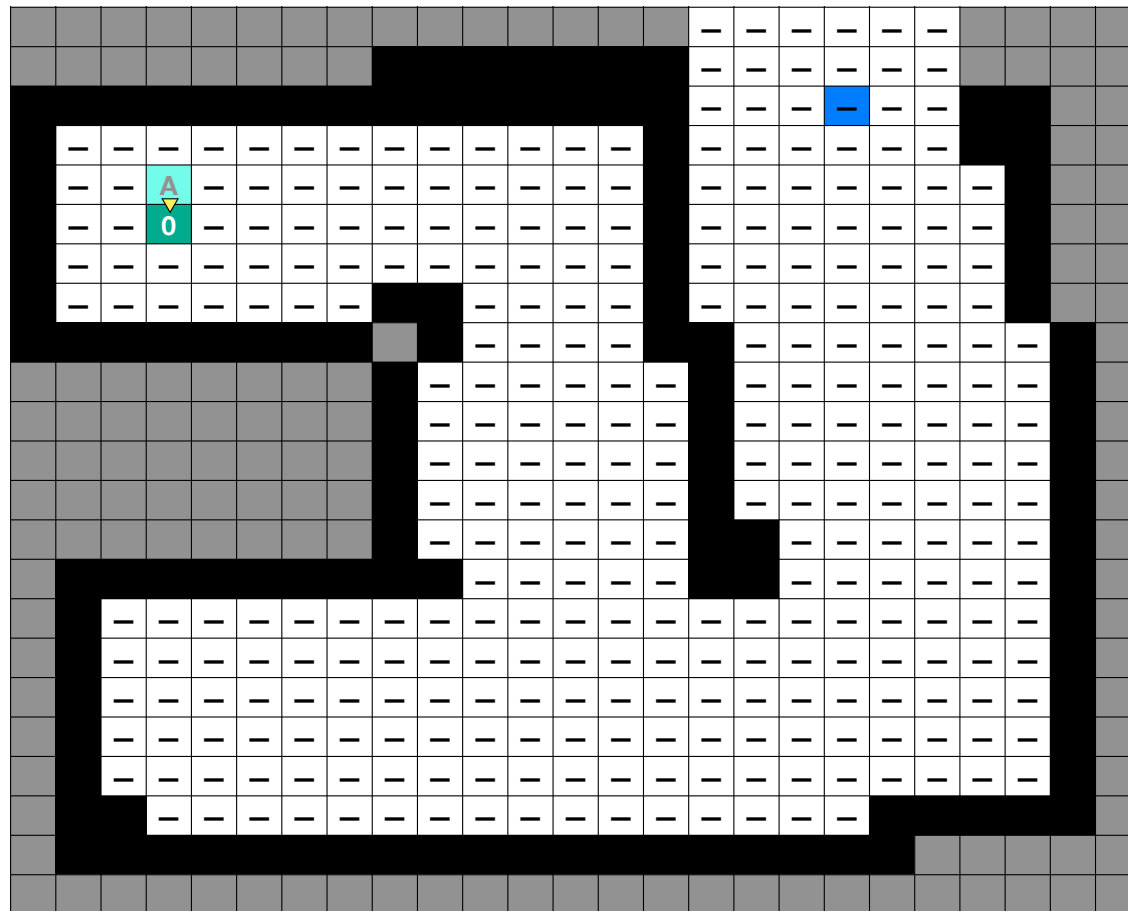


visit_queue



current_node

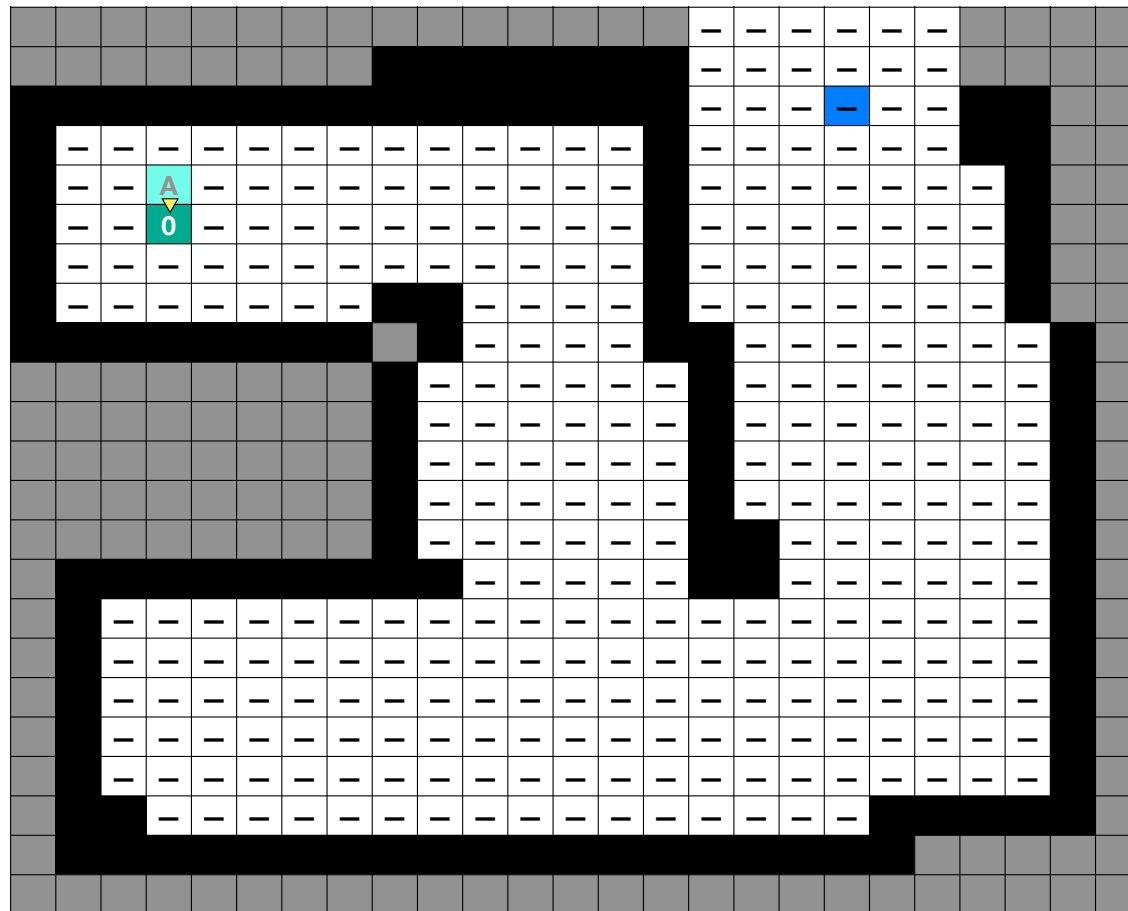
update neighbor's distance to be distance of current node + cost to move

$- > 0 + 1$
true



update neighbor's distance to be distance of current node + cost to move

$$0 + 1$$



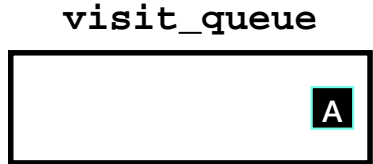
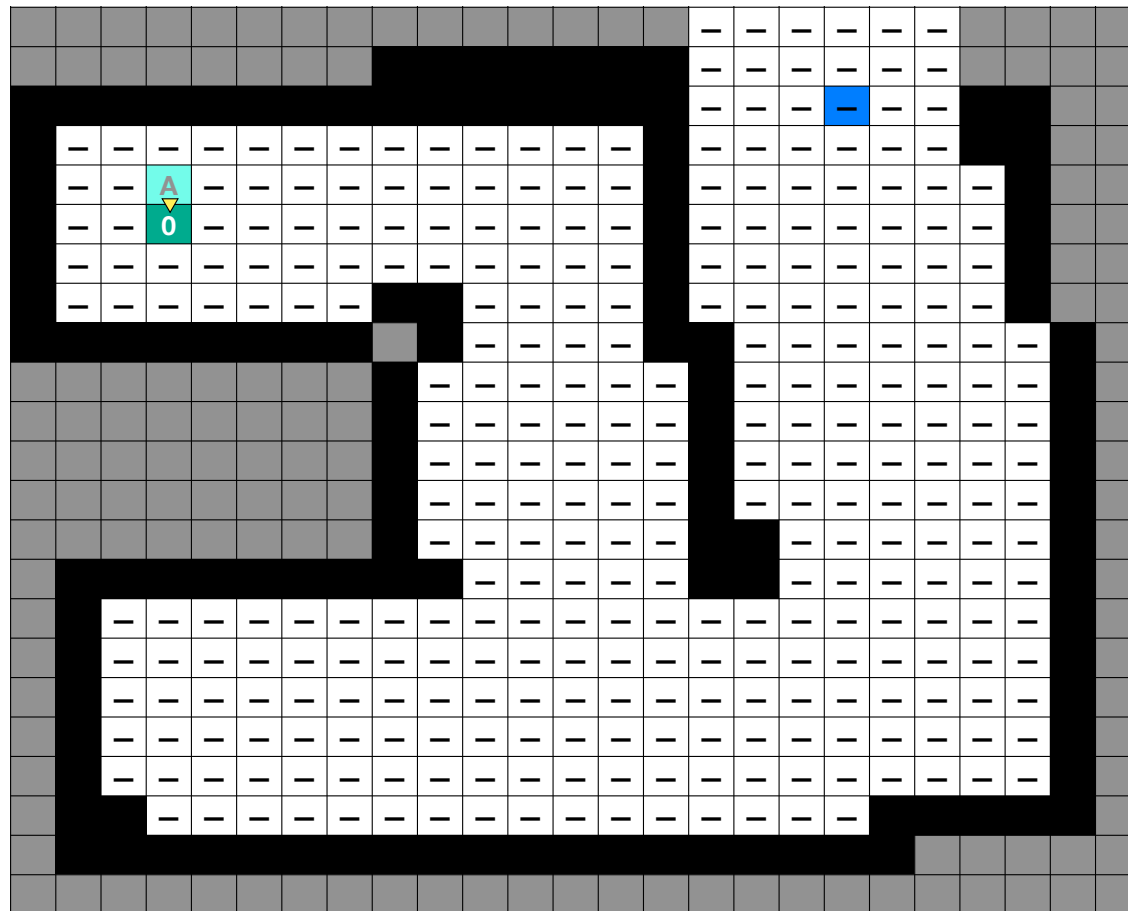
visit_queue



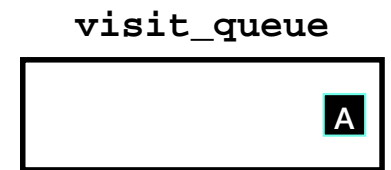
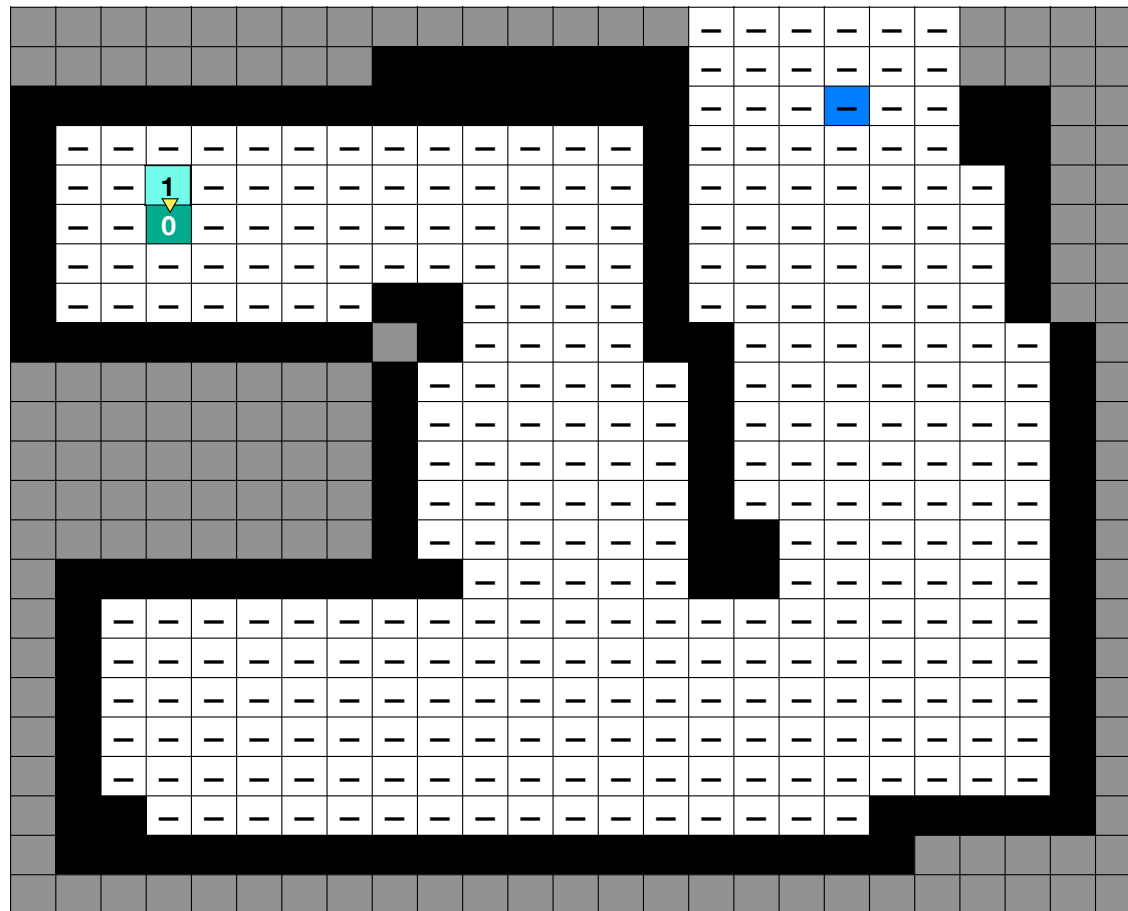
current_node

update neighbor's distance to be distance of current node + cost to move

1



update neighbor's distance to be distance of current node + cost to move



Initialize :

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Start node to have no parent and zero distance

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Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

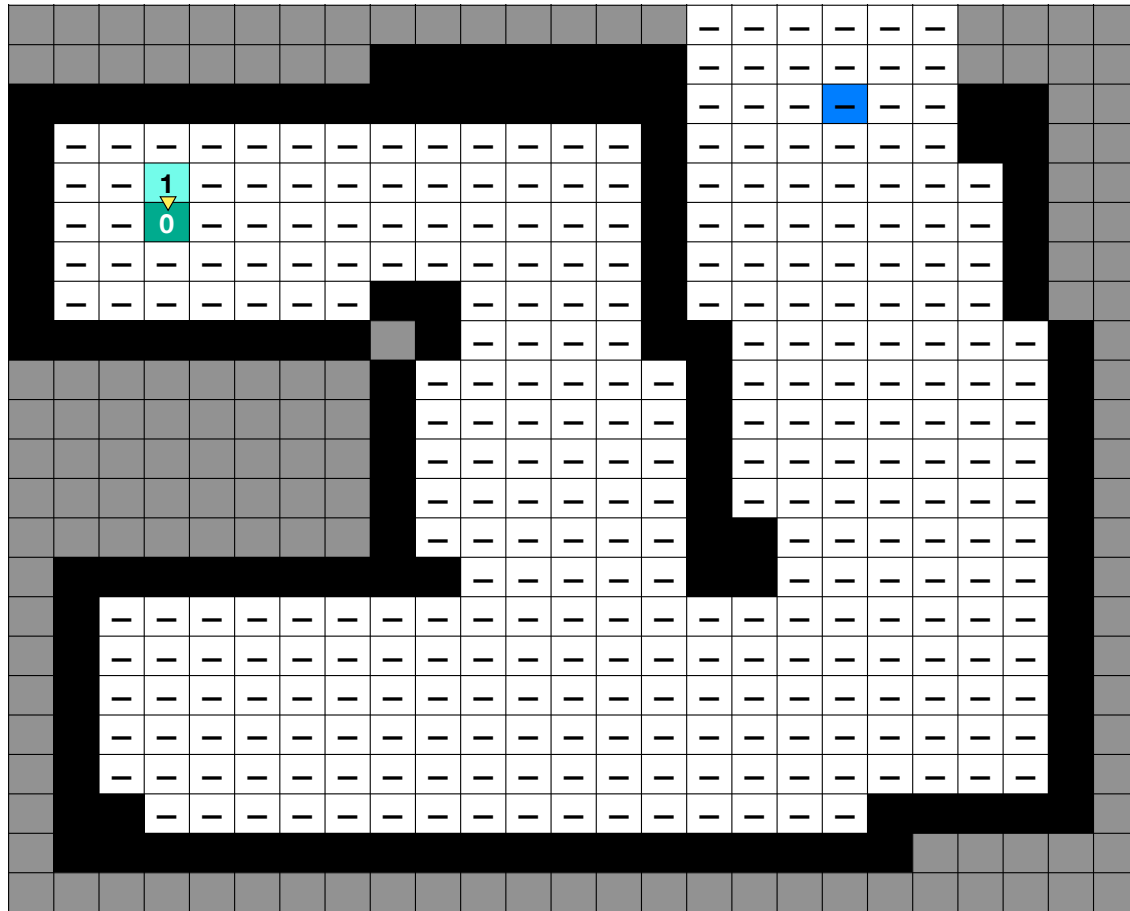
Add to visit queue, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

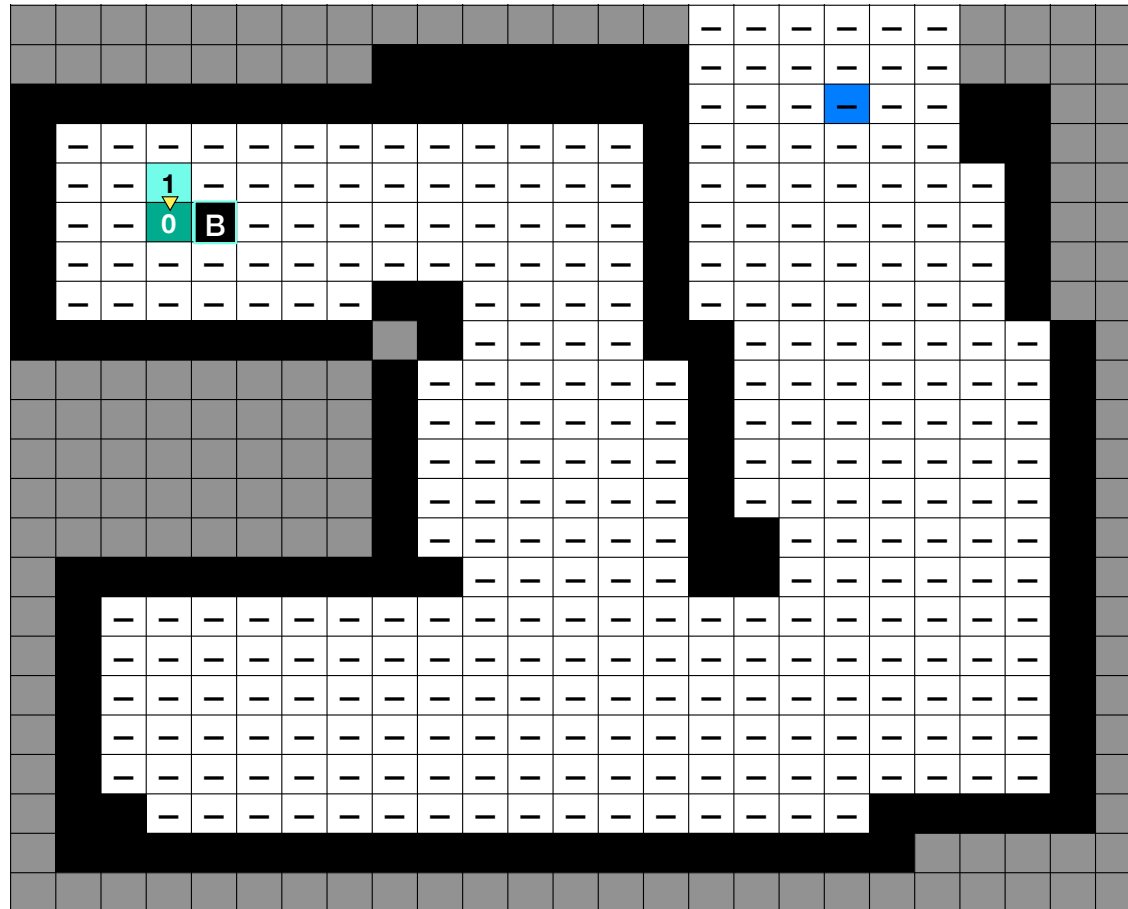


visit_queue



current_node

**Queue second
neighbor**



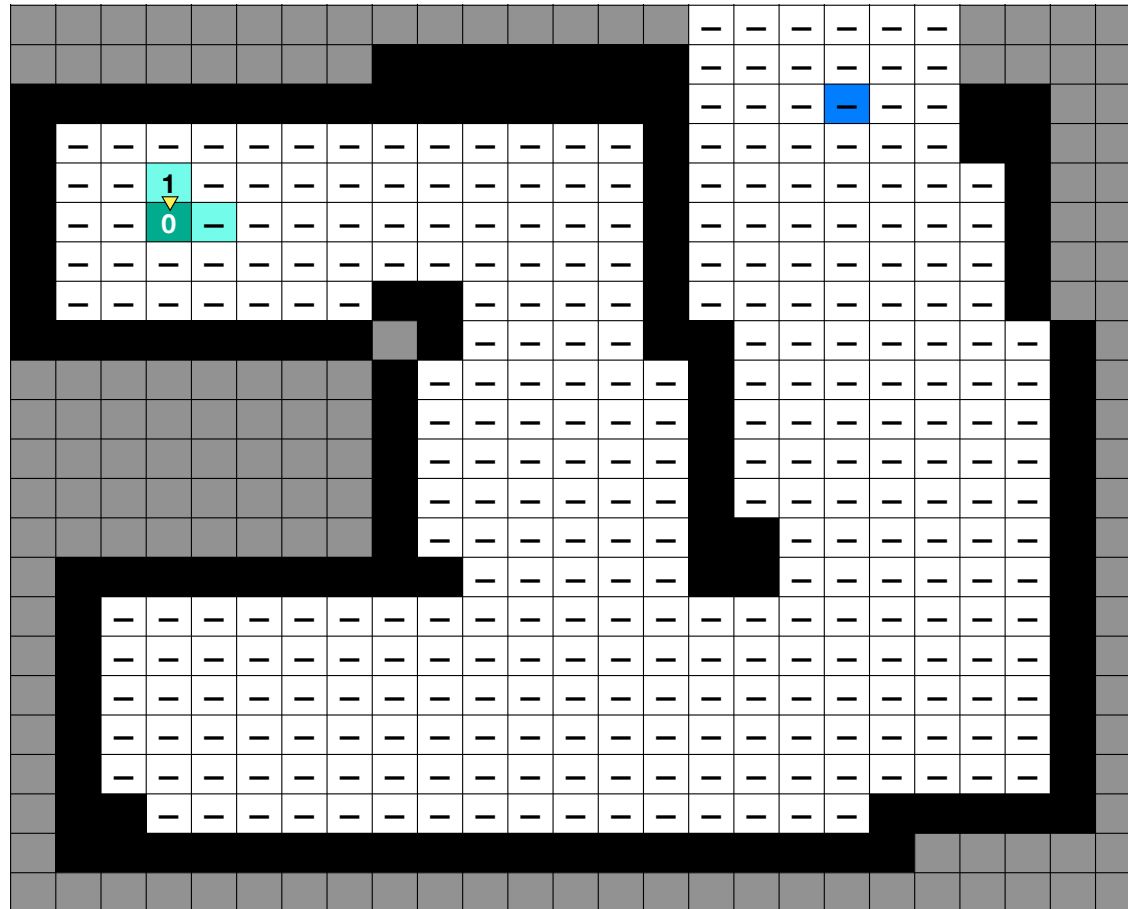
visit_queue



current_node



**Queue second
neighbor**

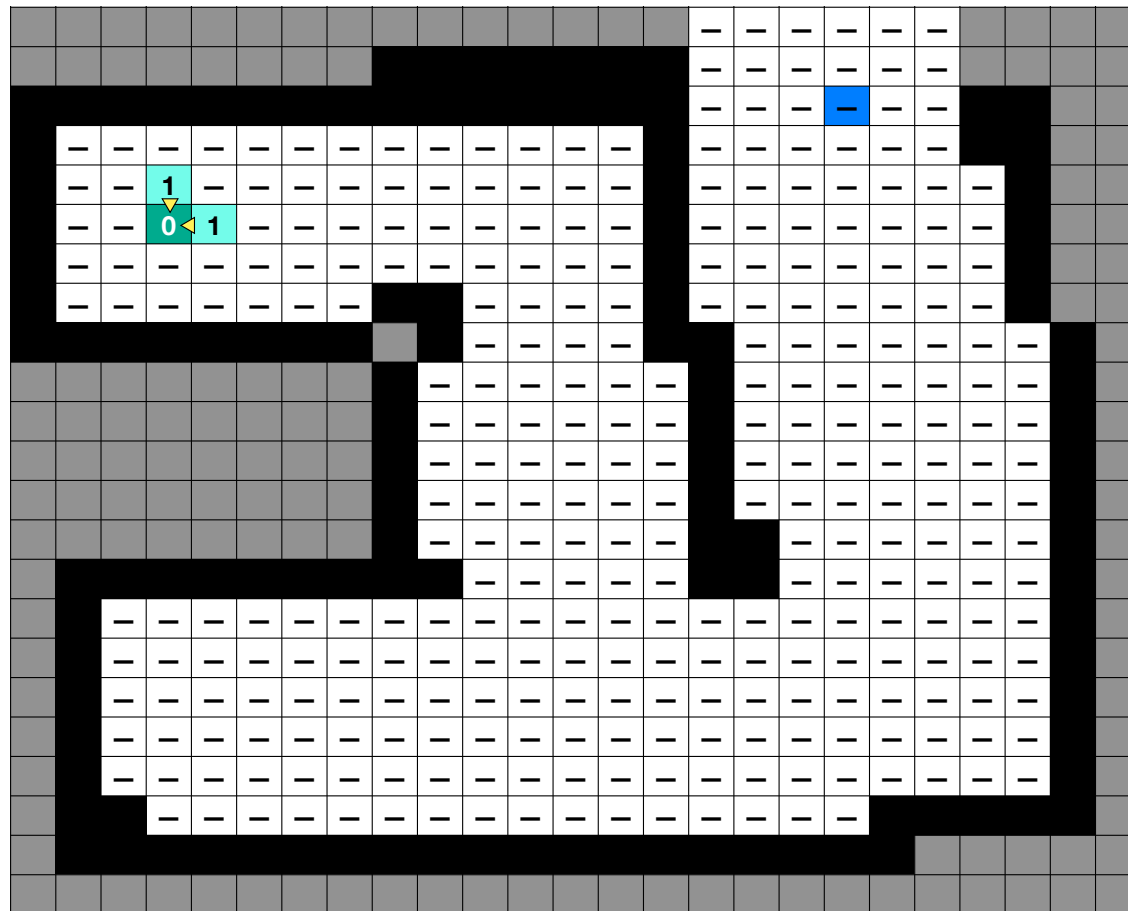


visit_queue



current_node

**Assign
distance and
parent**

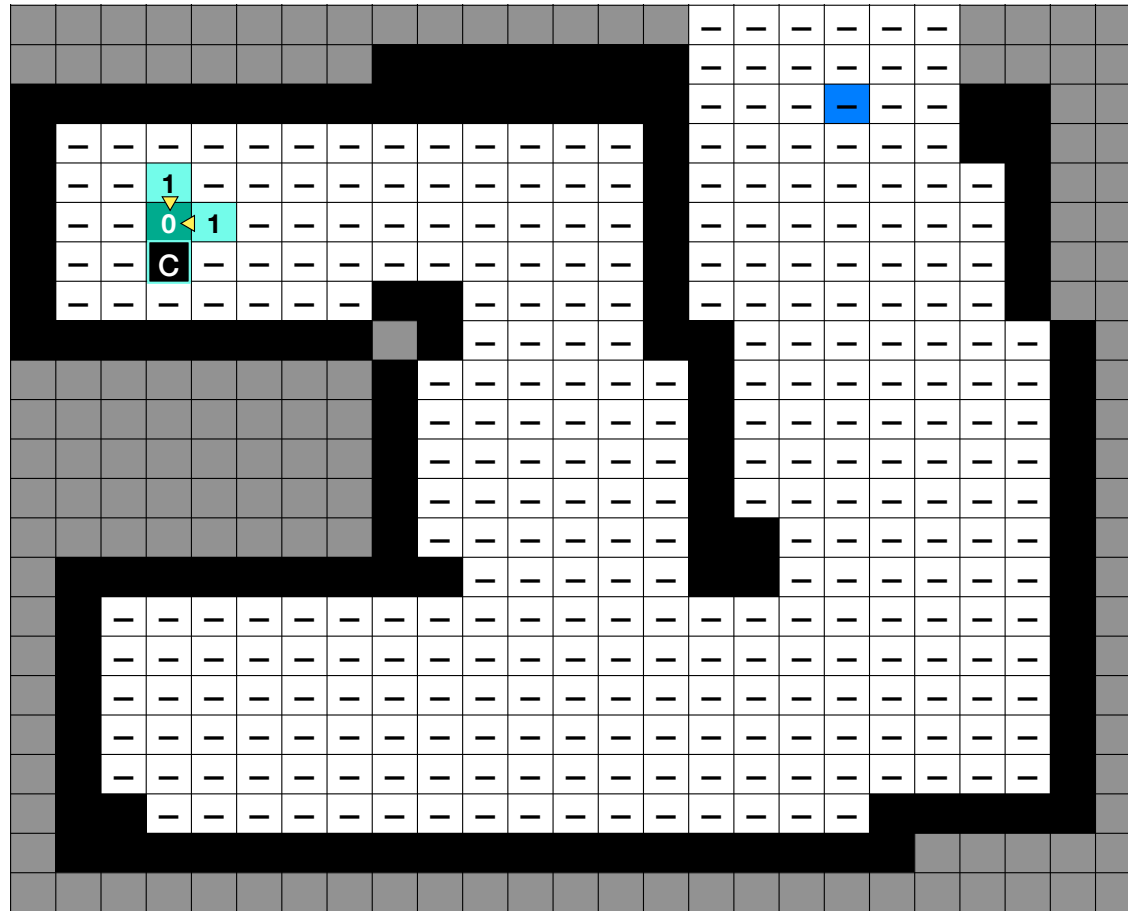


visit_queue

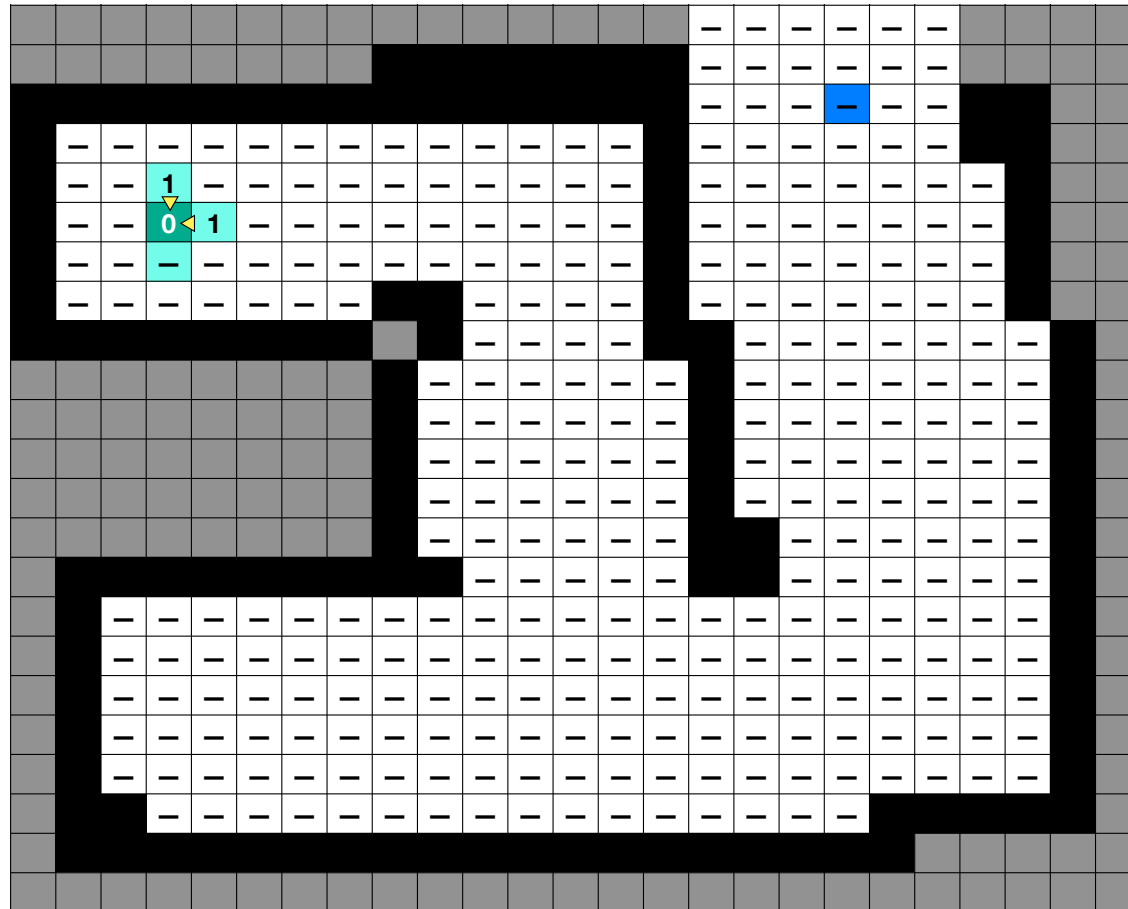


current_node

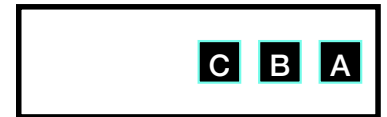
**Queue third
neighbor**



**Queue third
neighbor**

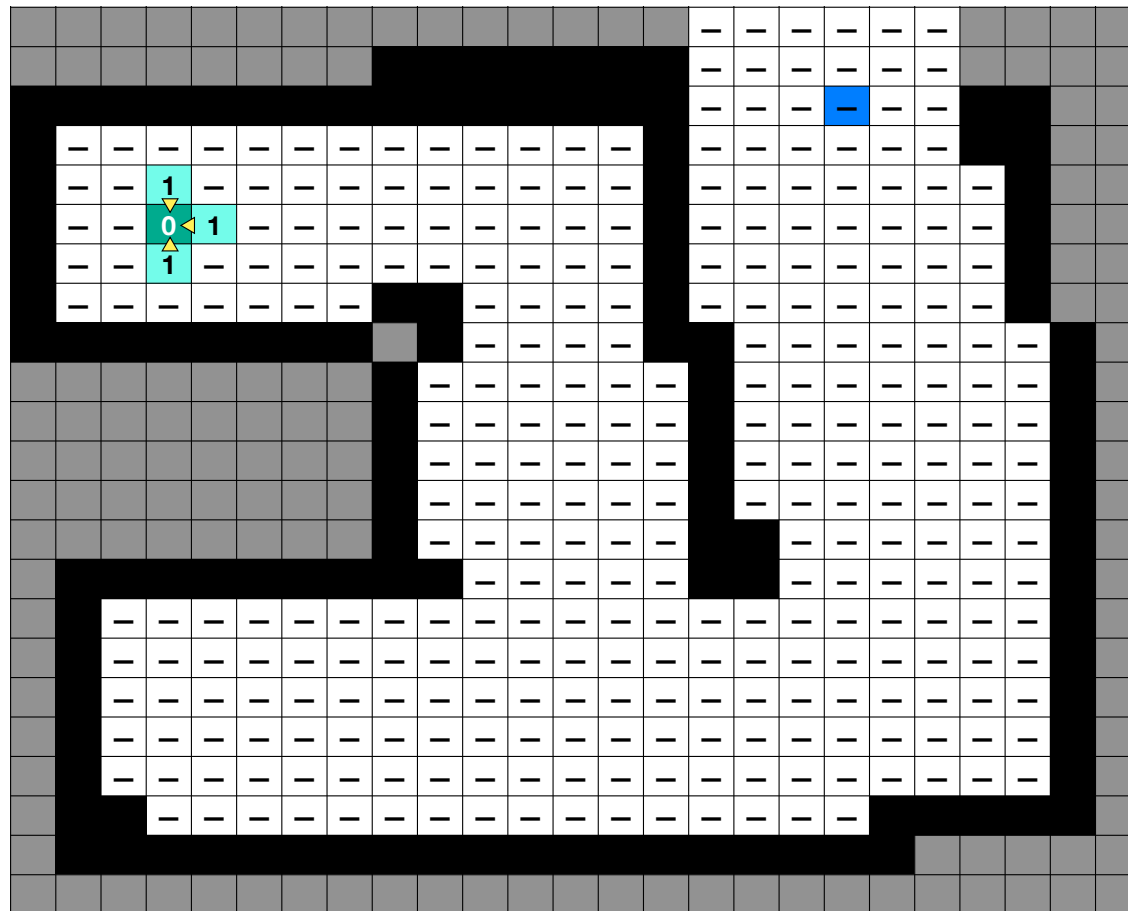


visit_queue

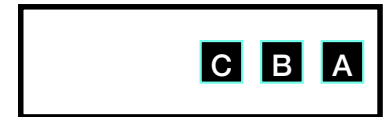


current_node

**Assign
distance and
parent**

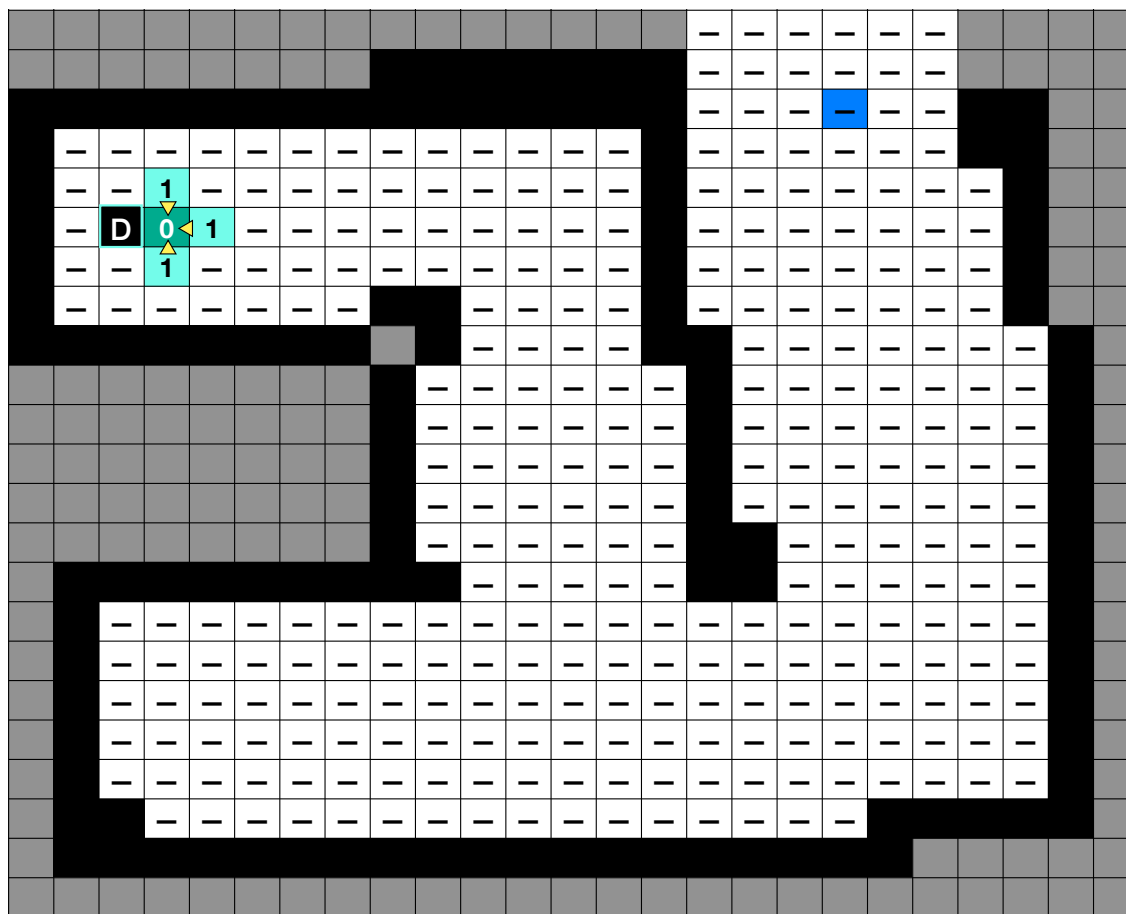


visit_queue

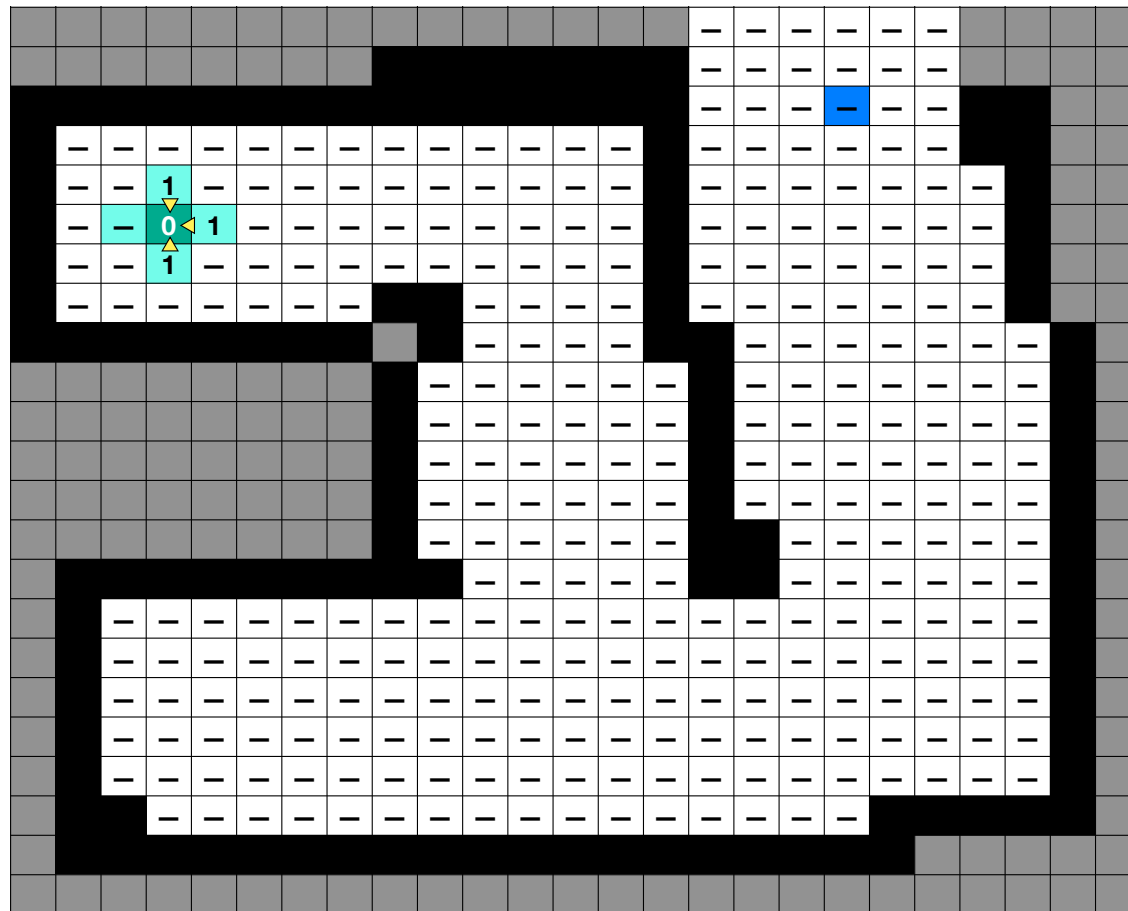


current_node

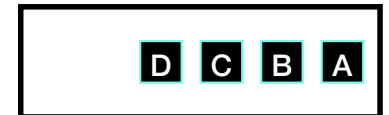
Queue last neighbor



**Queue last
neighbor**

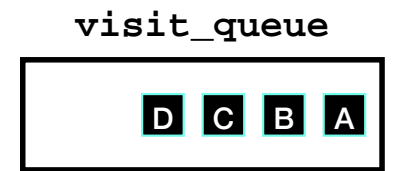
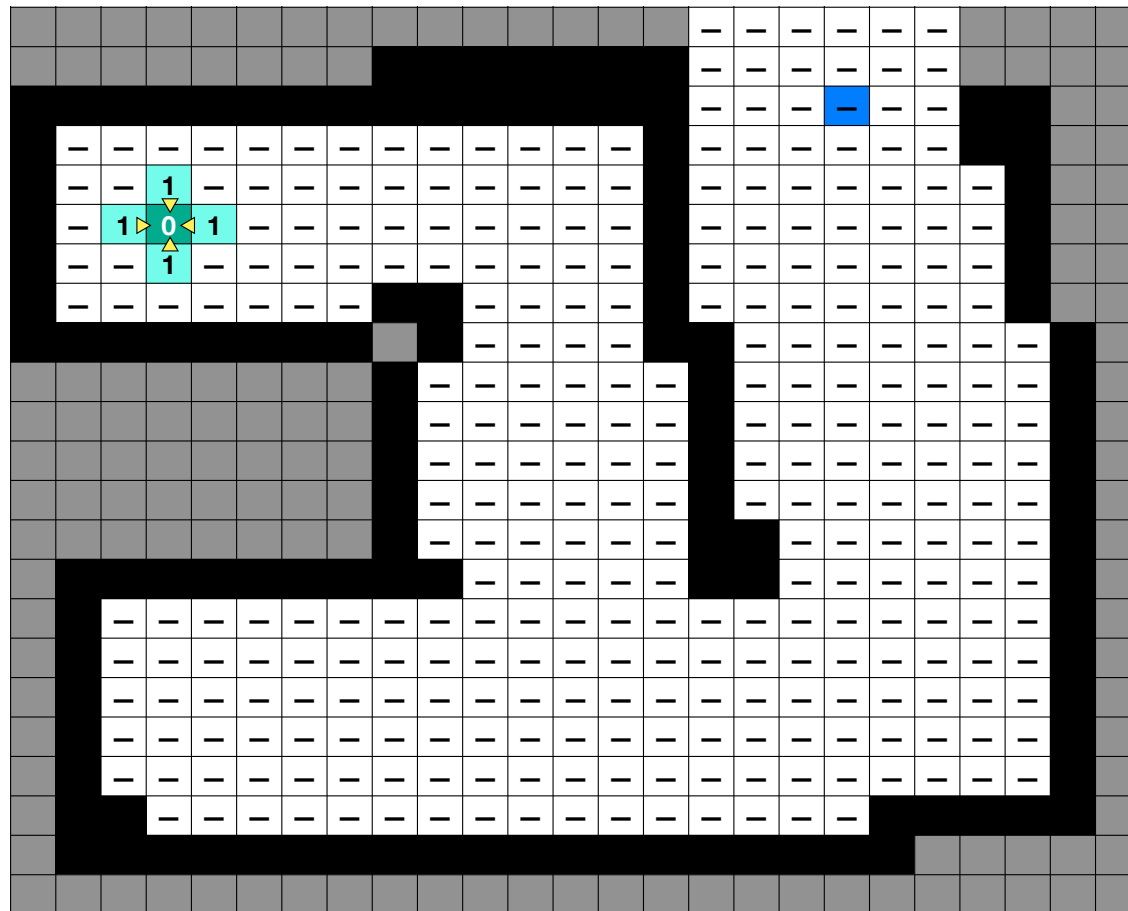


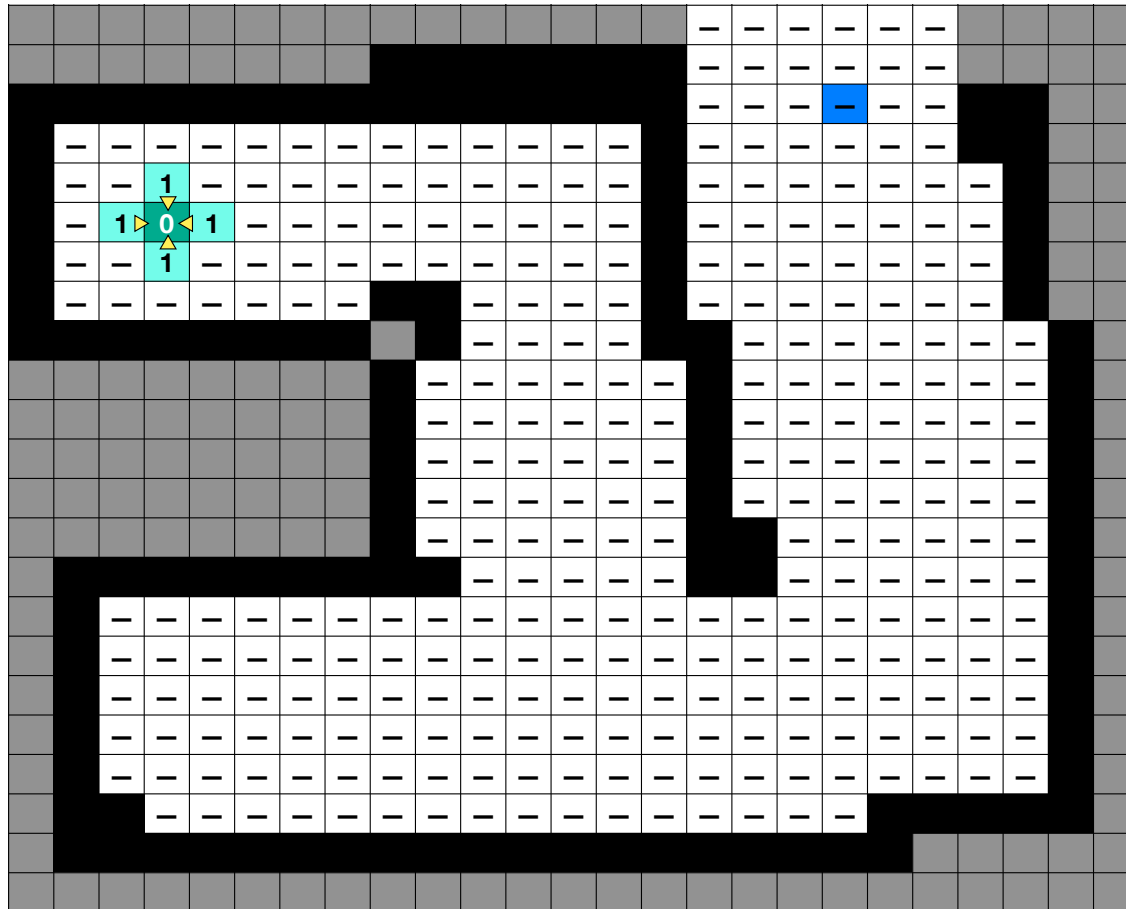
visit_queue



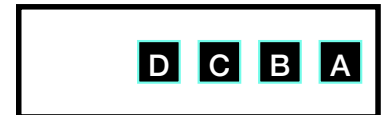
current_node

**Assign
distance and
parent**



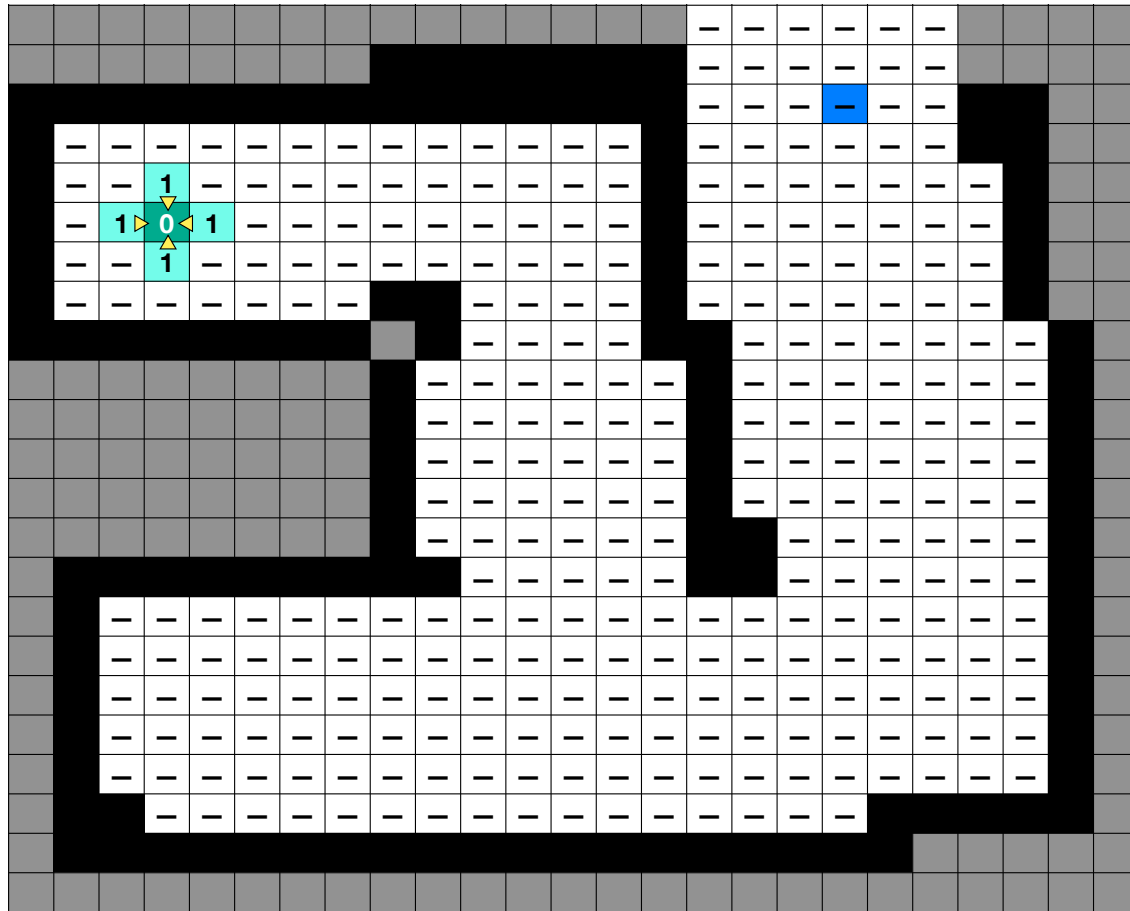


visit_queue

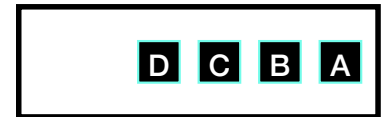


current_node

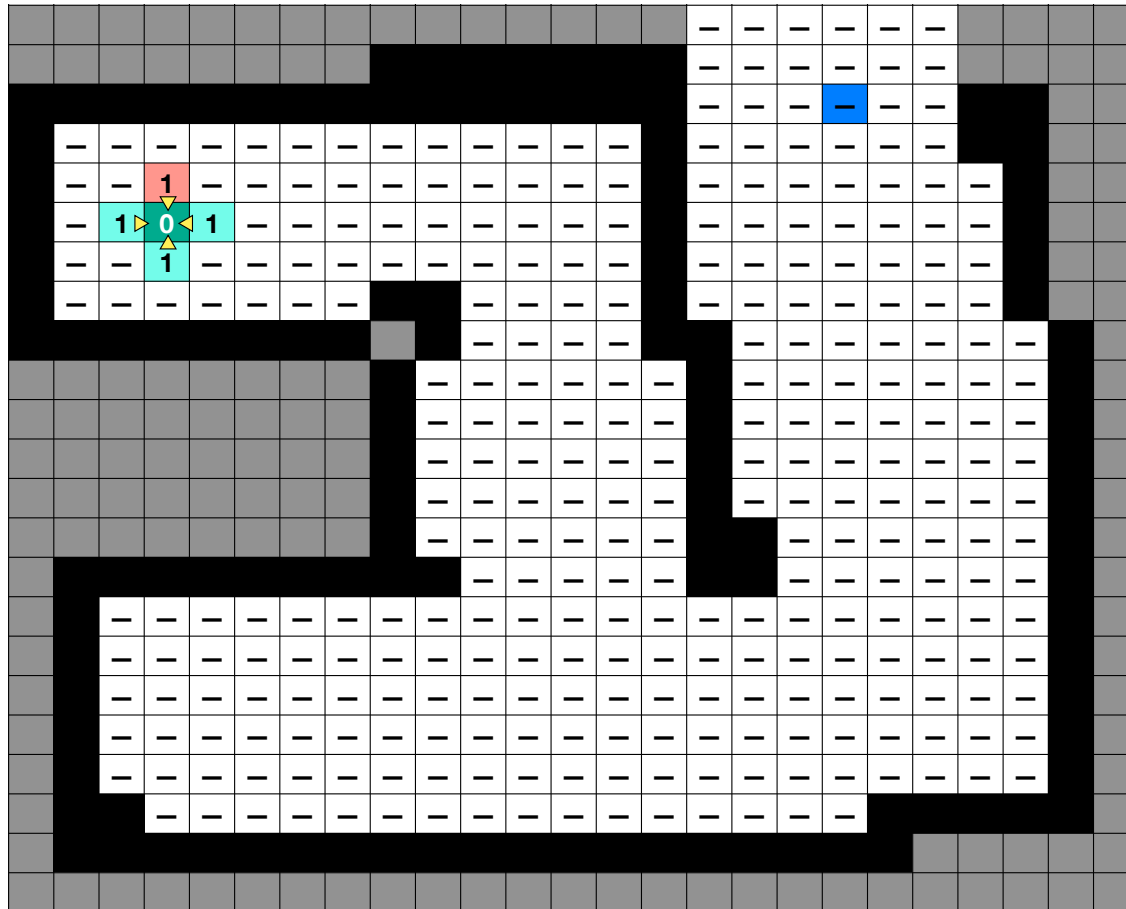
**Current node
fully processed**



visit_queue



current_node



visit_queue

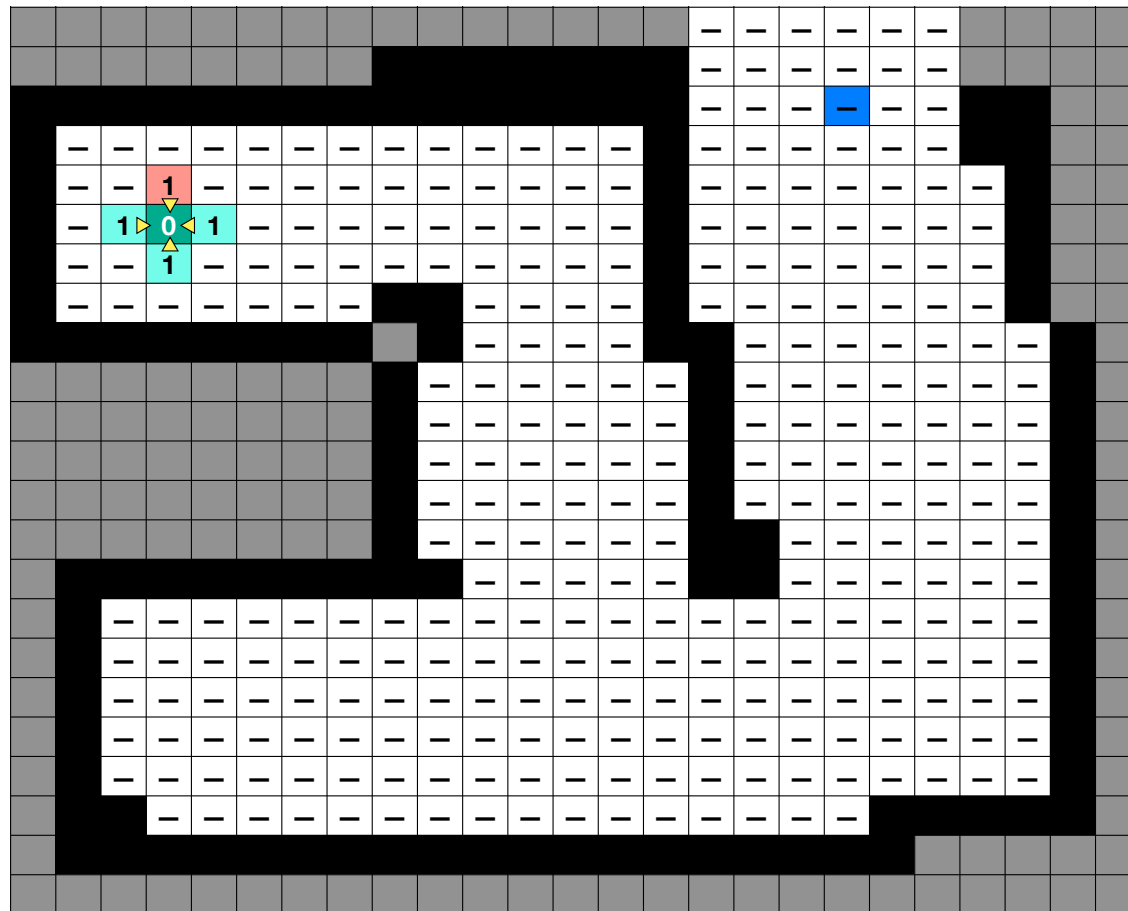


A

current_node

***Dequeue from
visit queue***

**Process
current node**



visit_queue



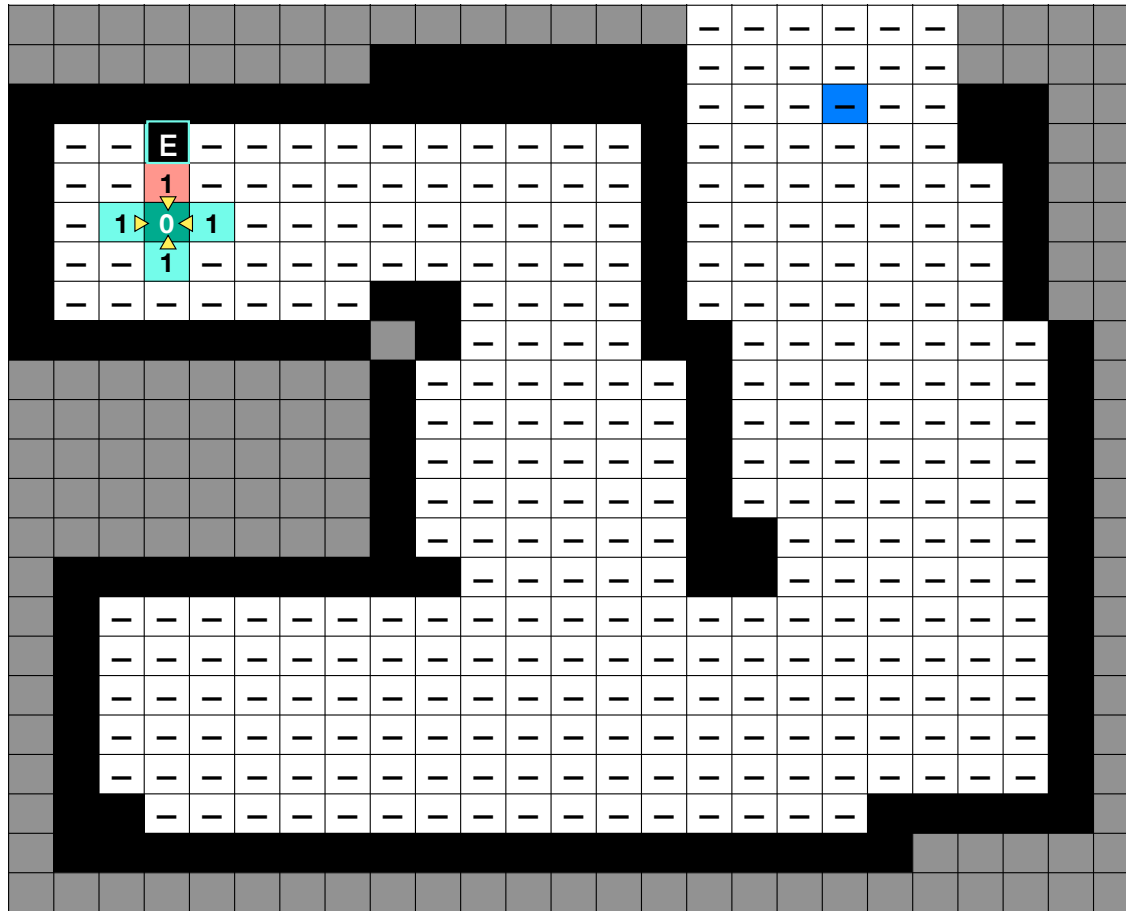
A

current_node

**Dequeue from
visit queue**

**Process
current node**

**Queue first
neighbor**



visit_queue

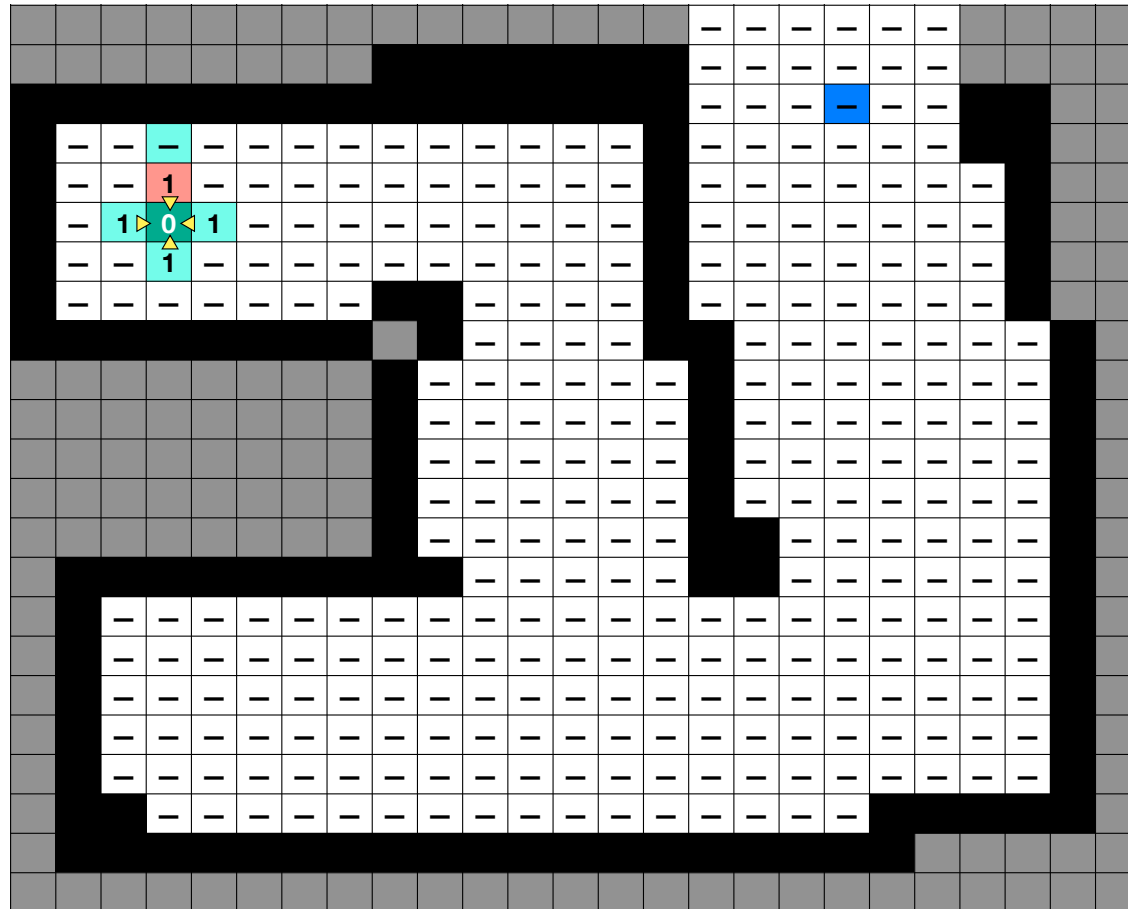


A

current_node

**Process
current node**

**Queue first
neighbor**



visit_queue



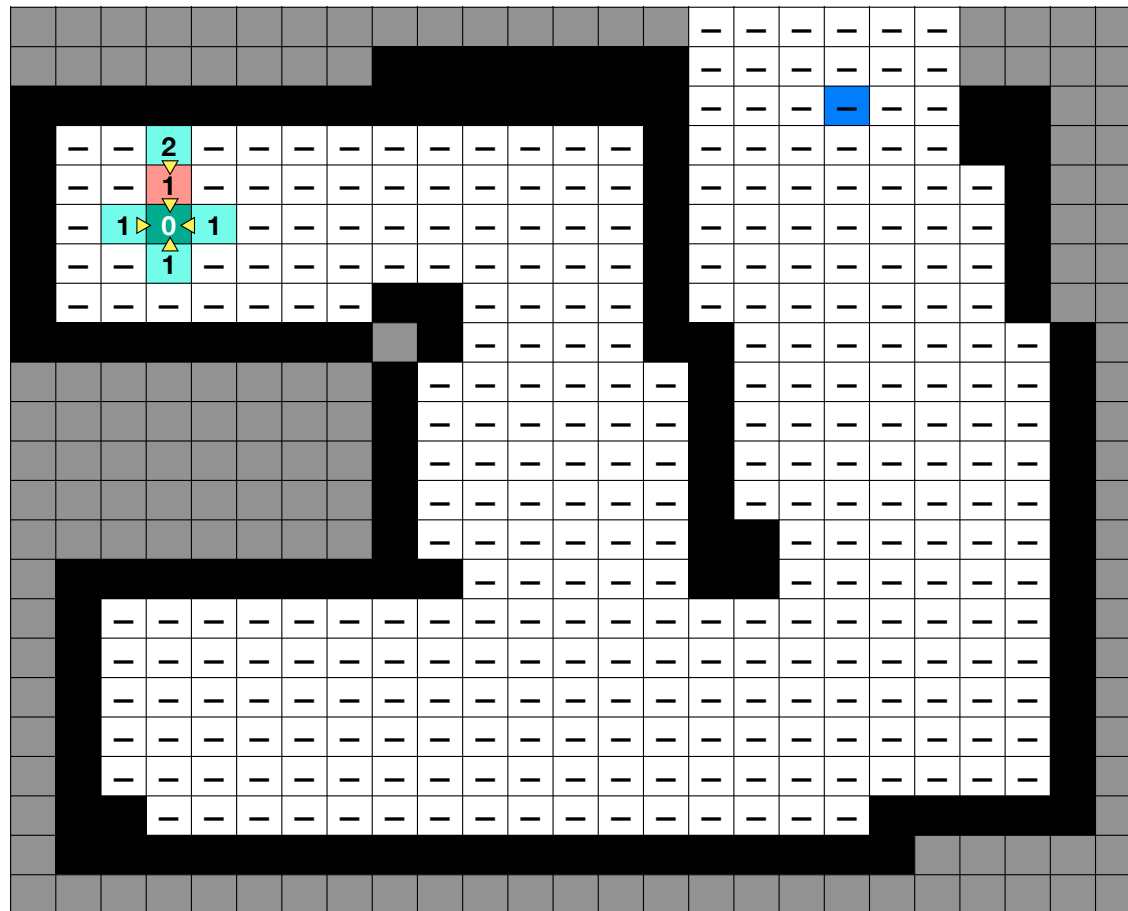
A

current_node

**Process
current node**

**Queue first
neighbor**

**Assign
distance and
parent**



visit_queue

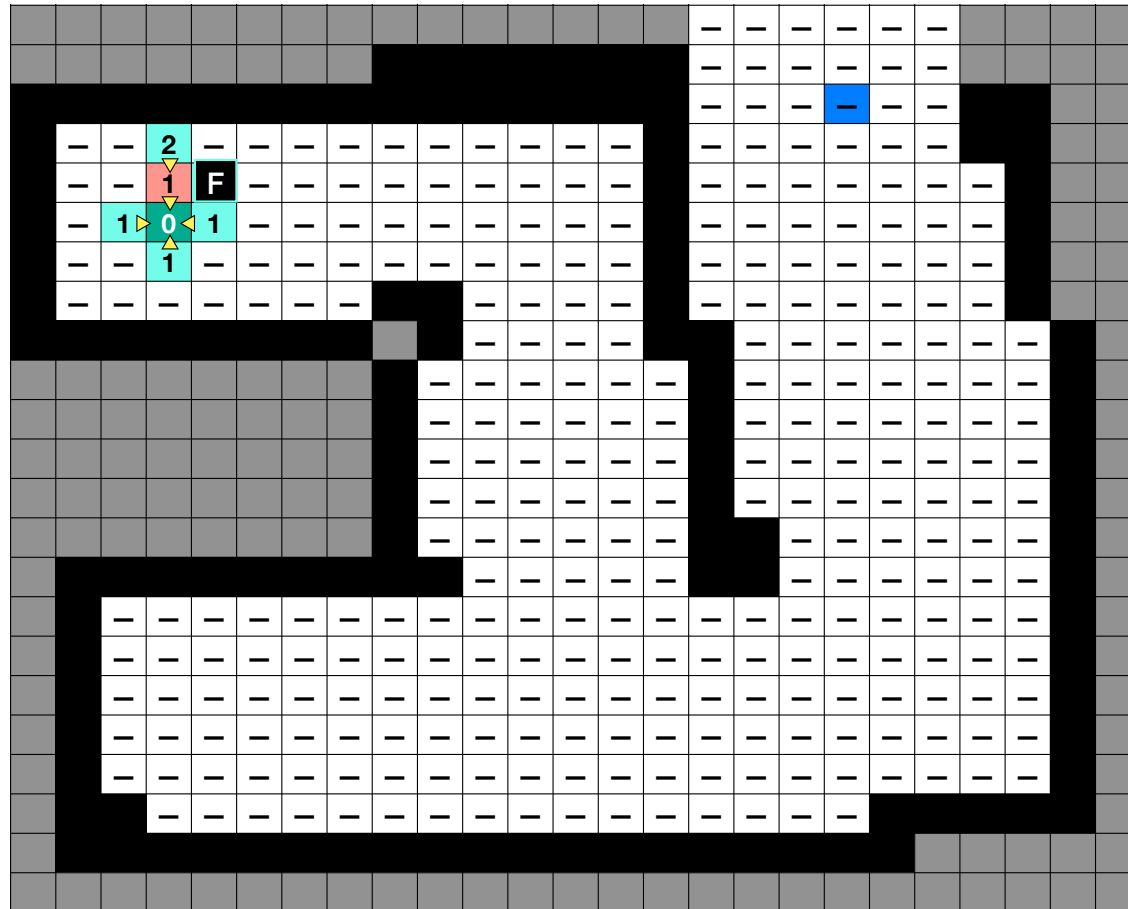
E D C B

A

current_node

**Process
current node**

**Queue second
neighbor**



visit_queue

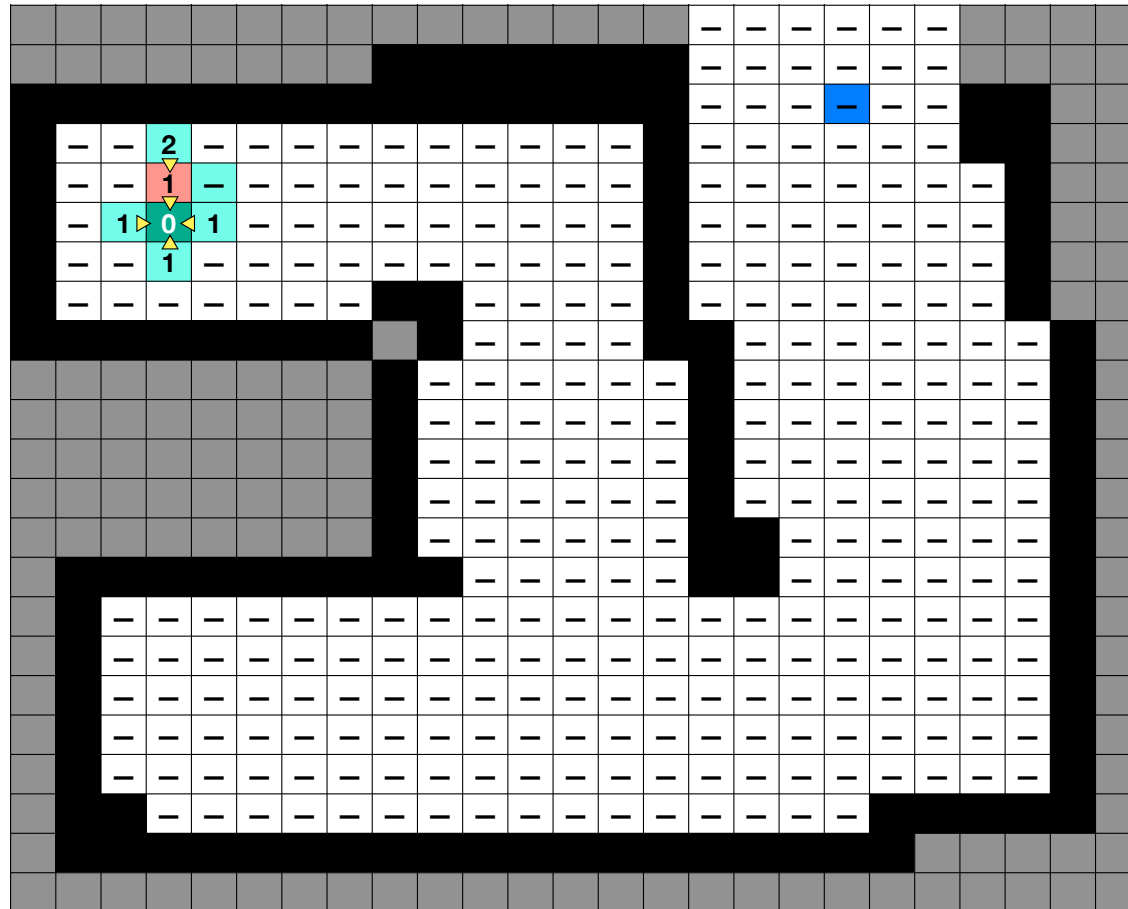
E	D	C	B
---	---	---	---

A

current_node

**Process
current node**

**Queue second
neighbor**



visit_queue

F	E	D	C	B
---	---	---	---	---

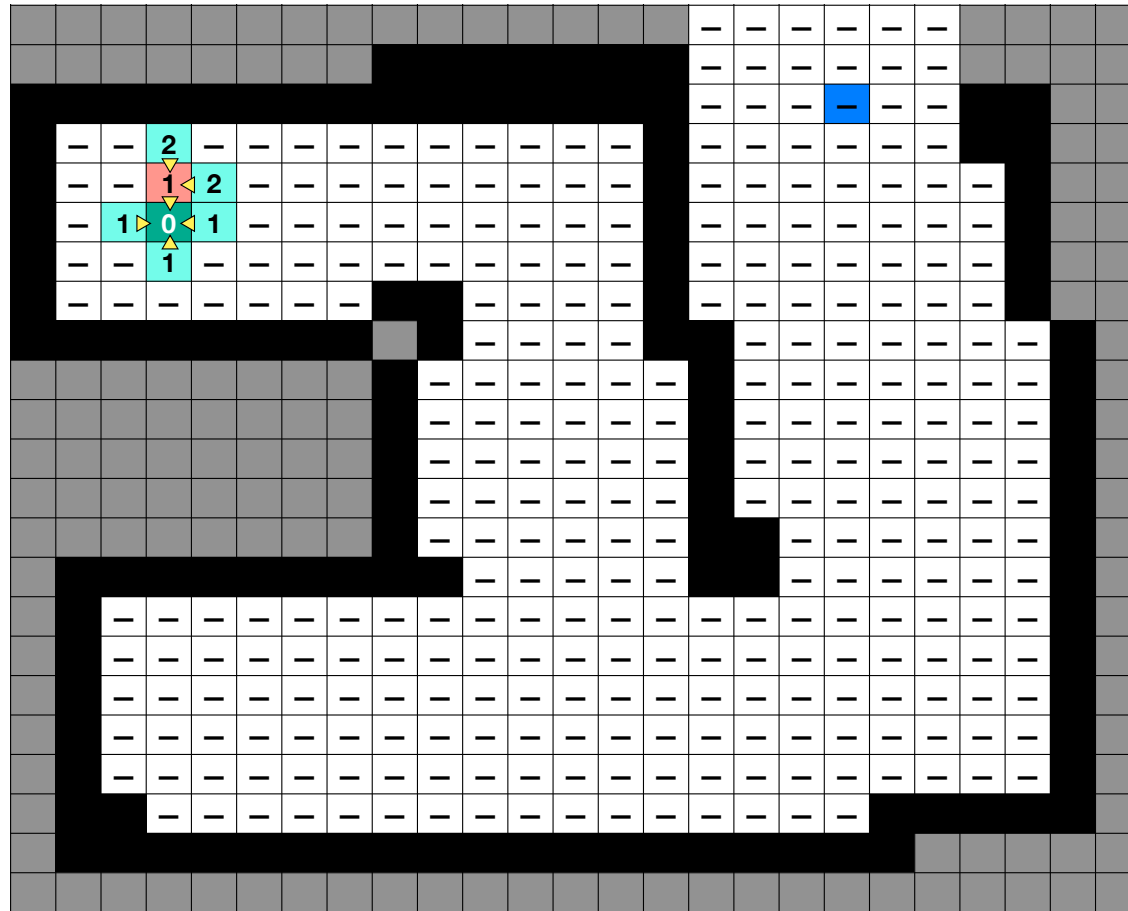
A

current_node

**Process
current node**

**Queue second
neighbor**

**Assign
distance and
parent**



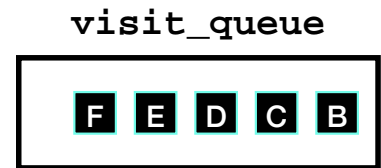
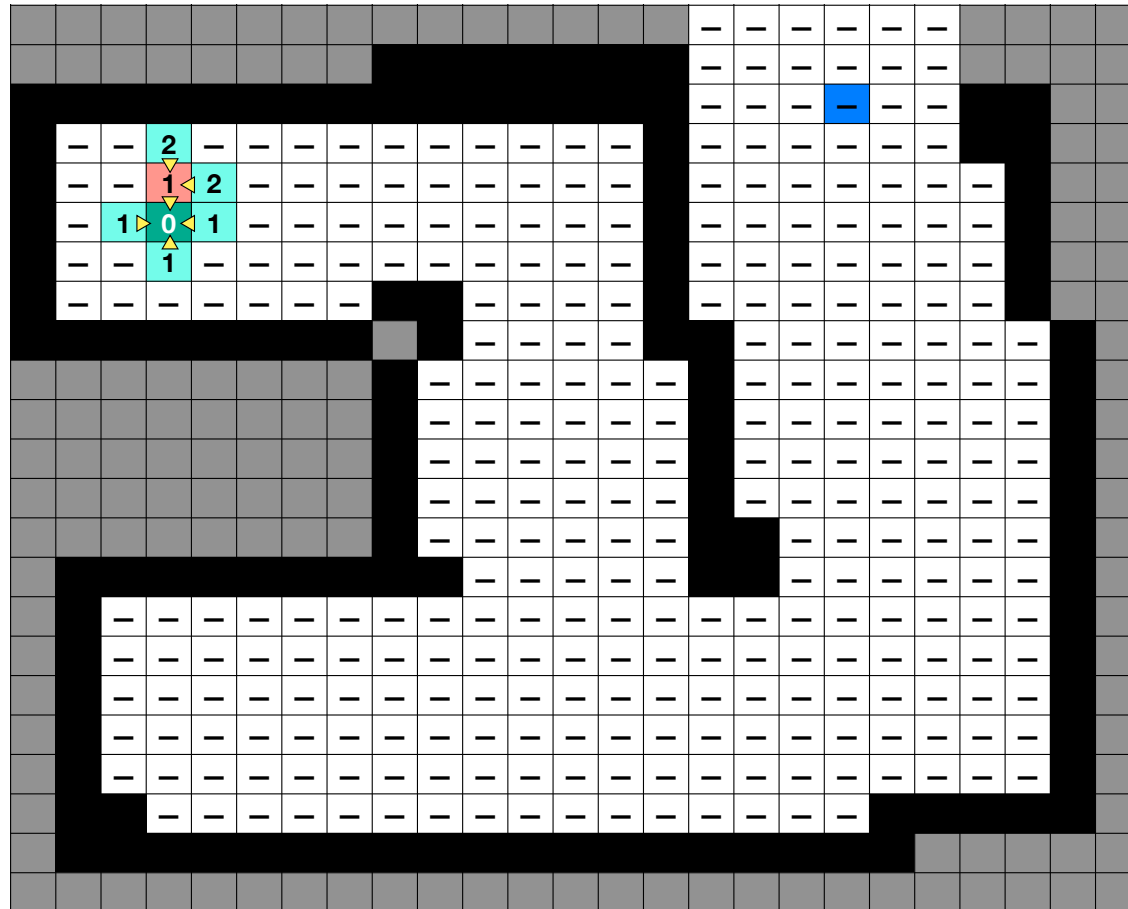
visit_queue

F	E	D	C	B
---	---	---	---	---

A
current_node

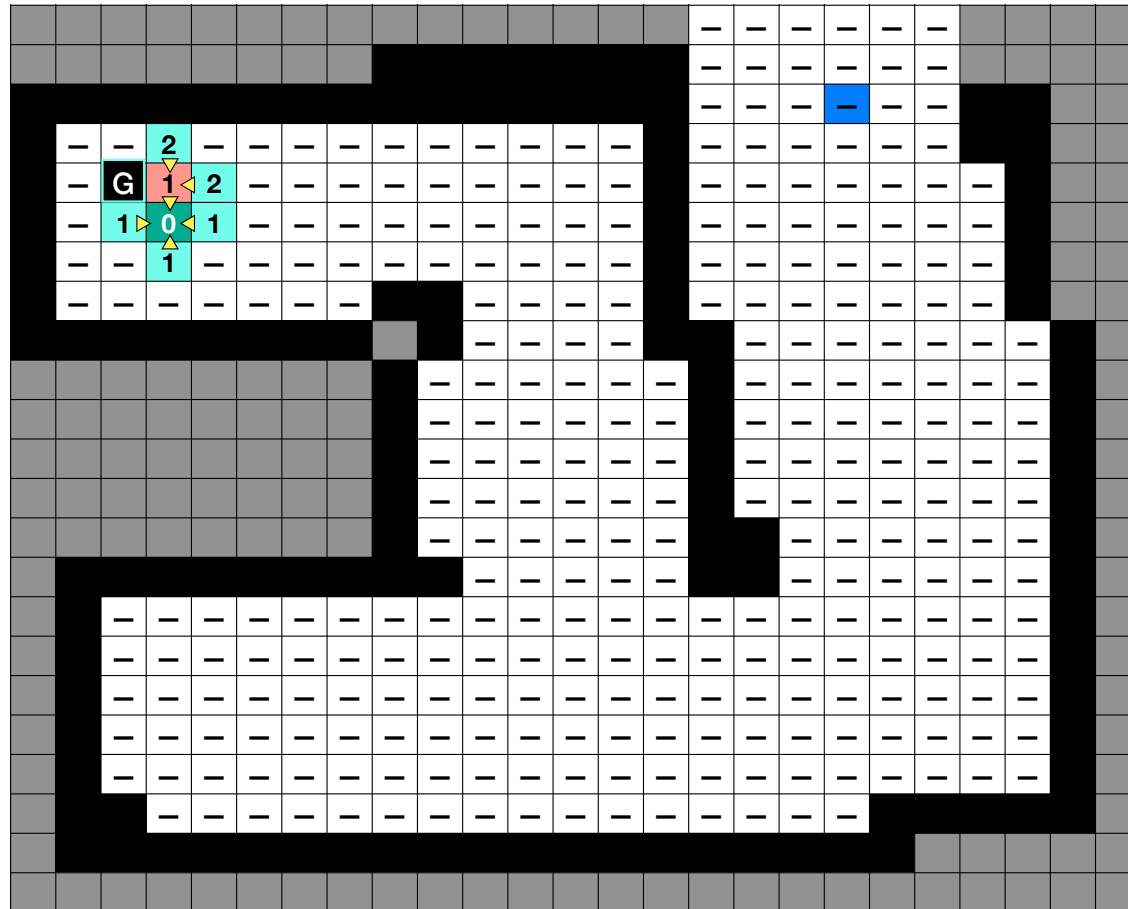
**Process
current node**

**Do not queue
third neighbor
(already
visited)**



**Process
current node**

**Queue last
neighbor**



visit_queue

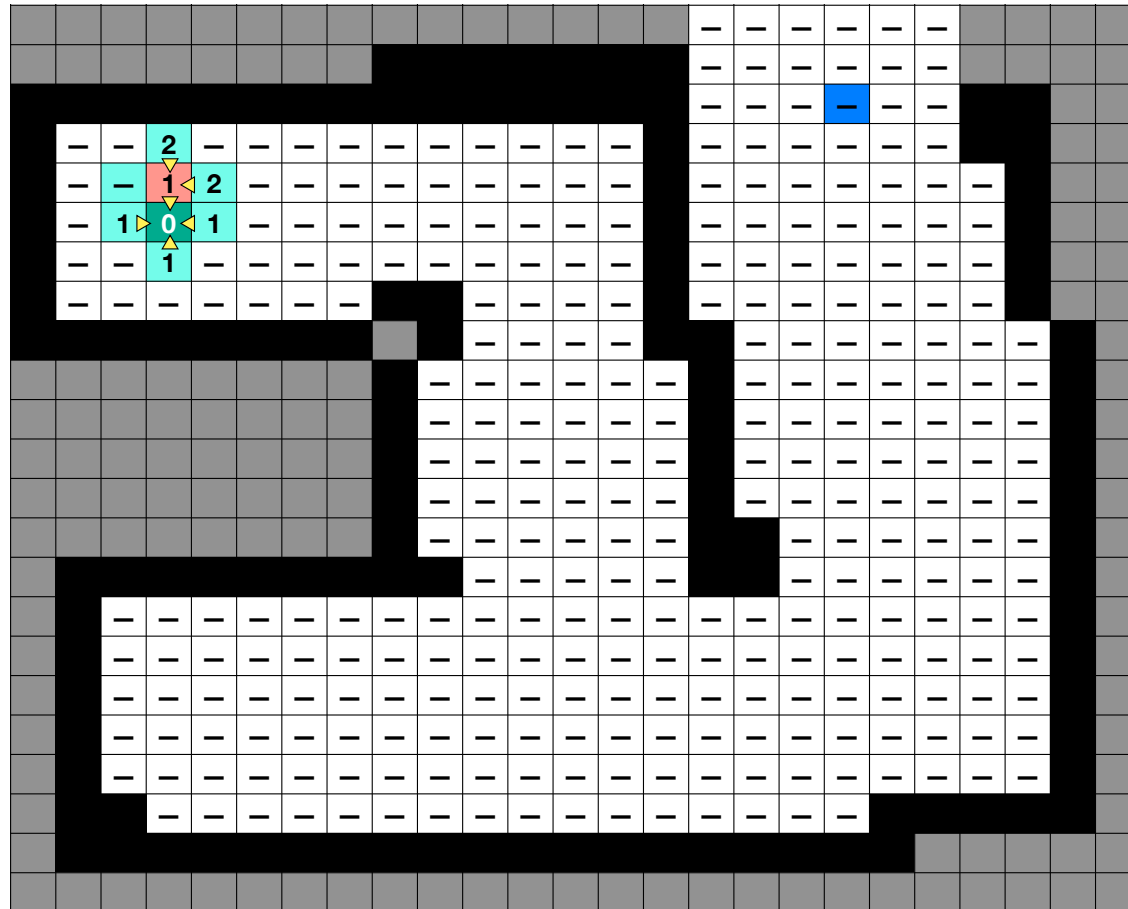


A

current_node

**Process
current node**

**Queue last
neighbor**



visit_queue



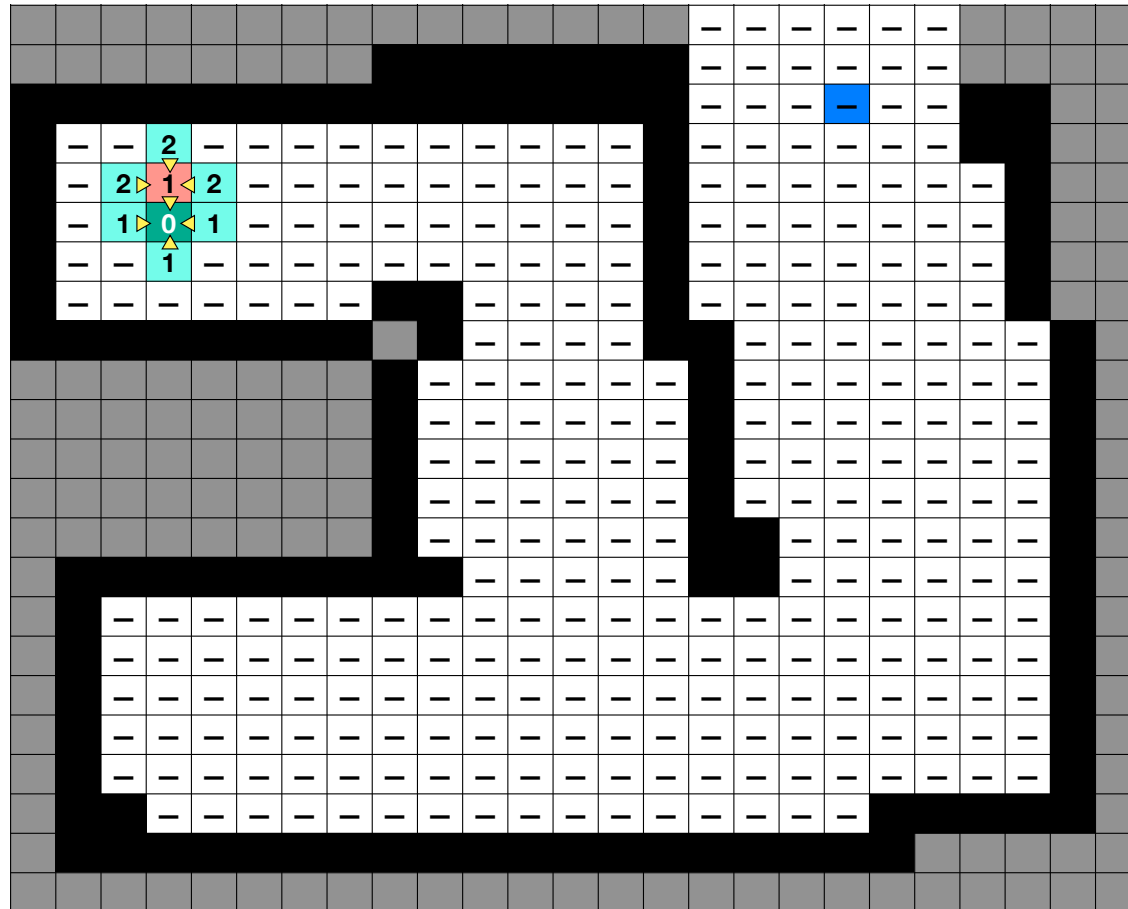
A

current_node

**Process
current node**

**Queue last
neighbor**

**Assign
distance and
parent**

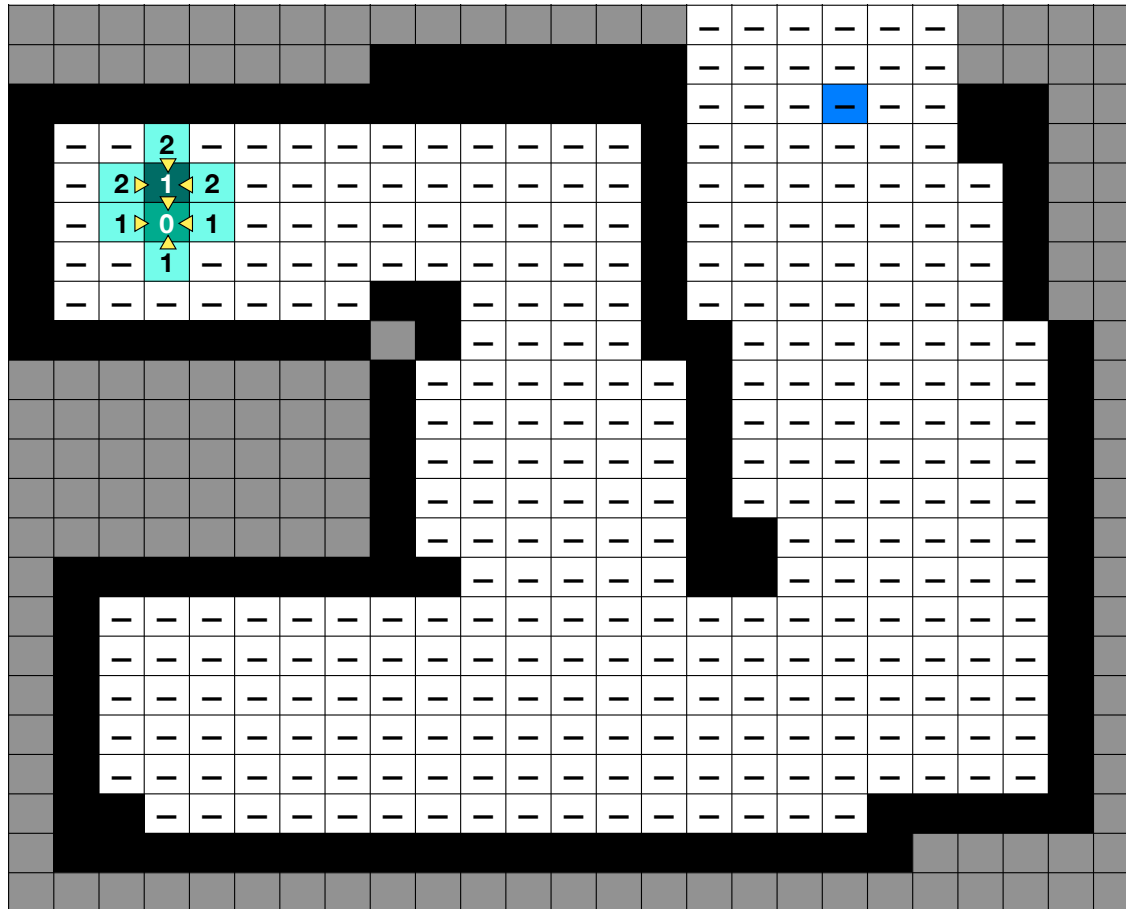


visit_queue



A

current_node



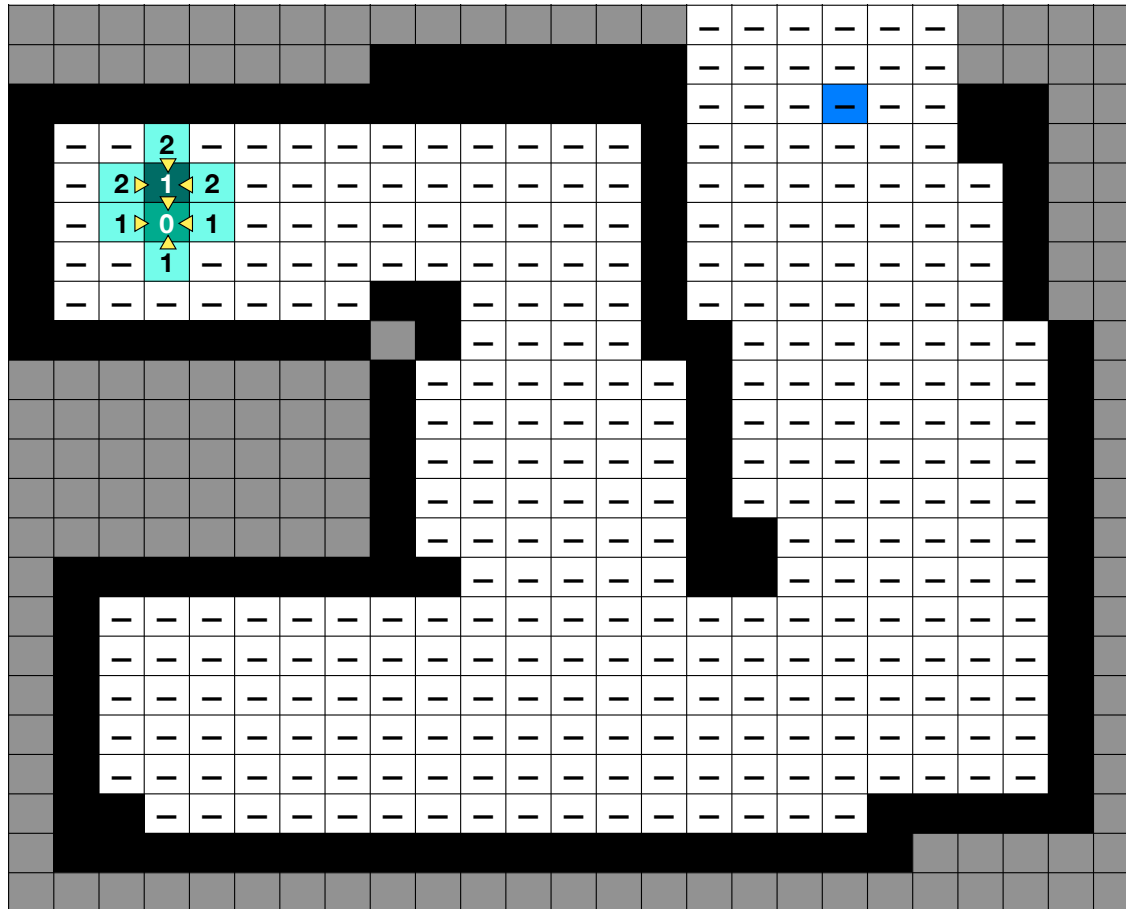
visit_queue



A

current_node

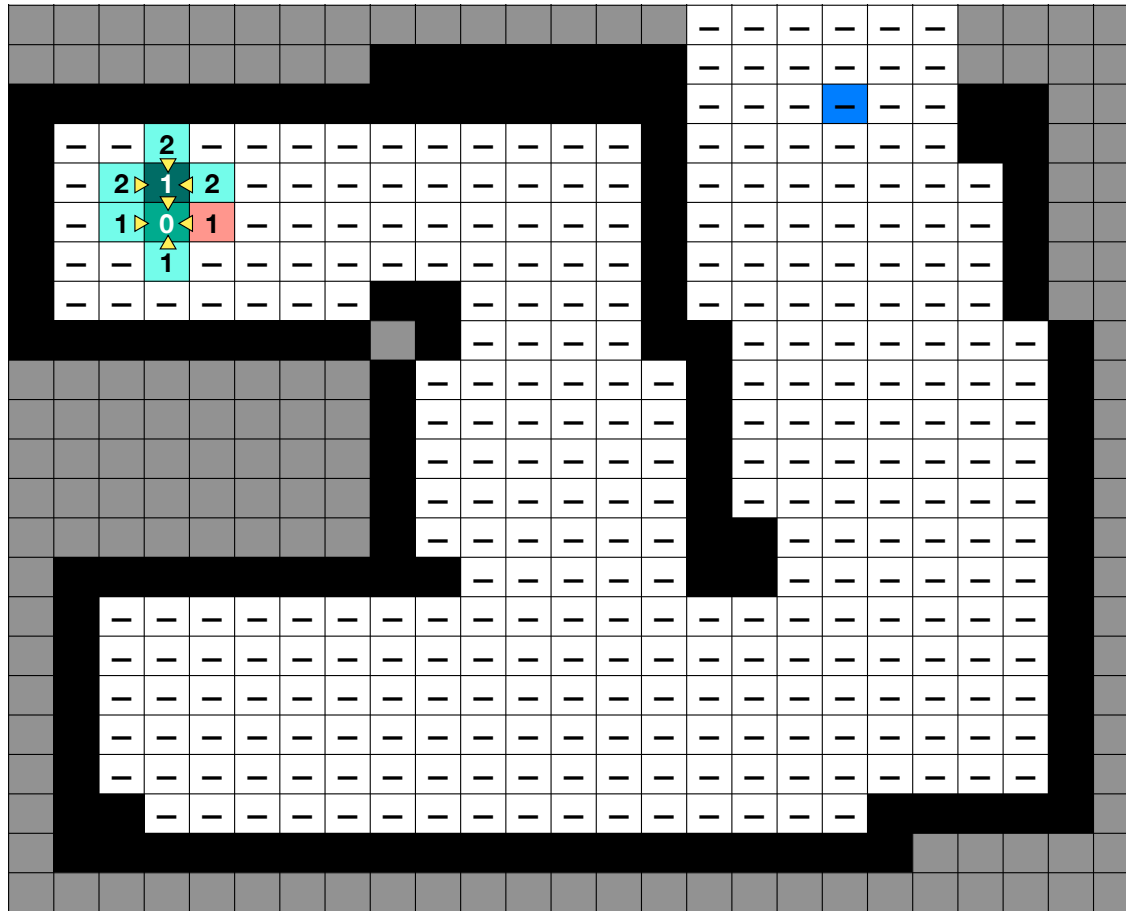
***Current node
fully processed***



visit_queue



current_node



visit_queue



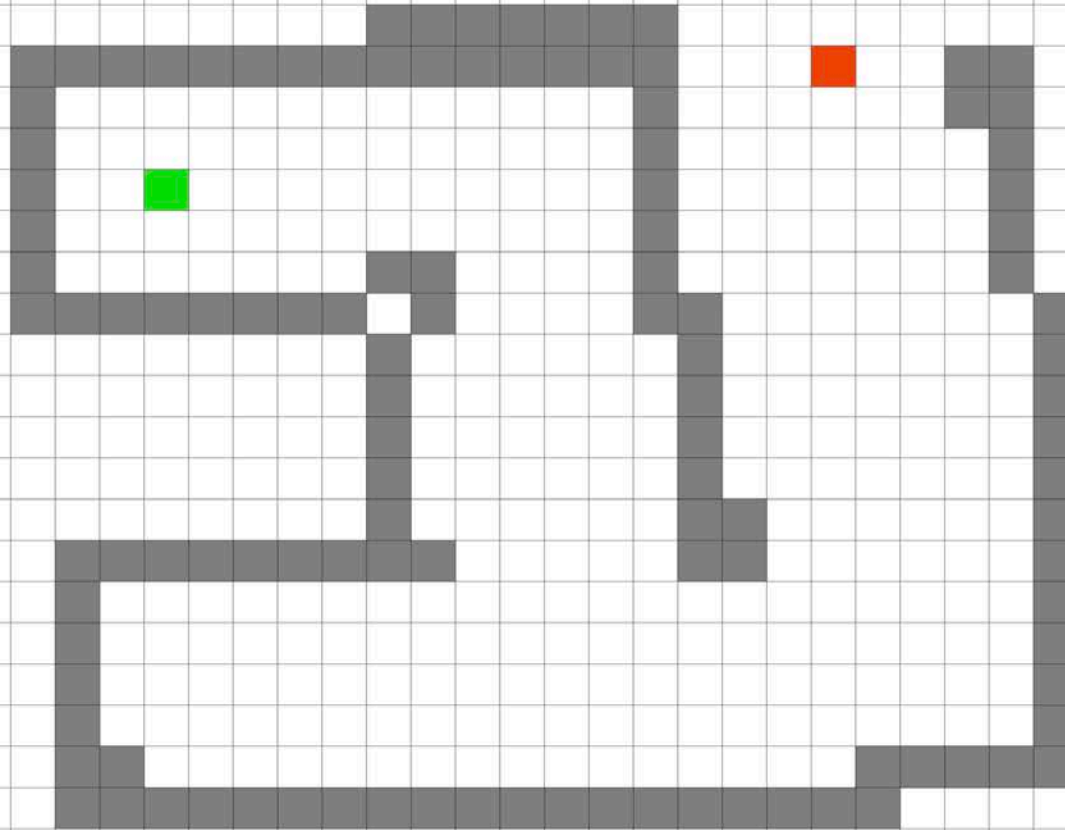
B

current_node

***Dequeue from
visit queue ...
process
continues***

Click within the white grid and drag your mouse to draw obstacles.
Drag the **green** node to set the start position.
Drag the **red** node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

<https://qiao.github.io/PathFinding.js/visual/>



A*

Heuristic

- Manha
- Euclid
- Octile
- Cheby

Options

- Allow
- Bi-dire
- Don't
- Wel

IDA*

Breadth-

Best-Firs

Dijkstra

Jump Po

Orthogo

Search

Trace

Start Search

generating grid 100%

qiao.github.io/PathFinding.js/visual/

Instructions

hide

Click within the white grid and drag your mouse to draw obstacles.
Drag the **green** node to set the start position.
Drag the **red** node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

Select Algorithm

A*

Heuristic

- Manhattan
- Euclidean
- Octile
- Chebyshev

Options

- Allow Diagonal
- Bi-directional
- Don't Cross Corners
- Weight

IDA*

Breadth-First-Search

Best-First-Search

Dijkstra

Jump Point Search

Orthogonal Jump Point Search

Trace

Start Search Pause Search Clear Walls

generating grid 100%

Project Hosted on [Github](#)

qiao.github.io/PathFinding.js/visual/

Instructions hide

Click within the white grid and drag your mouse to draw obstacles.
Drag the **green** node to set the start position.
Drag the **red** node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

Select Algorithm

- A*
- IDA*
- Breadth-First-Search**
 - Options
 - Allow Diagonal
 - Bi-directional
 - Don't Cross Corners
- Best-First-Search
- Dijkstra
- Jump Point Search
- Orthogonal Jump Point Search
- Trace

Restart Search Clear Path Clear Walls

length: 38
time: 1.5000ms
operations: 568

Project Hosted on [Github](#)

Considerations for BFS

Is any path that reaches the goal a good path?

How many cells do we need to visit?

Could we use another visit strategy?

qiao.github.io/PathFinding.js/visual/

Instructions hide

Click within the white grid and drag your mouse to draw obstacles.
 Drag the **green** node to set the start position.
 Drag the **red** node to set the end position.
 Choose an algorithm from the right-hand panel.
 Click Start Search in the lower-right corner to start the animation.

Select Algorithm

- > A*
- > IDA*
- v Breadth-First-Search
 - Options
 - Allow Diagonal
 - Bi-directional
 - Don't Cross Corners
- > Best-First-Search
- > Dijkstra
- > Jump Point Search
- > Orthogonal Jump Point Search
- > Trace

Restart Search Clear Path Clear Walls

length: 38
 time: 1.5000ms
 operations: 568

Project Hosted on [Github](https://github.com)

qiao.github.io/PathFinding.js/visual/

Instructions

Click within the white grid and drag your mouse to draw obstacles.
Drag the **green** node to set the start position.
Drag the **red** node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

hide



Select Algorithm

A*

Heuristic

- Manhattan
- Euclidean
- Octile
- Chebyshev

Options

- Allow Diagonal
- Bi-directional
- Don't Cross Corners
- Weight

IDA*

Breadth-First-Search

Best-First-Search

Dijkstra

Jump Point Search

Orthogonal Jump Point Search

Trace

Restart Search

Clear Path

Clear Walls

length: 38
time: 2.5000ms
operations: 309

Project Hosted on [Github](#)

qiao.github.io/PathFinding.js/visual/

Instructions hide
 Click within the white grid and drag your mouse to draw obstacles.
 Drag the green node to set the start position.
 Drag the red node to set the end position.
 Choose an algorithm from the right-hand panel.
 Click Start Search in the lower-right corner to start the animation.

Select Algorithm

- A*
 - Heuristic
 - Manhattan
 - Euclidean
 - Octile
 - Chebyshev
 - Options
 - Allow Diagonal
 - Bi-directional
 - Don't Cross Corners
 - Weight
- IDA*
- Breadth-First-Search
- Best-First-Search
- Dijkstra
- Jump Point Search
- Orthogonal Jump Point Search
- Trace

Restart Search Clear Path Clear Walls

length: 38
 time: 2.5000ms
 operations: 309

How does A-Star generate a shortest path while visiting fewer nodes?

Breadth-first Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor $>$ Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit **priority queue** if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

A-Star Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit priority queue if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

How do we implement a priority queue?

Then Update

What is a node's priority for A-Star?

distance to be distance of current node + cost to move

How do we implement a priority queue?

Topic for later courses in data structures (e.g., Michigan EECS 280)

Foreshadowing: use a binary heap

Considered an advanced extension for Project 3

What is a node's priority for A-Star?

How do we implement a priority queue?

Topic for later courses in data structures (e.g., Michigan EECS 280)

Foreshadowing: use a binary heap

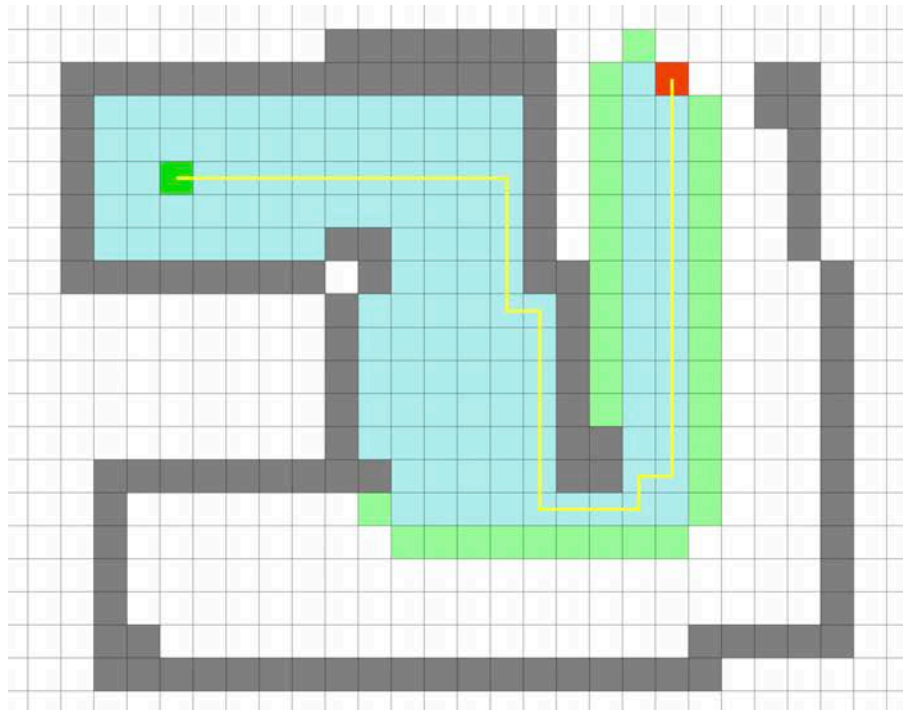
Considered an advanced extension for Project 3

What is a node's priority for A-Star?

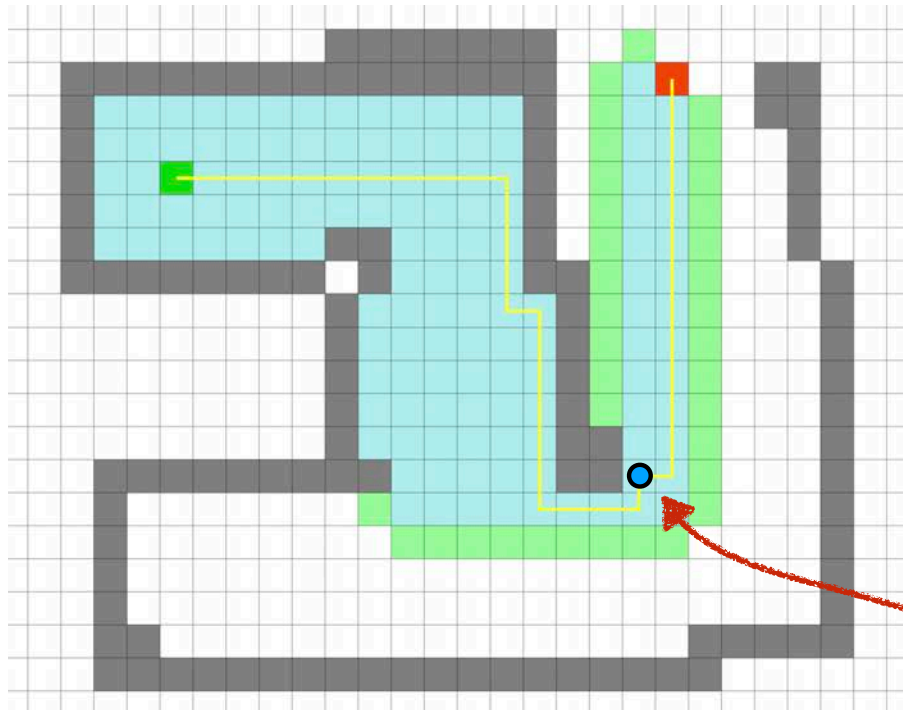
Use an optimistic heuristic for the best possible outcome

**Each node's priority is distance along path route to start +
best possible distance to goal**

**Each node's priority is distance along path route to start +
best possible distance to goal**

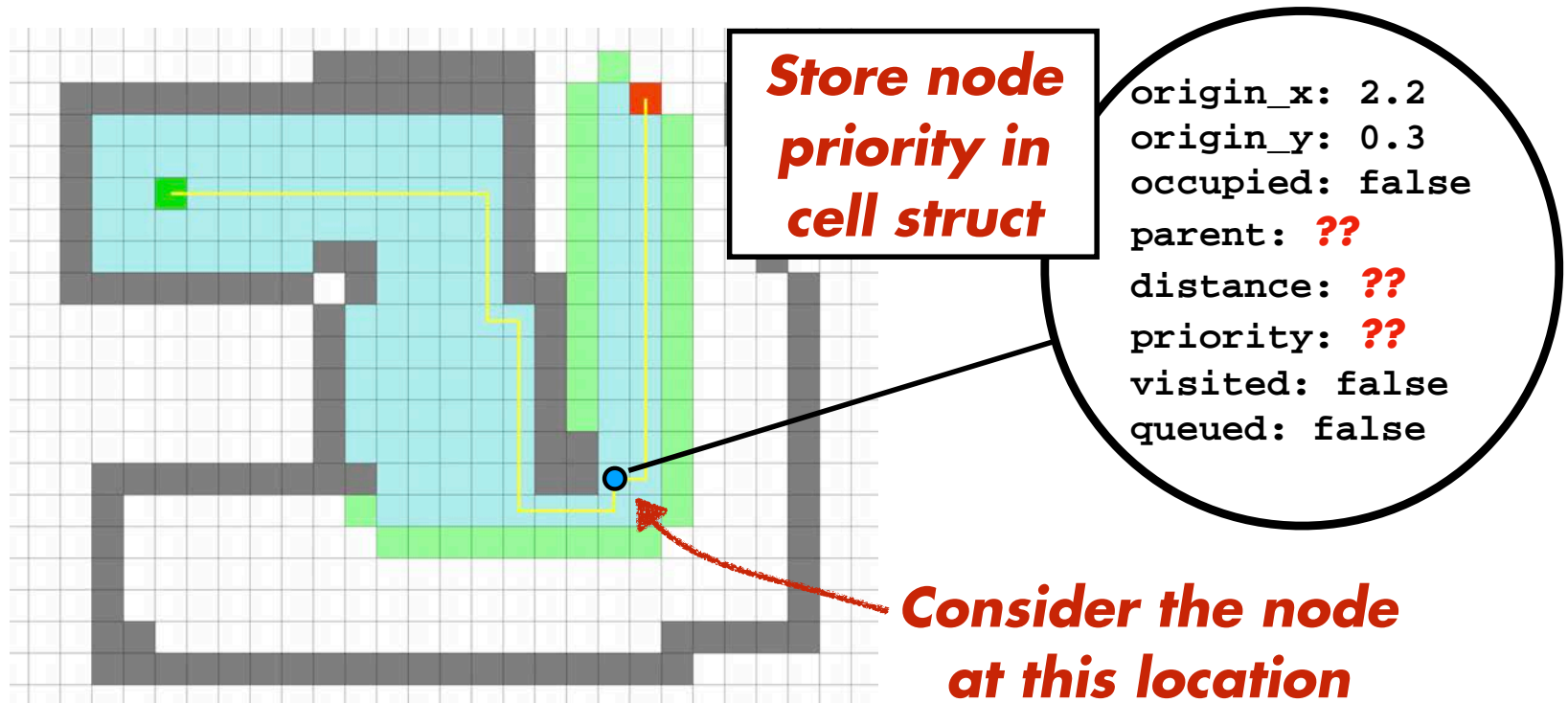


**Each node's priority is distance along path route to start +
best possible distance to goal**

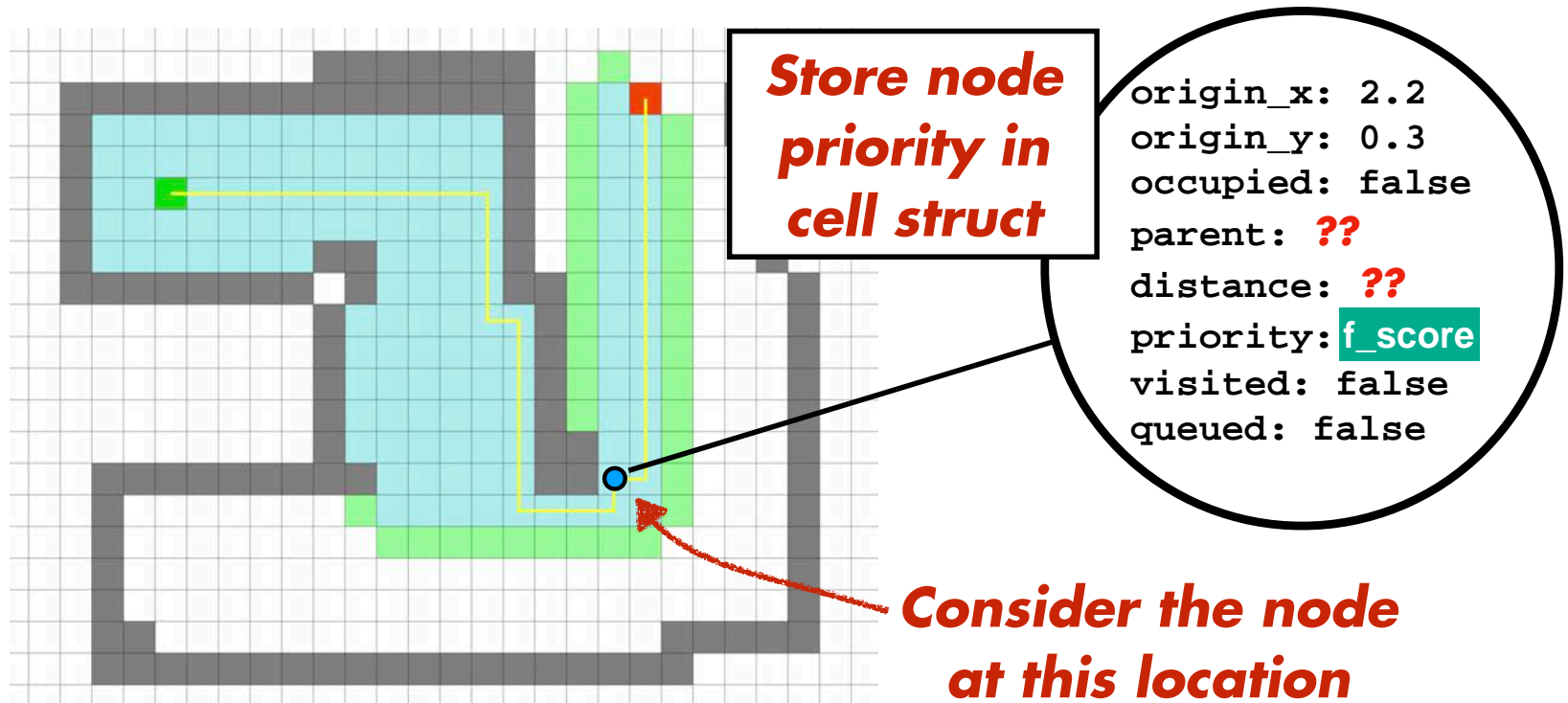


***Consider the node
at this location***

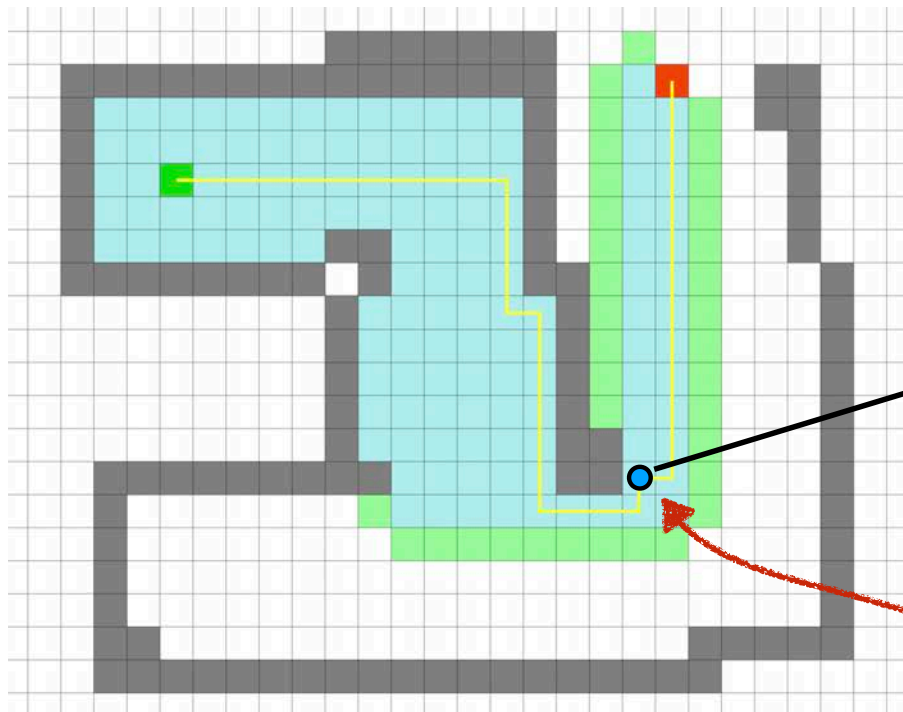
Each node's priority is distance along path route to start +
best possible distance to goal



Each node's priority is distance along path route to start +
best possible distance to goal



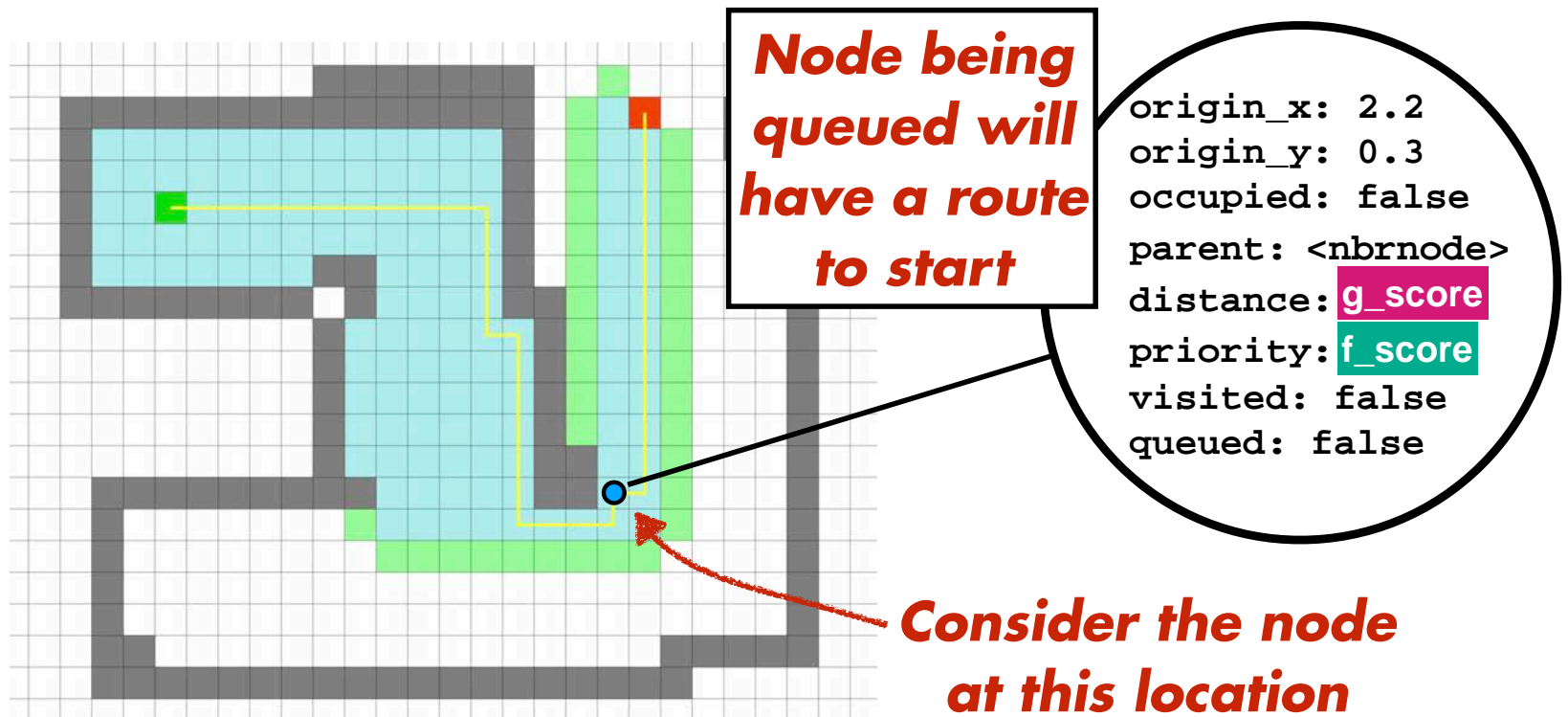
Each node's priority is distance along path route to start +
f_score best possible distance to goal



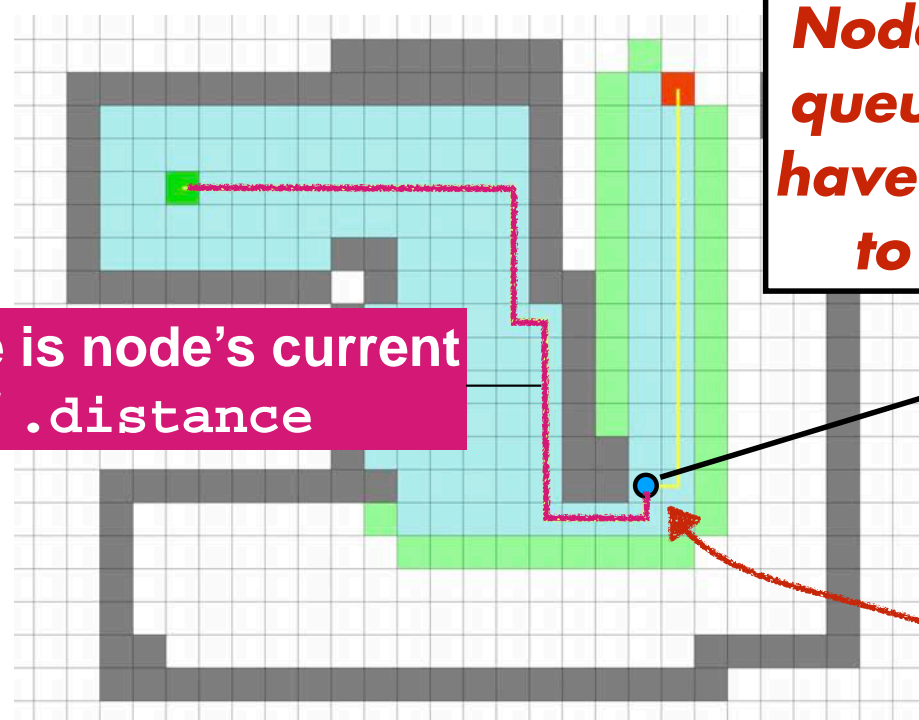
```
origin_x: 2.2  
origin_y: 0.3  
occupied: false  
parent: ??  
distance: ??  
priority: f_score  
visited: false  
queued: false
```

***Consider the node
at this location***

Each node's priority is distance along path route to start + **f_score** best possible distance to goal



Each node's priority is distance along path route to start +
g_score
f_score best possible distance to goal



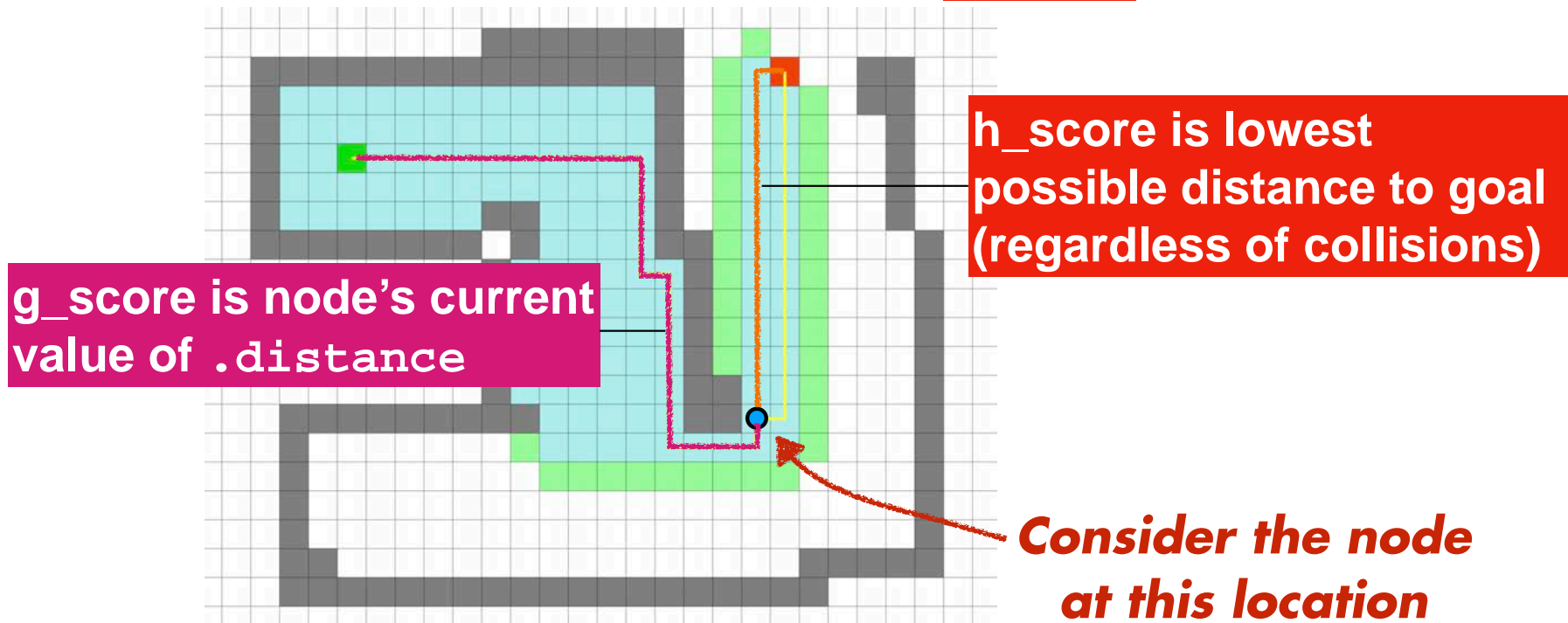
g_score is node's current value of `.distance`

Node being queued will have a route to start

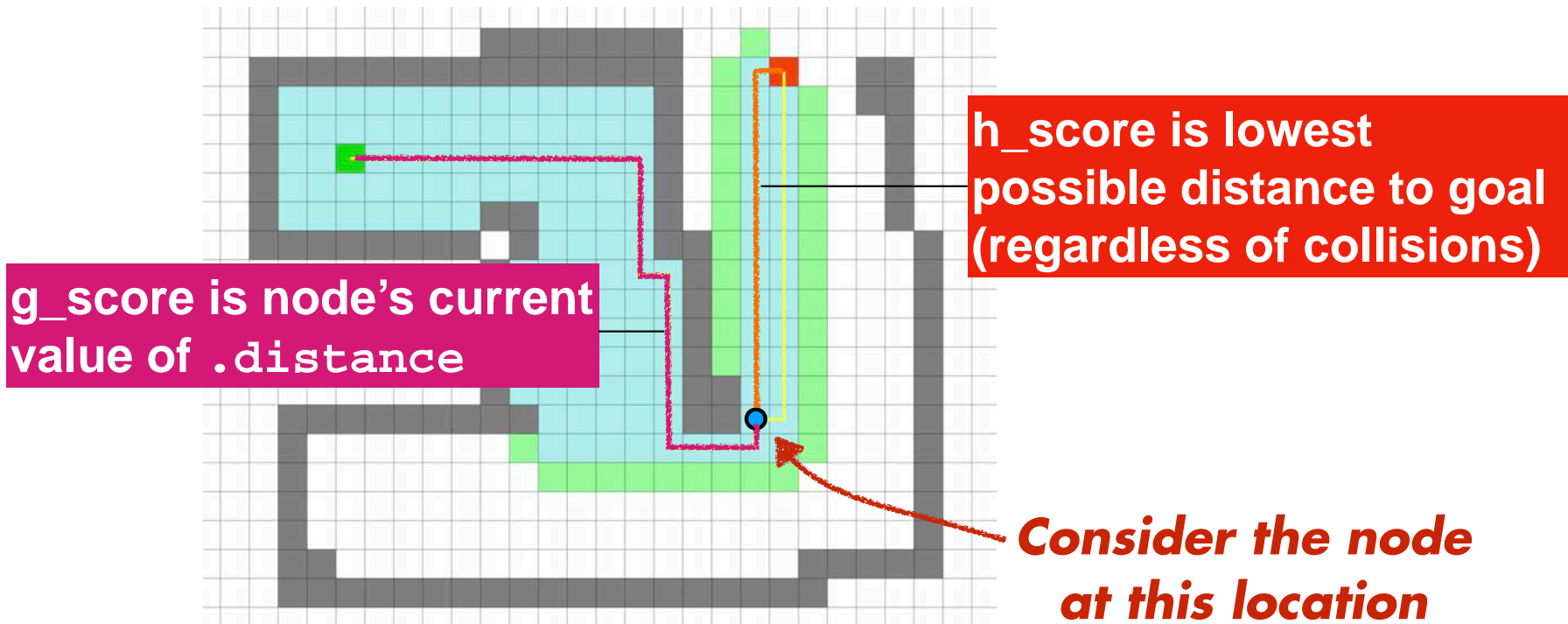
```
origin_x: 2.2  
origin_y: 0.3  
occupied: false  
parent: <nbrnode>  
distance: g_score  
priority: f_score  
visited: false  
queued: false
```

Consider the node at this location

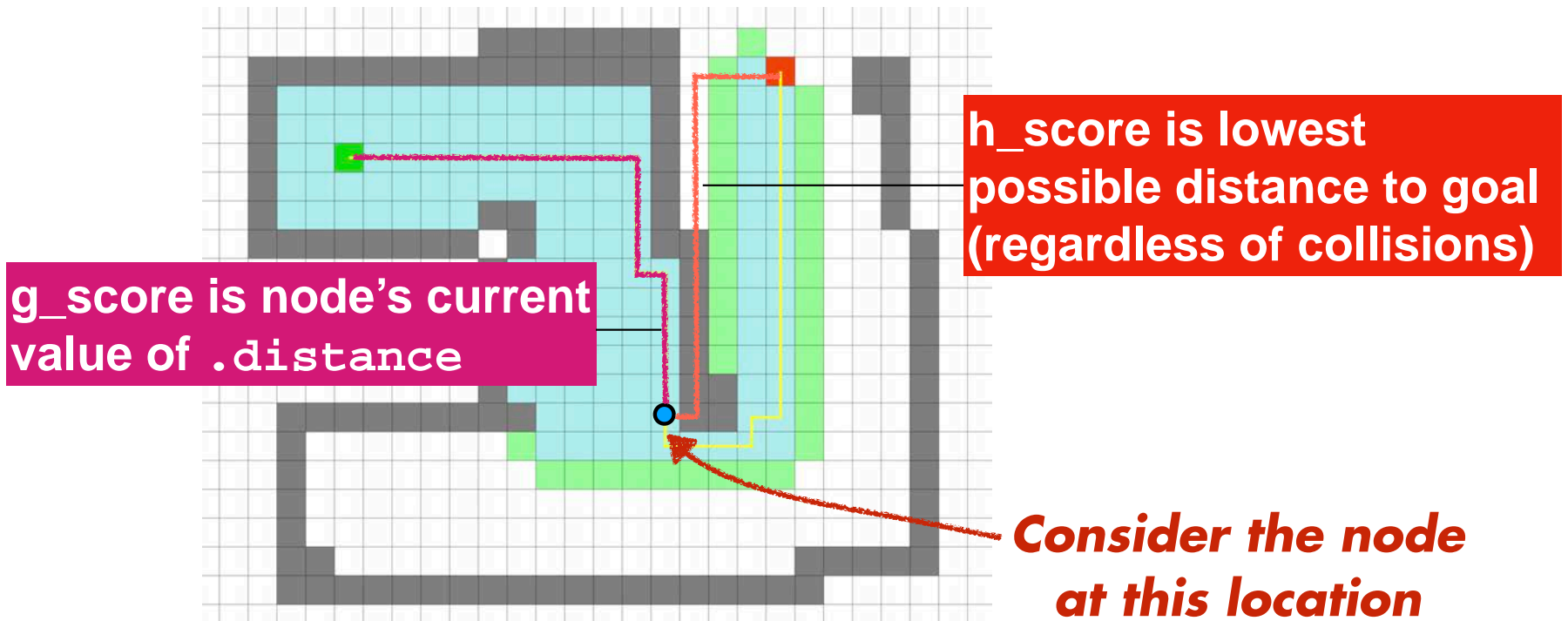
Each node's priority is distance along path route to start +
f_score best possible distance to goal
g_score
h_score



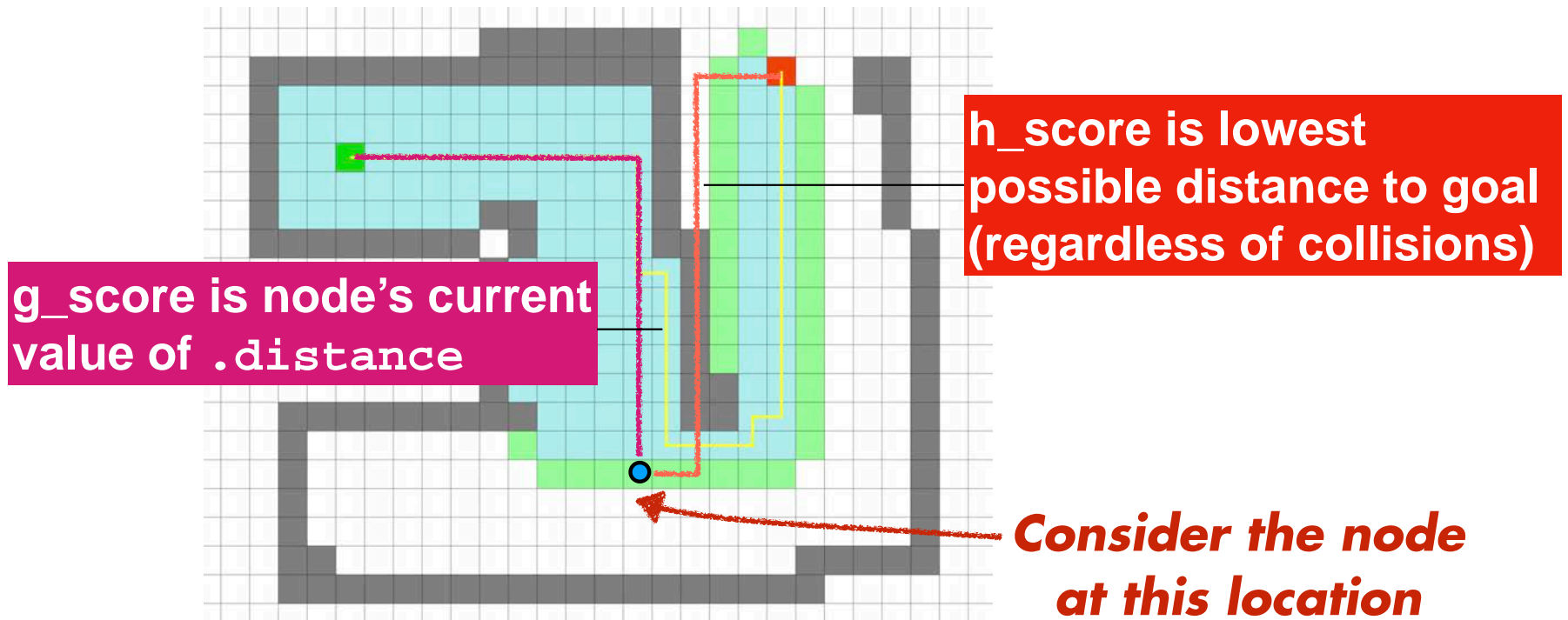
$$\begin{matrix} \text{.priority} \\ \text{f_score} \end{matrix} = \begin{matrix} \text{.distance} \\ \text{g_score} \end{matrix} + \begin{matrix} \text{h_score} \end{matrix}$$



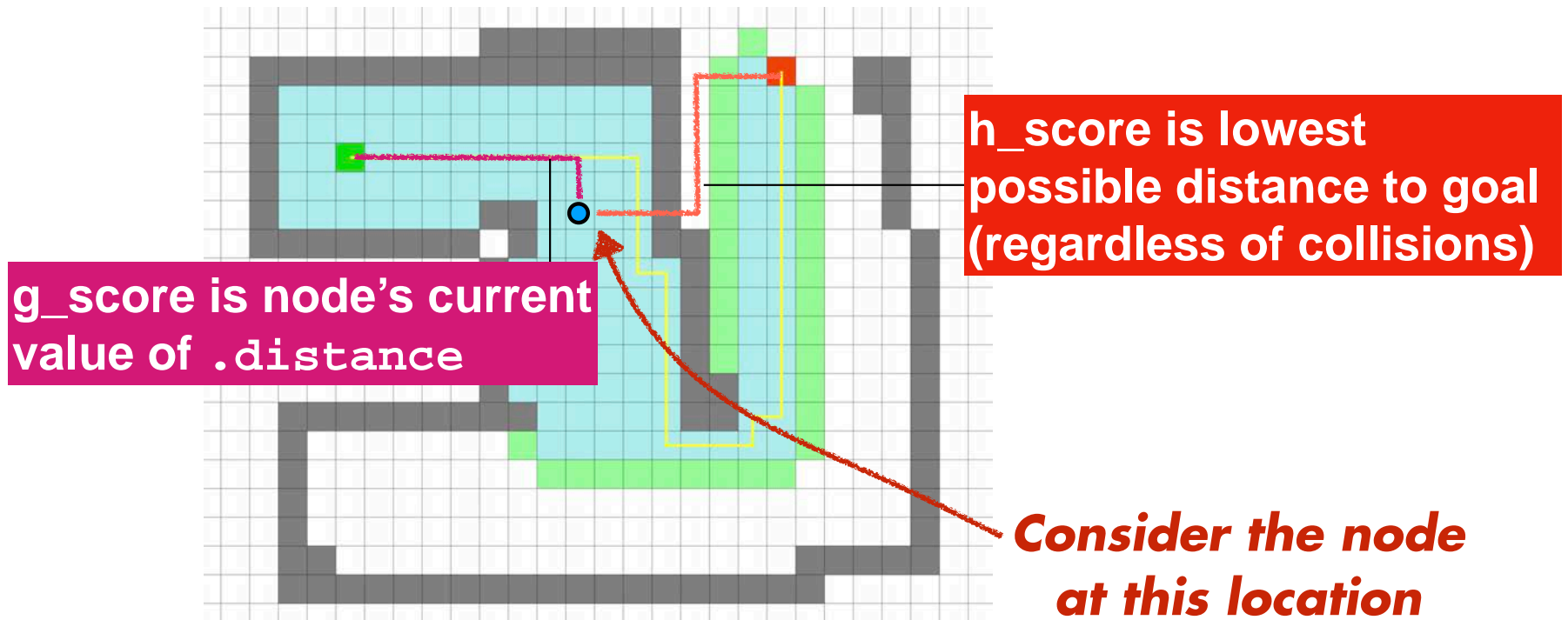
$$\begin{matrix} \text{.priority} \\ \mathbf{f_score} \end{matrix} = \begin{matrix} \text{.distance} \\ \mathbf{g_score} \end{matrix} + \begin{matrix} \mathbf{h_score} \end{matrix}$$

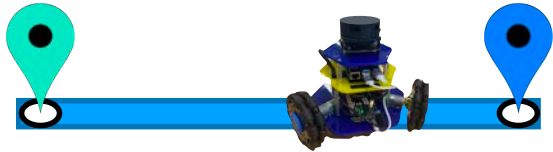


$$\begin{matrix} \text{.priority} \\ \mathbf{f_score} \end{matrix} = \begin{matrix} \text{.distance} \\ \mathbf{g_score} \end{matrix} + \begin{matrix} \mathbf{h_score} \end{matrix}$$



$$\begin{matrix} \text{.priority} \\ \mathbf{f_score} \end{matrix} = \begin{matrix} \text{.distance} \\ \mathbf{g_score} \end{matrix} + \begin{matrix} \mathbf{h_score} \end{matrix}$$





What options do we have for navigating our robot?

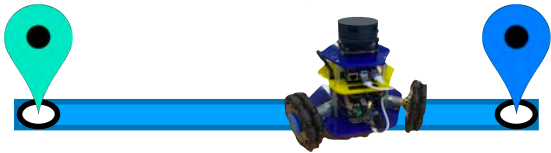
Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths

Robot that plans paths using global search ?



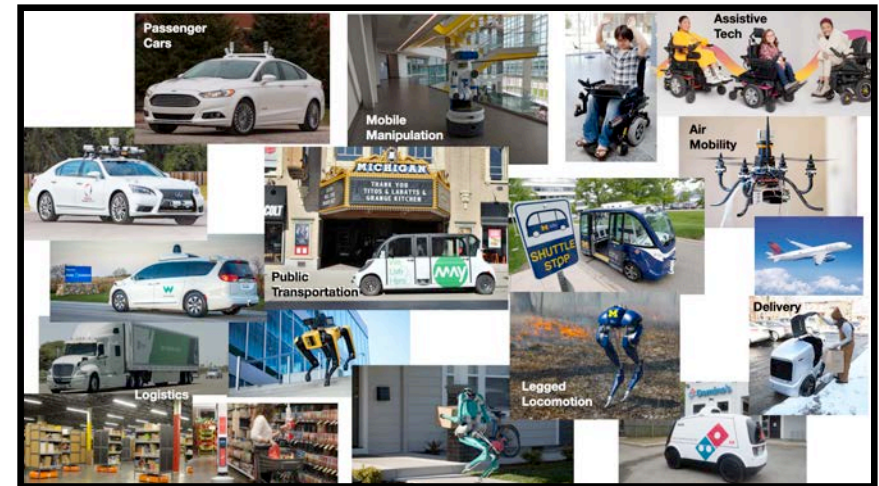
What options do we have for navigating our robot?

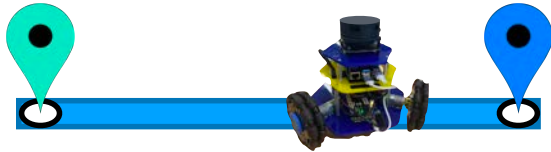
Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths





What options do we have for navigating our robot?

Just move randomly

Follow wall to goal

Build a map to guide us

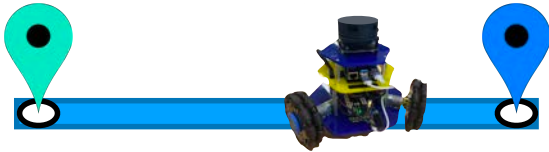
Search over all possible paths

+ Complete algorithm
(guarantees correct answer)

+ Optimal path

- Expensive

- Responsiveness



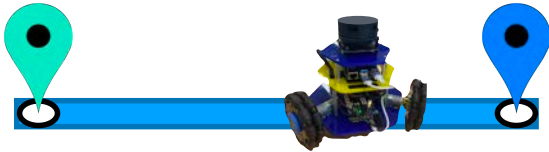
What options do we have for navigating our robot?

Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths



**What options do we have
for navigating our robot?**

Random Walk

Bug Algorithm

Local Search

Global Search

Reaction

Deliberation



Random Walk

Bug Algorithm

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Random Walk

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Random Walk

- + Cheap
- + Simple
- + Robust
- Slow

Bug Algorithm

- + Simple
- + Reliable
- Known goal location
- Forgetful

Local Search

- + Adaptable
- Requires SLAM
- Gets stuck

- + Complete
- + Optimal
- Expensive
- Responsive

Global Search

Reaction

Deliberation



Inexpensive

Overhead vs. Optimality

Complete

Simple

Speed vs. Guarantees

Thorough

Dynamic

Responsiveness to environment

Adaptable

*There is no one right algorithm.
There is a larger world of possibilities.*

Inexpensive

Overhead vs. Optimality

Complete

Simple

Speed vs. Guarantees

Thorough

Dynamic

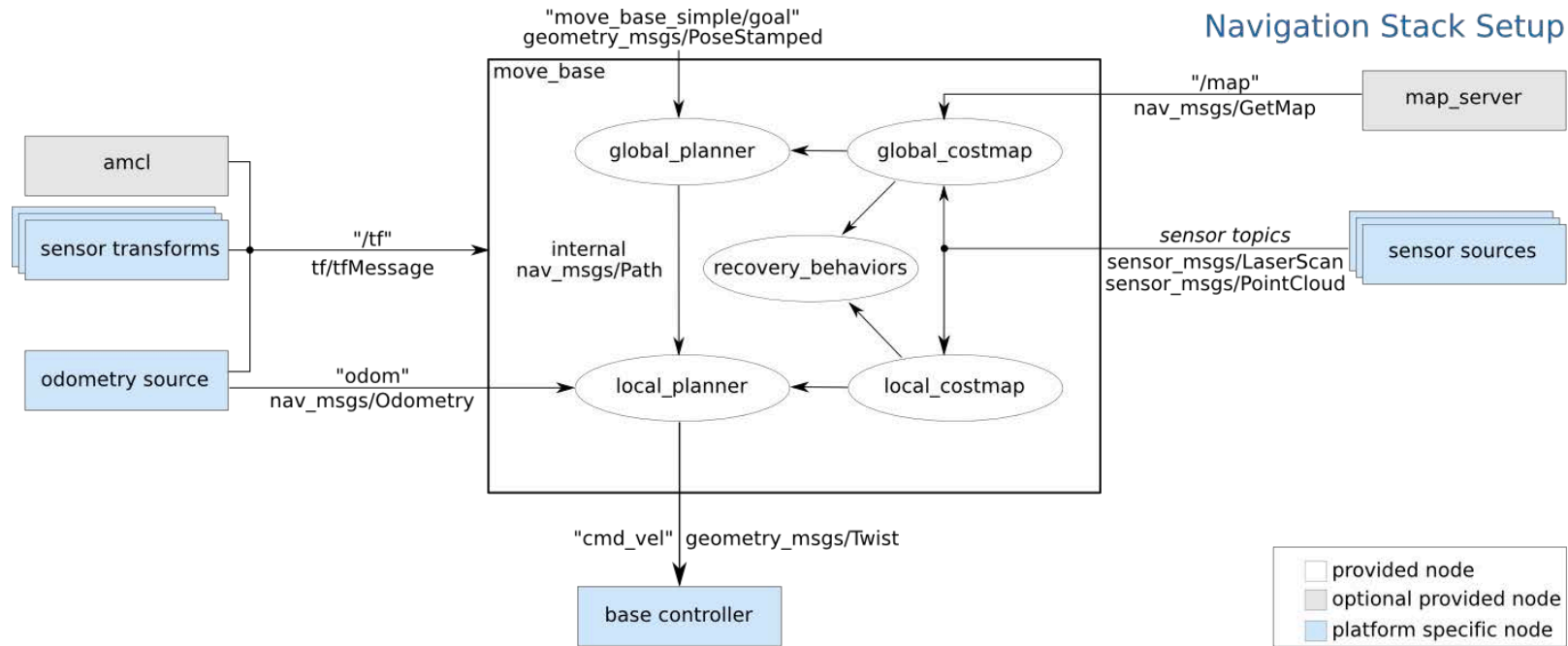
Responsiveness to environment

Adaptable

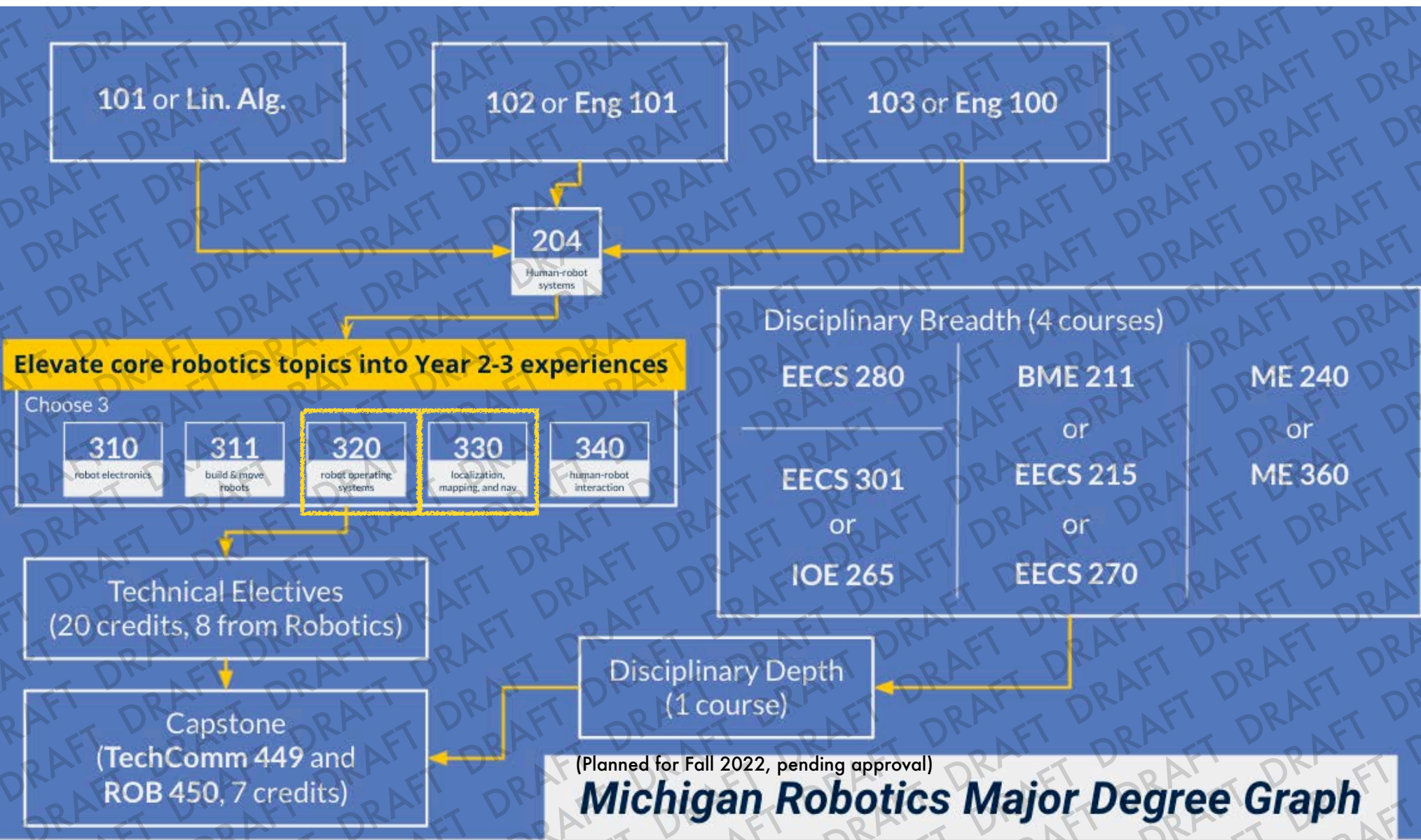
Reaction

Deliberation

navigation/ Tutorials/ RobotSetup



Navigation in Robot Operating Systems



Michigan Robotics Major Degree Graph

101 or Lin. Alg.

102 or Eng 101

103 or Eng 100

204
Human-robot systems

Robotics 320: Planning for mobile manipulation robots



Robotics 330: Build SLAM system of your own

Technical Electives
(20 credits, 8 from Robotics)

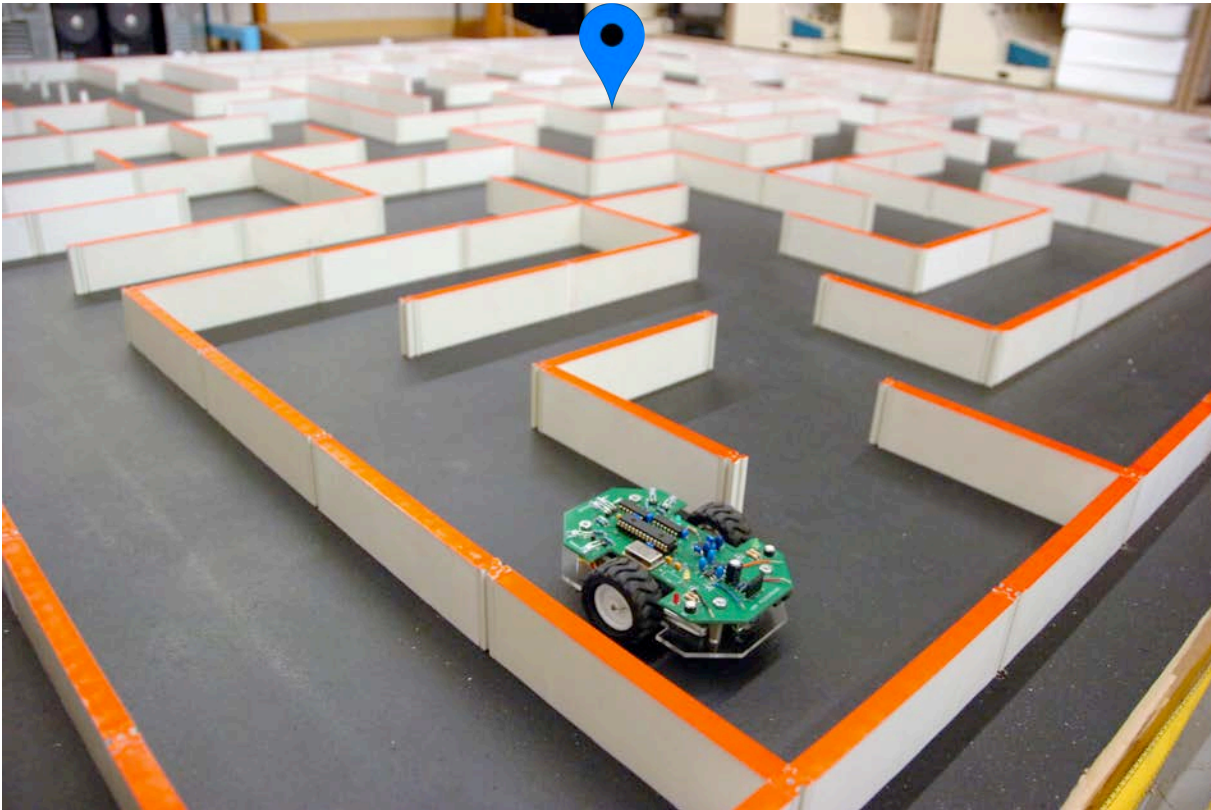
Disciplinary Depth
(1 course)

Capstone
(TechComm 449 and
ROB 450, 7 credits)

(Planned for Fall 2022, pending approval)

Michigan Robotics Major Degree Graph

Autonomous Navigation: Global Search



<https://app.emaze.com/@AIRRTROT/idea-2-the-robot-maze#1>

Robotics 102
Introduction to AI and Programming
University of Michigan and Berea College
Fall 2021

Michigan Robotics 102 - robotics102.org